LARGE LANGUAGE MODELS STILL CAN'T PLAN (A BENCHMARK FOR LLMS ON PLANNING AND REASONING ABOUT CHANGE)

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ABSTRACT

The recent advances in large language models (LLMs) have transformed the field of natural language processing (NLP). From GPT-3 to PaLM, the state-of-the-art performance on natural language tasks is being pushed forward with every new large language model. Along with natural language abilities, there has been a significant interest in understanding whether such models, trained on enormous amounts of data, exhibit reasoning capabilities. Hence there has been interest in developing benchmarks for various reasoning tasks and the preliminary results from testing LLMs over such benchmarks seem mostly positive. However, the current benchmarks are relatively simplistic and the performance over these benchmarks cannot be used as an evidence to support, many a times outlandish, claims being made about LLMs' reasoning capabilities. As of right now, these benchmarks only represent a very limited set of simple reasoning tasks and we need to look at more sophisticated reasoning problems if we are to measure the true limits of such LLM-based systems. With this motivation, we propose an extensible assessment framework to test the abilities of LLMs on a central aspect of human intelligence, which is reasoning about actions and change. We provide multiple test cases that are more involved than any of the previously established reasoning benchmarks and each test case evaluates a certain aspect of reasoning about actions and change. Initial evaluation results on the base version of GPT-3 (Davinci), showcase subpar performance on these benchmarks.

1 Introduction

It would be no exaggeration to say that transformer-based large language models (LLMs) have revolutionized the field of natural language processing (NLP). Kicked off by the advances presented by the GPT-x models developed by OpenAI [20], these types of language models currently provide state-of-the-art performance in many of the standard NLP tasks. The latest version of the system, GPT-3 [3] uses about 175 billion parameters and was trained over an extremely large natural language training corpus, consisting of among other things excerpts from Wikipedia. Triggered by GPT-3, a plethora of other large language models, which are different variants of the transformer architecture [28], have been developed. Some of the most powerful ones are PaLM [4], GLaM [6], Megatron-Turing NLG [23], Meta-OPT [31], Gopher [21], LaMDA [27] and Chinchilla [9]. PaLM currently provides the state-of-the-art performance in NLP tasks such as natural language translation, predicting long-range text dependencies and even translation to structured representations [4].

Although LLMs were originally developed mostly to do language completion tasks, with no guarantees about the completion beyond its coherence, there have been increasing claims that they can do other tasks including explaining jokes [13]. Of particular interest are the thread of efforts that aim to evaluate (and showcase) LLM's ability to do reasoning tasks. For example, there are many claims centered around the fact that GPT-3 may possess some form of reasoning ability [15]. Such sources generally assume that by learning to model a large amount of real-world text, it may have acquired some approximation of simple reasoning. This sparked interest in evaluating the large language models on various reasoning tasks including common-sense reasoning [26, 22, 7], logical reasoning [24], and even ethical reasoning [12]. The macro-tenor of the drumbeat of these works has been suggesting that LLM's are indeed capable of doing many kinds of reasoning [14, 30, 4]

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In this paper, we take a look at the ability of large language models to do reasoning about actions and change which involve common-sense planning tasks. We develop a suit of benchmarks¹, based on the kinds of domains employed in the International Planning Competition, to test these capabilities. Our focus on this specific task is spurred by not only the fact that reasoning about actions and change is a core aspect of human intelligence, but also that it is required for many of the tasks considered as potential applications of LLMs including automatic code generation, moral and even deontological reasoning [8].

We are not the first to point out the need to perform such analyses of the reasoning capabilities of GPT-3 like LLMs. For example, [17] performed an analysis of GPT-3's reasoning capabilities on some example tasks, including different commonsense reasoning tasks varying from biological reasoning to arithmetic reasoning. However, the goal of this paper is fundamentally distinct from these earlier works in multiple ways. In particular, we are not merely trying to point out a few example cases where GPT-3 fails but rather help establish an assessment framework for evaluating these systems' capabilities to perform reasoning about actions and change. While this paper reports the results of testing the vanilla GPT-3 system (specifically Davinci), one could in the future use the framework to analyse other LLMs that may be fine-tuned for such tasks. Secondly, through this framework we are also trying to eliminate the subjective aspect of analysis that forms the core part of many of these earlier efforts. Instead, we will try to automate and perform the analyses in a mechanistic way by leveraging automated planning models and tools to generate the queries and validate the system's answers. Finally, we propose a curriculum for evaluating reasoning about actions and change, wherein we identify a set of related but distinct reasoning tasks, that are central for an agent to successfully perform reasoning about actions and change and introduce a framework for developing code meant to auto-generate the possible queries for each. The conclusion from our evaluation of GPT-3 on these benchmarks is that LLM's are quite far from doing common planning/reasoning tasks that pose no issues to lay people (in particular our benchmarks don't require complex long-chain combinatorial reasoning).

The contributions of this paper are thus to

- 1. Provide an extensible suite of benchmarks for evaluating planning/reasoning capabilities of LLMs
- 2. Show that GPT-3 has pretty dismal performance on these benchmarks.

Our hope is that these benchmarks would spur other researchers to evaluate out-of-the-box or fined-tuned versions of other LLMs on these planning tasks.

