

# Neural Network Heuristic Functions for Classical Planning: Bootstrapping and Comparison to Other Methods

Patrick Ferber<sup>1,3</sup>   Florian Geißer<sup>2</sup>   Felipe Trevizan<sup>2</sup>  
Malte Helmert<sup>1</sup>   Jörg Hoffmann<sup>3</sup>



<sup>1</sup>University of Basel, Basel, Switzerland

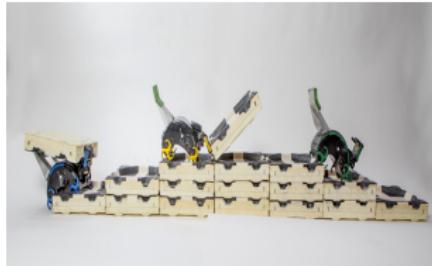
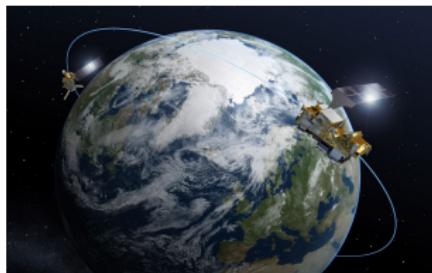
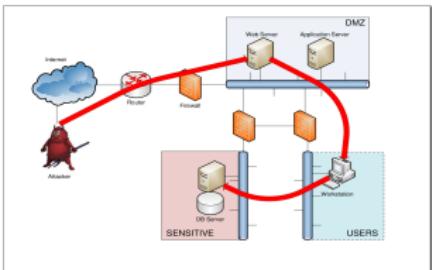
<sup>2</sup>Australian National University, Canberra, Australia

<sup>3</sup>Saarland University, Saarland Informatics Campus, Saarbrücken, Germany

32<sup>nd</sup> International Conference on Automated Planning and Scheduling

2022

# Motivation



Introduction  
○●○○

Background  
○○○○

Framework  
○○○

Experiemts  
○○○○○○

# Heuristic

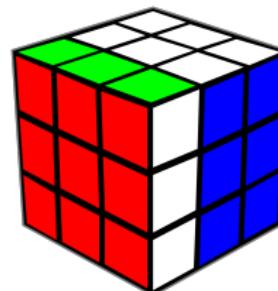


# Heuristic



Silver et al. (2016)  
Silver et al. (2017)  
Silver et al. (2018)

Agostinelli et al. (2019)



# Neural Networks as Planning Heuristics

*per-instance* heuristics



*per-domain* heuristics



- Ferber, Helmert, and Hoffmann (2020)
- Agostinelli et al. (2019)

- Shen, Trevizan, and Thiébaux (2020)
- Karia and Srivastava (2021)

# Neural Networks as Planning Heuristics

*per-instance* heuristics



*per-domain* heuristics



- Ferber, Helmert, and Hoffmann (2020)
- Agostinelli et al. (2019)

- Shen, Trevizan, and Thiébaux (2020)
- Karia and Srivastava (2021)

# Neural Networks as Planning Heuristics

*per-instance* heuristics



*per-domain* heuristics



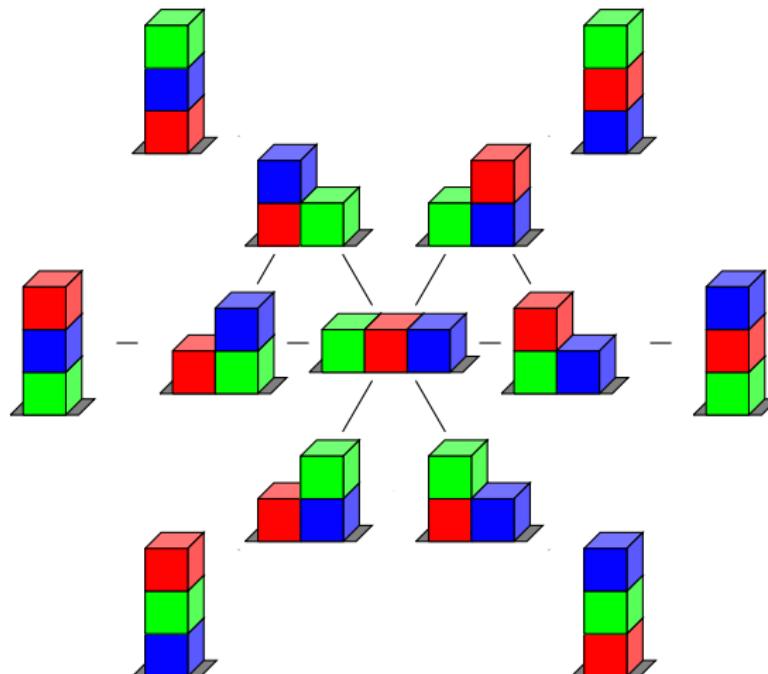
- Ferber, Helmert, and Hoffmann (2020)
- Agostinelli et al. (2019)