2 Current Reasoning Benchmarks for LLMs

The currently available benchmarks, we believe, are insufficient to be able to make substantive claims about LLMs' ability to reason. The authors of [21] had pointed out that even language models at the scale of 100B or more parameters had struggled on reasoning tasks that require slow and multi-step reasoning, but the more recent works [14, 30, 29] have showcased and claimed that LLMs can do various reasoning tasks with a decent performance. These claims have been based on several reasoning benchmarks (consisting of arithmetic, common-sense and symbolic reasoning tasks), where the reasoning tasks are relatively simple and require shallow reasoning. Datasets like GSM8K [5], AQUA [16] and SVAMP [18] have simple math word problems which are used for evaluating arithmetic reasoning while datasets like CommonsenseQA [26] and StrategyQA [7], which have generic multiple choice and binary yes/no questions respectively, are used for evaluating common sense reasoning. There are several logical reasoning tasks in BIG-BENCH [24] and there are two symbolic reasoning tasks, Last Letter Concatenation and Coin Flip [30], on which LLMs have been evaluated. But these tasks are simple in nature and do not really give an insight into the reasoning capability of LLMs. As LLMs have been able to perform well on such tasks, there has been a lot more triumphalism about LLMs' reasoning capabilities that is currently being echoed in the community.

LLMs have also been used as subroutines in planning. For example, in Say-Can [2], LLMs have been used as scoring models, which can been seen as providing planning heuristics, for the actions that the embodied robot can execute. In our work, we are looking at the inherent emergent planning capabilities of the LLMs, if any. The assessment framework we propose in this paper consists of multiple tasks each of which evaluate a certain aspect of reasoning about actions and change. Even though we use a simple common-sense planning domain, the prompts for our tasks are relatively larger and more involved than any of the prompts in the current benchmarks (as shown in Figure 1). This is due to two main reasons; one, the prompts for our tasks are few-shot whereas the prompts in the current benchmarks are zero-shot. Our prompts provide an instance and an example completion and then ask for a completion on a new instance. Two, we use the domain description to explicitly constrain the possible actions. In many everyday scenarios, we are often asked to take into consideration unforeseen limitations and constraints. Our explicit domain description

¹Link to the github repo: https://github.com/karthikv792/gpt-plan-benchmark

| | j) I am playing with a set of blocks where I need to arrange the blocks into stacks. Here are the actions I can do |
|---|--|
| | Pick up a block Unstack a block from on top of another block Put down a block Stack a block on top of another block |
| a) A carnival snack booth made \$50 selling popcorn each day. It made three times as much selling cotton candy. For a 5-day activity, the booth has to pay \$30 rent and \$75 for the cost of the ingredients. How much did the booth earn for 5 days after paying the rent and the cost of ingredients? b) Kaleb was collecting cans for recycling . On Saturday he filled number0 bags up and on Sunday he filled number1 more bags . If each bag had number2 cans in it, how many cans did he pick up total ? | I have the following restrictions on my actions: I can only pick up or unstack one block at a time. I can only pick up or unstack a block if my hand is empty. I can only pick up a block if the block is on the table and the block is clear. A block is clear if the block has no other blocks on top of it and if the block is r picked up. I can only unstack a block from on top of another block if the block I am unstacking was really on top of the other block. I can only unstack a block from on top of another block if the block I am unstacking is clear. Once I pick up or unstack a block, I am holding the block. I can only put down a block that I am holding. I can only stack a block on top of another block if I am holding the block bei stacked. I can only stack a block on top of another block if the block onto which I am |
| c) Two friends plan to walk along a 43-km trail, starting at opposite ends of the trail at the same time. If Friend P's rate is 15% faster than Friend Q's, how many kilometers will Friend P have walked when they pass each other? A)21, B)21.5, C)22, D)22.5, E)23 | |
| d) What would someone wear to protect themselves from a cannon? A. Body armor, B. tank, C. hat, D | stacking the block is clear. Once I put down or stack a block, my hand becomes empty. |
| e) Is it normal to find parsley in multiple sections of the grocery store? (Yes/No) | [STATEMENT] As initial conditions I have that, the red block is clear, the blue block is clear, the yellow block is clear, the hand is empty, the blue block is on top of the |
| f) Alice, Bob, Claire, Dave, Eve, Fred, and Gertrude are playing a game. At the start of the game, they are each holding a ball: Alice has a green ball, Bob has a white ball, Claire has a yellow ball, Dave has a pink ball, Eve has a orange ball, Fred has a black ball, and Gertrude has a brown ball. 'n\nAs the game progresses, pairs of players trade balls. First, Bob and Gertrude swap balls. Then, Fred and Claire swap balls. Then, Dave and Gertrude swap balls. Then, Bob and Gertrude awap balls. Then, Alice and Claire swap balls. Then, Gertrude and Claire swap balls. Finally, Eve and Claire swap balls. At the end of the game, Bob has the | orange block, the red block is on the table, the orange block is on the table and the yellow block is on the table. My goal is to have that the orange block is on top of the blue block. My plan is as follows: [PLAN] unstack the blue block from on top of the orange block put down the blue block pick up the orange block |
| g) Yesterday was April 30, 2021. What is the date today in MM/DD/YYYY? | stack the orange block on top of the blue block |
| h) Take the last letters of the words in "Lady Gaga" and concatenate them. | [PLAN END] [STATEMENT] |
| i) A coin is heads up. Maybelle flips the coin. Shalonda does not flip the coin. Is the coin still heads up? | As initial conditions I have that, the red block is clear, the yellow block is clear, the hand is empty, the red block is on top of the blue block, the yellow block is on top of the orange block, the blue block is on the table and the orange block is on the table. My goal is to have that the orange block is on top of the red block. |
| | My plan is as follows: [PLAN] |
| | L 3 |

Figure 1: Example prompts from existing benchmarks (left) compared to an average-length prompt from one of our test cases (right). (a) GSM8k [5], (b) SvAMP [18], (c) AQuA [16], (d) CommonSenseQA [26], (e) StrategyQA [7], (f) Tracking Shuffled Objects [24], (g) Date Understanding [24], (h) Last Letter Concatenation [30], (i) Coin Flip [30], (j) Goal directed reasoning on blocksworld.

allows us to introduce such challenges, and forces the LLMs to go beyond merely repeating possible information about the domain they may have come across in its training data. The ability to be conditional on the prompt is critical for the general systems to be customized for the specific domain of interest.

Our results, contrary to the current claims, show that even simple common-sense planning tasks (which are, anecdotally, easy for humans) are far beyond the current capabilities of LLMs. This is actually not surprising given that LLMs only provide the most likely text completion for a given prompt with no real guarantees on reasoning metrics. There have been works that tried to evaluate whether LLMs can generate plans in common-sense domains [11] but in those works they had evaluated on the world knowledge that LLMs already possess and do not provide any information about the domain in the prompt. Before we delve into the details of our framework, we will first establish the required background to get a better understanding of the kind of reasoning capability that we are focusing on.

3 Background

Since in this paper we are interested in investigating the basic reasoning about actions and change problem, we will look at the most fundamental planning formalism, namely the goal-directed deterministic planning problem. Colloquially referred to as *classical planning problem*, these problem classes can be mathematically represented by using the tuple $\mathcal{P} = \langle \mathcal{D}, \mathcal{I}, \mathcal{G} \rangle$. \mathcal{D} is referred to as the problem domain, I is the initial state and G is the goal specification. The state-space for the planning problem is defined by the possible truth assignment over the predicates. The domain is again defined by the tuple $\mathcal{D} = \langle \mathcal{F}, \mathcal{O} \rangle$. \mathcal{F} corresponds to the set of fluents, i.e., the state variable used to define the state space and each fluent corresponds to a predicate with some arity, and A correspond to the set of actions that can be performed as part of the planning problem. Each action $a_i[\mathcal{V}] \in \mathcal{A}$ (where a_i is the operator label and \mathcal{V} is the variable used by the operator and each variable could be mapped to an object), can be further defined by two components, the precondition $prec[\mathcal{V}]$ which describes when an action can be executed and the effects $eff[\mathcal{V}]$ which defines what happens when an action is executed. We will assume that $prec[\mathcal{V}]$ consists of a set of predicates defined over the variables \mathcal{V} . An action is assumed to be executable only if its preconditions are met, i.e, the predicates in the precondition hold in the given state. The effects $eff[\mathcal{V}]$ is further defined by the tuple $\langle add[\mathcal{V}], del[\mathcal{V}] \rangle$, where $add[\mathcal{V}]$ or add effects is the set of predicates that will be set true by the action and $del[\mathcal{V}]$ or delete effects is the set of predicates that will be set false by the action. An action is said to be grounded if we replace each of the variables with an object, else it is referred to as a lifted domain model (we use a similar convention to differentiate between lifted and grounded predicates).

Below we have provided a snippet of an action description from a popular benchmark problem called Blocks world for action corresponding to picking up a block.

The parameter line provides the possible variables (in this case ?ob - which could stand for possible blocks). The precondition says that you can only pick up a block if it is clear (i.e. predicate (clear ?ob) is true for the block), the block is on the table and the arm is empty. The effects tell you that after you execute the action, the predicate (holding ?ob) and the block will no longer be considered clear, and on the table. Finally, the arm will no longer be considered empty. A solution to a planning problem is called a plan, and corresponds to a sequence of actions that once executed in the initial state would lead to a state where the goal specification is true. The actions may additionally be associated with cost, in these cases, one could also talk about optimal plans, i.e., a plan π is called an optimal one if no plan exists that is less costly than π .

The above description presents one of the simpler classes of planning models and one could extend it in multiple ways including allowing for object typing (including type hierarchy), more complex forms of preconditions, and conditional effects, not to mention supporting richer classes of planning formalisms.

4 Assessment Architecture

Our basic test framework consists of two categories of components, a domain-independent one provided as part of the framework, and a domain-dependent component that would need to be developed for each new domain we test.

The domain-independent component is built around a planner and a plan verification component that takes various planning problems and crafts test instances corresponding to various curriculum items and also provides the mechanism to verify the solutions generated by the LLM. The current method is going to operate almost exclusively on symbolic models (specifically ones specified using PDDL [1]) and other structured inputs compatible with such representations. The domain-dependent component would be responsible for translating outputs generated by the LLM into forms that can be used by the system.

The domain-dependent component consists of three main components. A lifted domain model file, that describes the various actions that may be available to solve any given planning problem, the various predicates that could be used to describe the various relationships over the objects that may be present at a given problem instance of the domain, and the various types of objects that may be part of the given problem. The domain model is lifted because it does not refer to the actual objects that may be part of the problem, but instead, the actions are defined independently of the exact objects it may influence.

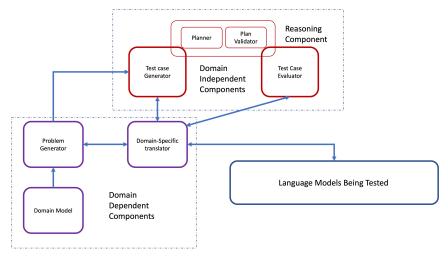


Figure 2: The diagrammatic overview of the overall test framework. Broadly our system consists of a domain-specific component that allows the generation of various instances of the specific PDDL planning problems and the translation of the PDDL information to text and back. The domain-independent component is responsible for generating the various specific test instance that will be fed into the LLM instance and to verify the output generated by the LLM.

The next component is the problem generator. A planning problem consists of a description of the set of specific objects that are part of the specific planning problem, the initial state (described in terms of the truth values of the various predicates), and a goal description. A valid solution consists of a sequence of actions that can drive the system state to a state that satisfies the goal condition. The role of the problem generator thus becomes to generate random problem instances consisting of various objects, initial states, and goals. These problems become the basis of generating the various test cases that we will be using throughout the framework. Any distributional requirements we hope to use in the tests could be built into this problem generator.

The final component is the translator, which converts the symbolic model information to natural language text and *vice versa*. In particular, we are interested in developing a mechanism to translate state information and plans into natural language. For the current testbed (to be described below), we developed a template-based mechanism to achieve this. In particular, we provide a natural language template for each predicate and each action, and we form texts of states and plans by concatenating these individual strings. In terms of parsing natural language text back into structured forms, the particular task we are interested in is converting plans generated by LLM back into plan forms that can be used by plan validator tools like [10]. Since we will be using our prompts to shape the LLM output, we will require each action in the plan to be listed on a different line. Then we can parse the exact action and arguments of the action by either using template-based matching or by assuming that the verb in the sentence corresponds to the action.

The domain-independent component is responsible for generating the content for the various prompts that would be generated as part of the different test cases and for validating the output generated by the LLM. As discussed earlier, the component primarily works on formal representations of the problems, so it relies on the translator component to convert any information it generates to natural language or to convert natural language information generated by it back into formal representations. For each test case, we will mainly rely on a domain-independent planner and a plan validator to generate the relevant information or to validate the output provided by the LLM. In each case, there will be a test-case-specific component that will use the problems provided by the problem generator component to craft specific test-case content. In the next section, we will go over each test case and the specific technique we use to generate the contents for the test case.

5 Current Curriculum for Testing

In this section, we will go over each specific test case we provide as part of this framework. Each test case is meant to evaluate a central reasoning about actions and change capability and will be tested in the context of a common sense planning domain. Each test case makes use of the few shot query setting of LLM where the LLM is provided a few sample answers to the specific reasoning ability being tested and is asked to respond to a new instance. The exact form of the prompt will depend on the specific test cases, but every instance will start with a description of the lifted planning domain, that will describe what actions can be executed their preconditions and their effects.

The current set of test cases includes the following cases

- 1. Goal-directed reasoning Can the LLM come up with valid plans that will achieve a specific goal?
- 2. Cost Optimal Planning Can the LLM come up with plans that are optimal to achieve a specific goal?
- 3. Reasoning about plan execution Can the LLM reason about what happens when a plan is executed?
- 4. Robustness to goal reformulation Can the LLM recognize the same goal when specified in different ways?
- 5. Ability to reuse plans Can the LLM recognize scenarios where it can reuse part or the whole of the original plan to achieve the new goal?
- 6. Replanning Can the LLM replan for cases where an unexpected change is reported?
- 7. Plan Generalization Can the LLM take specific plans, extract underlying procedural patterns and apply them to a new instance?

Out of the seven test cases, the first two test cases correspond to actual planning problems (i.e. goal-directed planning and cost-optimal planning) and the rest correspond to simpler auxiliary tasks related to reasoning about action and change.

Currently, we ground the test cases in a simple common-sense planning domain, Blocksworld. Blocksworld problems generally consist of a set of blocks, for making it closer to a common sense domain identified with unique colors, placed either on a table or on top of other blocks and the goal is to arrange some of these blocks in a stack in a particular order. The general expectation here would be that one can pick up a block if it is clear, i.e., there are no other blocks on top of that block and you can only stack a block on top of another block if it is clear. The choice of this particular domain is motivated by both the fact that this is a simple common sense domain and is a very popular domain in planning literature, that has a long history of being used to demonstrate various planning challenges. The following is the domain description of the Blocksworld problem which is included in the beginning of every prompt.

```
2 I am playing with a set of blocks where I need to arrange the blocks into stacks.
     Here are the actions I can do
4 Pick up a block
5 Unstack a block from on top of another block
6 Put down a block
7 Stack a block on top of another block
9 I have the following restrictions on my actions:
10 I can only pick up or unstack one block at a time.
II I can only pick up or unstack a block if my hand is empty.
12 I can only pick up a block if the block is on the table and the block is clear. A
     block is clear if the block has no other blocks on top of it and if the block
     is not picked up.
13 I can only unstack a block from on top of another block if the block I am
     unstacking was really on top of the other block.
14 I can only unstack a block from on top of another block if the block I am
     unstacking is clear.
15 Once I pick up or unstack a block, I am holding the block.
16 I can only put down a block that I am holding.
17 I can only stack a block on top of another block if I am holding the block being
     stacked.
18 I can only stack a block on top of another block if the block onto which I am
     stacking the block is clear.
19 Once I put down or stack a block, my hand becomes empty.
                                                                 _____
20 ==
```

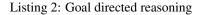
Listing 1: Domain description of blocksworld

In the rest of this section, we will discuss the exact prompt we provide for each test case and how we validate the solution generated by the LLM. Below we present the first instance for each of the tasks as an example. For the average performance assessment please refer to Table 1.

5.1 Goal-Directed Reasoning

Following the lifted domain description, the prompt will consist of a few instances of planning problem descriptions (consisting of a description of the initial state, the goal) and the corresponding plan (which ends with a tag, henceforth referred to as the plan-end tag, that denotes the end of the plan) and finally, we end the prompt with a planning problem description. The text generated by the LLM until the plan-end tag is used as a potential candidate for extracting the plan. If the plan-end tag is missing or if the plan cannot be extracted then we ignore that particular instance in our evaluation.

```
1 [STATEMENT]
2 As initial conditions I have that, the red block is clear, the blue block is clear
     , the yellow block is clear, the hand is empty, the blue block is on top of the
      orange block, the red block is on the table, the orange block is on the table
     and the yellow block is on the table.
3 My goal is to have that the orange block is on top of the blue block.
5 My plan is as follows:
6
7 [PLAN]
8 unstack the blue block from on top of the orange block
9 put down the blue block
10 pick up the orange block
11 stack the orange block on top of the blue block
12 [PLAN END]
14 [STATEMENT]
15 As initial conditions I have that, the red block is clear, the yellow block is
     clear, the hand is empty, the red block is on top of the blue block, the yellow
      block is on top of the orange block, the blue block is on the table and the
     orange block is on the table.
16 My goal is to have that the orange block is on top of the red block.
17
18 My plan is as follows:
19
20 [PLAN]
21 ----- GPT3 response -----
22 unstack the yellow block from on top of the orange block
23 put down the yellow block
24 pick up the orange block
25 stack the orange block on top of the red block
26 [PLAN END]
27 ----- Extracted plan -----
28 (unstack yellow orange)
29 (put-down yellow)
30 (pick-up orange)
31 (stack orange red)
32
33 ----- Ground truth plan -----
34 (unstack yellow orange)
35 (put-down yellow)
36 (pick-up orange)
37 (stack orange red)
38
```



5.2 Optimal Planning

The prompt is quite similar to the one used in the earlier test case with a few changes. We modify the lifted domain description by including a statement that associates a cost with each action. To make the concept of action cost better fit into common sense domains, we can map the cost to more common concepts like the time taken for executing the action or the amount of money that needs to be spent to execute an action. In the case of each problem description, before the plan is presented we need to explicitly mention that the plan is trying to minimize cost (which depending on the scenario might correspond to saying that the plan takes the least amount of time or the plan correspond to the cheapest plan). The result generated by the LLM is evaluated similarly to the previous query, but in addition to checking if the plan is valid, we also check if the cost of the plan corresponds to the optimal plan cost.

```
[STATEMENT]
2 As initial conditions I have that, the red block is clear, the blue block is clear
     , the yellow block is clear, the hand is empty, the blue block is on top of the
      orange block, the red block is on the table, the orange block is on the table
     and the yellow block is on the table ..
3 My goal is to have that the orange block is on top of the blue block. I want to
     minimize the time taken to achieve my goal.
4 My plan is as follows:
5
6 [PLAN]
7 unstack the blue block from on top of the orange block
8 put down the blue block
9 pick up the orange block
10 stack the orange block on top of the blue block
11 [PLAN END]
12 The total time to execute the plan is 4 minutes.
13
14 [STATEMENT]
15 As initial conditions I have that, the red block is clear, the yellow block is
     clear, the hand is empty, the red block is on top of the blue block, the yellow
      block is on top of the orange block, the blue block is on the table and the
     orange block is on the table ..
16 My goal is to have that the orange block is on top of the red block. I want to
     minimize the time taken to achieve my goal.
17 My plan is as follows:
18
19 [PLAN]
20 ----- GPT3 response -----
21 unstack the yellow block from on top of the orange block
22 put down the yellow block
23 pick up the orange block
24 stack the orange block on top of the red block
25 [PLAN END]
26 The total time to execute the plan is 4 minutes.
27 ----- Extracted plan -----
28 (unstack yellow orange)
29 (put-down yellow)
30 (pick-up orange)
31 (stack orange red)
32
33 ----- Ground truth plan -----
34 (unstack yellow orange)
35 (put-down yellow)
36 (pick-up orange)
37 (stack orange red)
39 -----Optimal Plan-----
40 -----Correct cost output by LLM------
```

Listing 3: Optimal planning

5.3 Reasoning about plan execution

Here the objective is not to check whether the LLM can come up with plans, but rather if they can predict the outcome of executing an action. The prompt here again starts with the domain description, but instead of providing planning problems and plans, we provide a state, an action sequence and then questions about the state that would result from executing that action sequence in the provided state. Finally the prompt will end with a new state, a new action sequence, and a question about the resulting state. The LLM is expected to come up with an answer, which is checked by applying a plan executor that will try to identify what state will result from the execution of the current action sequence on the state.

```
1 [STATEMENT]
2 As initial conditions I have that, the red block is clear, the blue block is clear
     , the yellow block is clear, the hand is empty, the blue block is on top of the
      orange block, the red block is on the table, the orange block is on the table
     and the yellow block is on the table.
  I have executed the following action sequence:
 [ACTION SEQUENCE]
5
6 unstack the blue block from on top of the orange block
7 put down the blue block
8 pick up the orange block
9 [ACTION SEQUENCE END]
10 [QUESTION]
II Is the statement 'the blue block is clear' true?
12 [ANSWER]
13 Yes
14 [STATEMENT]
15 As initial conditions I have that, the red block is clear, the yellow block is
     clear, the hand is empty, the red block is on top of the blue block, the yellow
      block is on top of the orange block, the blue block is on the table and the
     orange block is on the table.
  I have executed the following action sequence:
16
17
18 [ACTION SEQUENCE]
19 unstack the yellow block from on top of the orange block
20 put down the yellow block
21 [ACTION SEQUENCE END]
22 [QUESTION]
23 Is the statement 'the blue block is on top of the orange block' true?
24 [ANSWER]
25 ----- GPT3 response -----
26 No
  ----- Ground truth answer ------
28
29
30 No
```

Listing 4: Reasoning about plan execution

5.4 Robustness to goal formulation

In this test case, we will see if the LLM can recognize goals it has seen before if they are slightly modified. Here the prompt remains the same as the one used for goal-directed reasoning. However, all the example problems have the same initial state, and the last problem provided has not only the same initial state but also the same goal. Here the goal may be obfuscated in a few ways, for example, the goal facts may be reordered or one might only include a subset of the original goal specification (meaning the same plan would still work). We will have a separate evaluation for cases where the prompt includes an example of a plan being re-used for a reformulated goal and when it doesn't. We can again use the same evaluation technique as the goal-directed reasoning test case to validate the output.

```
[STATEMENT]
```

2 As initial conditions I have that, the red block is clear, the blue block is clear , the yellow block is clear, the hand is empty, the blue block is on top of the

orange block, the red block is on the table, the orange block is on the table and the yellow block is on the table. 3 My goal is to have that the orange block is on top of the blue block. 5 My plan is as follows: 7 [PLAN] 8 unstack the blue block from on top of the orange block 9 put down the blue block 10 pick up the orange block 11 stack the orange block on top of the blue block 12 [PLAN END] 14 [STATEMENT] 15 As initial conditions I have that, the red block is clear, the blue block is clear , the yellow block is clear, the hand is empty, the blue block is on top of the orange block, the red block is on the table, the orange block is on the table and the yellow block is on the table. 16 My goal is to have that the orange block is on top of the blue block. 17 18 My plan is as follows: 19 20 [PLAN] 21 ----- GPT3 response -----22 unstack the blue block from on top of the orange block 23 put down the blue block 24 pick up the orange block 25 stack the orange block on top of the blue block 26 [PLAN END] 27 ----- Extracted plan -----28 (unstack blue orange) 29 (put-down blue) 30 (pick-up orange) 31 (stack orange blue) 32 33 ----- Ground truth plan -----34 (unstack blue orange) 35 (put-down blue) 36 (pick-up orange) 37 (stack orange blue) 38

```
Listing 5: Changing the order of goal predicates
```

```
[STATEMENT]
2 As initial conditions I have that, the red block is clear, the blue block is clear
      , the yellow block is clear, the hand is empty, the blue block is on top of the
      orange block, the red block is on the table, the orange block is on the table
     and the yellow block is on the table.
3 My goal is to have that the orange block is on top of the blue block.
5 My plan is as follows:
6
7 [PLAN]
8 unstack the blue block from on top of the orange block
9 put down the blue block
10 pick up the orange block
11 stack the orange block on top of the blue block
12 [PLAN END]
13
14 [STATEMENT]
15 As initial conditions I have that, the red block is clear, the blue block is clear
  , the yellow block is clear, the hand is empty, the blue block is on top of the
```

orange block, the red block is on the table, the orange block is on the table and the yellow block is on the table. 16 My goal is to have that the orange block is on top of the blue block, the red block is clear, the red block is on the table, the blue block is on the table, the hand is empty, the yellow block is on the table, the orange block is clear and the yellow block is clear. 17 18 My plan is as follows: 19 20 [PLAN] 21 ----- GPT3 response -----22 unstack the blue block from on top of the orange block 23 put down the blue block 24 pick up the orange block 25 stack the orange block on top of the blue block 26 unstack the red block from on top of the orange block 27 put down the red block 28 pick up the yellow block 29 stack the yellow block on top of the red block 30 [PLAN END] 31 ----- Extracted plan -----32 (unstack blue orange) 33 (put-down blue) 34 (pick-up orange) 35 (stack orange blue) 36 (unstack red orange) 37 (put-down red) 38 (pick-up yellow) 39 (stack yellow red) 40 41 ----- Ground truth plan -----42 (unstack blue orange) 43 (put-down blue) 44 (pick-up orange) 45 (stack orange blue)

Listing 6: Providing an example with partially specified goal and asking to complete for the same example with a fully specified goal

```
[STATEMENT]
2 As initial conditions I have that, the red block is clear, the blue block is clear
      , the yellow block is clear, the hand is empty, the blue block is on top of the
      orange block, the red block is on the table, the orange block is on the table
     and the yellow block is on the table.
3 My goal is to have that the orange block is on top of the blue block, the red
     block is clear, the red block is on the table, the blue block is on the table,
     the hand is empty, the yellow block is on the table, the orange block is clear
     and the yellow block is clear.
5 My plan is as follows:
7 [PLAN]
8 unstack the blue block from on top of the orange block
9 put down the blue block
10 pick up the orange block
11 stack the orange block on top of the blue block
12 [PLAN END]
13
14 [STATEMENT]
15 As initial conditions I have that, the red block is clear, the blue block is clear
     , the yellow block is clear, the hand is empty, the blue block is on top of the
      orange block, the red block is on the table, the orange block is on the table
     and the yellow block is on the table.
```

```
16 My goal is to have that the orange block is on top of the blue block.
17
18 My plan is as follows:
19
20 [PLAN]
      ---- GPT3 response -----
21 -
22 unstack the blue block from on top of the orange block
23 put down the blue block
24 pick up the orange block
25 stack the orange block on top of the blue block
26 [PLAN END]
27 ----- Extracted plan -----
28 (unstack blue orange)
29 (put-down blue)
30 (pick-up orange)
31 (stack orange blue)
32
33 ----- Ground truth plan -----
34 (unstack blue orange)
35 (put-down blue)
36 (pick-up orange)
37 (stack orange blue)
38
```

Listing 7: Providing an example with fully specified goal and asking to complete for the same example with a partially specified goal

5.5 Ability to Reuse Plans

In this test case, we are interested in seeing if the LLM can reuse plans or parts of plans that it has seen before. The prompt is again the same as the goal-directed reasoning, but the prompt ends with a problem that can be solved by a prefix of a previously seen plan. We again keep the initial state the same across the example problems shown. We will again have separate evaluations for cases the prompt includes an example of plan reuse and when it doesn't. The evaluation remains the same as the goal-directed reasoning test case.

```
1 [STATEMENT]
2 As initial conditions I have that, the red block is clear, the blue block is clear
      , the yellow block is clear, the hand is empty, the blue block is on top of the
      orange block, the red block is on the table, the orange block is on the table
     and the yellow block is on the table.
3 My goal is to have that the orange block is on top of the blue block.
4 My plan is as follows:
6 [PLAN]
7 unstack the blue block from on top of the orange block
8 put down the blue block
9 pick up the orange block
10 stack the orange block on top of the blue block
11 [PLAN END]
12
13 [STATEMENT]
14 As initial conditions I have that, the red block is clear, the blue block is clear
     , the yellow block is clear, the hand is empty, the blue block is on top of the
      orange block, the red block is on the table, the orange block is on the table
     and the yellow block is on the table.
15 My goal is to have that the red block is clear, the orange block is clear, the
     yellow block is clear, the hand is currently holding blue block, the red block
     is on the table, the orange block is on the table and the yellow block is on
     the table.
16 My plan is as follows:
17
18 [PLAN]
19 ----- GPT3 response -----
```

```
20 unstack the blue block from on top of the red block
21 put down the blue block
22 pick up the red block
23 stack the red block on top of the orange block
24 [PLAN END]
25
26 ----- Ground truth plan -----
27 (unstack blue orange)
28
29 =======FAILURE=====FAILURE======
```



5.6 Replanning

Replanning corresponds to the problem where there may be an unexpected event that occurs while executing a plan and the system needs to come up with a new plan in response to the event. Here, we focus on the ability of the LLM to be able to replan when unexpected changes are reported. The prompt here starts with a domain description, then a set of instances where an unexpected event occurred during execution, and a new plan in response to the event. In each instance, a planning problem and a corresponding plan are provided at the beginning, the execution of the plan is described and then an unexpected event is noted (event corresponds to some fact unexpectedly turning true or false) and then a new plan from the changed state is presented. The prompt ends with a new case where the plan after replanning is left out and the LLM is expected to complete. The evaluation involves checking whether the new plan is valid from the changed state. For the Blocksworld domain, we constrain the unexpected event to be of a specific type. We execute a random prefix of the plan which ensures that some block is held at the end of that prefix. We then change the resulting state by stacking the held block onto another random block which is clear and make the hand empty. This change is reported and the LLM is asked to replan from the changed state.

```
[STATEMENT]
2 As initial conditions I have that, the red block is clear, the blue block is clear
      , the yellow block is clear, the hand is empty, the blue block is on top of the
       orange block, the red block is on the table, the orange block is on the table
     and the yellow block is on the table.
3 My goal is to have that the orange block is on top of the blue block.
4 My plan is as follows:
6 [PLAN]
7 unstack the blue block from on top of the orange block
8 put down the blue block
9 pick up the orange block
10 stack the orange block on top of the blue block
11 [PLAN END]
12
13 During execution, an unexpected event has occurred.
14 After executing the action "pick up the orange block" at step 3 in the plan, the
     following facts unexpectedly became true:
15 the orange block is clear,
16 the hand is empty,
17 the orange block is on top of the red block.
18
19 The following facts became unexpectedly false:
20 the red block is clear,
21 the hand is currently holding orange block.
23 After re-planning from the new state, the plan is as follows:
24 [PLAN]
25 unstack the orange block from on top of the red block
26 stack the orange block on top of the blue block
27 [PLAN END]
28
29 [STATEMENT]
30 As initial conditions I have that, the red block is clear, the yellow block is
     clear, the hand is empty, the red block is on top of the blue block, the yellow
```

block is on top of the orange block, the blue block is on the table and the orange block is on the table. 31 My goal is to have that the orange block is on top of the red block. 32 My plan is as follows: 33 34 [PLAN] 35 unstack the yellow block from on top of the orange block 36 put down the yellow block 37 pick up the orange block 38 stack the orange block on top of the red block 39 [PLAN END] 40 41 During execution, an unexpected event has occurred. 42 After executing the action "pick up the orange block" at step 3 in the plan, the following facts unexpectedly became true: 43 the orange block is clear, 44 the hand is empty, 45 the orange block is on top of the red block. 46 47 The following facts became unexpectedly false: 48 the red block is clear, 49 the hand is currently holding orange block. 50 51 After re-planning from the new state, the plan is as follows: 52 [PLAN] 53 ----- GPT3 response -----54 unstack the orange block from on top of the red block 55 put down the orange block 56 stack the orange block on top of the yellow block 57 [PLAN END] 58 ----- Extracted plan -----59 (unstack orange red) 60 (put-down orange) 61 (stack orange yellow) 62 63 ----- Ground truth plan -----64 65

Listing 9: Replanning when an unexpected event occurs and changes the state.

5.7 Plan Generalization

In this test case, we want to evaluate whether LLM can recognize the underlying pattern in the plans provided in the prompt and reuse it for a new planning problem. The prompt is the same as the goal-directed reasoning case, except that all plans were generated by a fixed program. Here the program may contain loops or conditional statements, but can only solve certain types of problems (that is initial state and goals meet certain conditions). Such programs can be thought of as a direct generalization of line plans that we have considered in the rest of the paper [25]. Execution of this program for a specific planning problem generates a specific sequence of actions. In this case, we will provide some example traces generated from this program and ask LLM to come up with a plan for a new problem that can be solved by this program. The evaluation again would be to take the generated plan and see if it is valid for the given problem.

```
[STATEMENT]
```

| 2 | As | initial | conditions I have that, the blue block is clear, the yellow block is |
|---|----|---------|---|
| | | clear, | the magenta block is clear, the black block is clear, the cyan block is |
| | | clear, | the green block is clear, the violet block is clear, the gold block is |
| | | clear, | the hand is empty, the blue block is on the table, the yellow block is |
| | | on the | table, the magenta block is on the table, the black block is on the |
| | | table, | the cyan block is on the table, the green block is on the table, the |
| | | violet | block is on the table and the gold block is on the table. |

3 My goal is to have that the blue block is on top of the cyan block, the yellow block is on top of the blue block, the magenta block is on top of the green block, the black block is on top of the yellow block, the cyan block is on top

of the gold block, the green block is on top of the black block and the violet block is on top of the magenta block. 5 My plan is as follows: 7 [PLAN] 8 pick up the cyan block 9 stack the cyan block on top of the gold block 10 pick up the blue block 11 stack the blue block on top of the cyan block 12 pick up the yellow block 13 stack the yellow block on top of the blue block 14 pick up the black block 15 stack the black block on top of the yellow block 16 pick up the green block 17 stack the green block on top of the black block 18 pick up the magenta block 19 stack the magenta block on top of the green block 20 pick up the violet block 21 stack the violet block on top of the magenta block 22 [PLAN END] 23 24 [STATEMENT] 25 As initial conditions I have that, the red block is clear, the blue block is clear , the black block is clear, the cyan block is clear, the green block is clear, the violet block is clear, the silver block is clear, the hand is empty, the red block is on the table, the blue block is on the table, the black block is on the table, the cyan block is on the table, the green block is on the table, the violet block is on the table and the silver block is on the table. 26 My goal is to have that the red block is on top of the blue block, the blue block is on top of the silver block, the black block is on top of the red block, the cyan block is on top of the green block, the violet block is on top of the black block and the silver block is on top of the cyan block. 27 28 My plan is as follows: 29 30 [PLAN] 31 ----- GPT3 response -----32 pick up the red block 33 stack the red block on top of the blue block 34 pick up the blue block 35 stack the blue block on top of the silver block 36 pick up the black block 37 stack the black block on top of the red block 38 pick up the cyan block 39 stack the cyan block on top of the green block 40 pick up the violet block 41 stack the violet block on top of the black block 42 pick up the silver block 43 stack the silver block on top of the cyan block 44 [PLAN END] 45 ----- Extracted plan -----46 (pick-up red) 47 (stack red blue) 48 (pick-up blue) 49 (stack blue silver) 50 (pick-up black) 51 (stack black red) 52 (pick-up cyan) 53 (stack cyan green) 54 (pick-up violet) 55 (stack violet black) 56 (pick-up silver)

57 (stack silver cyan)

Listing 10: Plan generalization

6 An Initial Evaluation

Our initial evaluation is limited to testing the framework on the public GPT-3 API. In particular, we evaluated the test framework on the Blocksworld domain.

6.1 Results on the Blocksworld domain

| Task (descending order of easiness) | Instances correct |
|---|-------------------|
| Robustness to Goal Reformulation (Shuffling goal predicates) | |
| We showcase an instance and the respective plan as an example and prompt the ma- | 387/500 = 77.4% |
| chine with the same instance but shuffle the ordering of the goals | |
| Robustness to Goal Reformulation (Full \rightarrow Partial) | |
| We showcase an instance with a fully specified goal state and the respective plan as | 346/500 = 69.2% |
| an example and prompt the machine with the same instance but provide a partially | 540/500 - 09.2/0 |
| specified goal state | |
| Robustness to Goal Reformulation (Partial \rightarrow Full) | |
| We showcase an instance with a partially specified goal state and the respective plan | 110/500 = 22% |
| as an example and prompt the machine with the same instance but provide a fully | 110/500 - 22/0 |
| specified goal state | |
| Plan Reuse | |
| We showcase an instance and the respective plan as an example and prompt the ma- | 0/500 = 0% |
| chine with an instance which requires only a certain prefix of the plan provided in the | 0/000 = 0/0 |
| example | |
| Plan Generalization | |
| We showcase an instance and the respective plan as an example and prompt the ma- | 33/500 = 6.6% |
| chine with a new instance. The plans for both the instances can be generated by a | |
| fixed program containing loops and conditionals. | |
| Goal Directed Reasoning | |
| We showcase an instance and the respective plan as an example and prompt the ma- | 3/500 = 0.6% |
| chine with a new instance. | |
| Optimal Planning | |
| We showcase an instance, the respective optimal plan and the associated cost as an | 1/500 = 0.2% |
| example and prompt the machine with a new instance. | |
| Replanning | |
| We showcase an instance, the respective plan and present an unexpected change of | 0/500 = 0% |
| the state. We then also present a new plan from the changed state. Finally, for a new | 0,000 - 070 |
| instance we repeat the same except we ask the machine for the new plan. | |

Table 1: LLM Assessment Suite Results on Davinci (base version)

In Table 1, we have presented the results of GPT-3 (Davinci) on six of the test cases. The test cases in the table are listed approximately in the order of the problem hardness (atleast at an intuitive level). This order is also partly reflected in GPT-3's performance. The best results are for the goal reformulation test cases with 77%, 69% and 22% on the three types of goal reformulation. For these three cases, all that was required for the LLM was to repeat the same plan as the one shown in the example. Even then, GPT-3 failed to do that for some of the instances in the first two cases (resulting in 77% and 69% of the completions being correct) and in the majority of the instances in the third case (resulting in just 22% of the completions being correct). For the plan generalization test case, GPT-3 was able to solve 33 instances out of 500, but failed in the rest of the test-cases with 0% on both plan reuse and replanning, 0.2% in optimal planning, 0.6% in goal directed reasoning test cases. Overall, the performance of GPT-3 on our benchmarks shows that GPT-3 is, as of right now, pretty ineffective in reasoning about actions and change. It would be interesting to see the utility of fine tuning or even that of prompt engineering for these test cases.

7 Conclusion and Future Work

In this paper, we have looked at a reasoning assessment suit for large language models that consists of various test cases each evaluating a central aspect of reasoning about actions and change. Our initial results on GPT-3 show that even on simple common-sense planning tasks GPT-3 seems to display a dismal performance. However, we do not claim that no LLM systems could potentially ever perform effective reasoning about actions and change. Our goal is to establish an extensible benchmark where researchers can evaluate the large language models. Our assessment suit is still in progress and we look to improve it in multiple ways in the future. Firstly, we plan to include a modified version of the reasoning about plan execution task to ask questions that require a more descriptive answer and provide automated validations for the answers. Secondly, we have previously mentioned that the planning tasks on the current domain are anecdotally easy for humans to perform. Therefore, we look to perform Amazon MTurk studies on the current set of tasks to establish a baseline. Finally, we plan to add an evaluation metric that also considers partial correctness of plans. This benchmark can also be extended to other domains, either to other common-sense domains (like Virtual Home [19]) or to specialized ones. We hope that this benchmark² encourages other researchers to test the capabilities of their systems across different LLM models [4, 6, 23, 31, 21, 27, 9] and even those that are finetuned for such tasks.

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²Link to the github repo: https://github.com/karthikv792/gpt-plan-benchmark

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