- Shen, Trevizan, and Thiébaut (2020)
- Karia and Srivastava (2021)

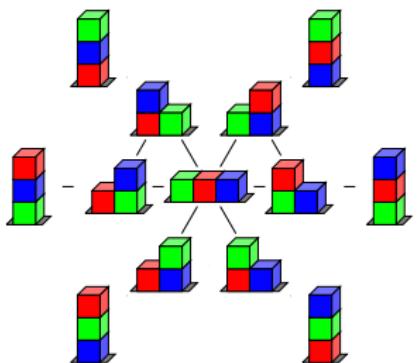
# Contributions

- three *per-instance* heuristics
  - only state as input
  - curriculum learning
  - prove convergence to  $h^*$
- comparison between state-of-the-art
  - neural network heuristics
  - model-based heuristics

# Finite-Domain Representation (Helmert, 2009)



# Finite-Domain Representation (Helmert, 2009)



$$\Pi = \langle V, O, I, g \rangle$$

$$V = \{ \textcolor{red}{\blacksquare}, \textcolor{green}{\blacksquare}, \textcolor{blue}{\blacksquare} \}$$

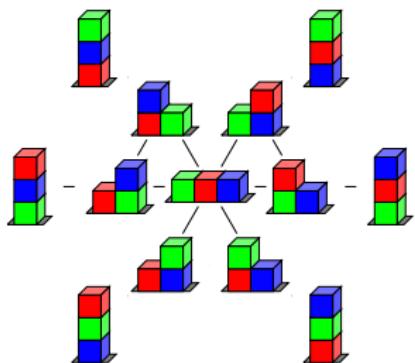
$$dom(\textcolor{red}{\blacksquare}) = \{ \text{on } \textcolor{green}{\blacksquare}, \text{on } \textcolor{blue}{\blacksquare}, \text{on } \textcolor{black}{\blacksquare} \}$$

$$O = \{ \text{move } \blacksquare \text{ from } X \text{ to } Y \}$$

$$I = \textcolor{green}{\blacksquare} \text{ on } \textcolor{black}{\blacksquare}$$

$$g = \{ \textcolor{green}{\blacksquare} \mapsto \text{on } \textcolor{black}{\blacksquare} \}$$

# Finite-Domain Representation (Helmert, 2009)



$$\Pi = \langle V, O, I, g \rangle$$

$$V = \{ \text{red}, \text{green}, \text{blue} \}$$

$$dom(\text{red}) = \{ \text{on green}, \text{on blue}, \text{on } \_ \}$$

$$O = \{ \text{move } \square \text{ from X to Y} \}$$

$$I = \begin{array}{c} \text{red} \\ \text{green} \\ \text{blue} \end{array}$$

$$g = \{ \text{green} \mapsto \text{on } \_ \}$$

$$\pi = \langle \text{move red from green to } \_, \\ \text{move green from blue to } \_ \rangle$$

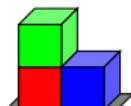
# Progression & Regression

move from to

*pre* : {  $\mapsto$  on }

*eff* : {  $\mapsto$  on }

## Progression



## Regression



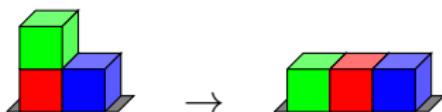
# Progression & Regression

move from to

*pre* : {  $\mapsto$  on }

*eff* : {  $\mapsto$  on }

## Progression



## Regression



# Progression & Regression

move from to

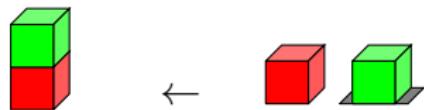
*pre* : {  $\mapsto$  on }

*eff* : {  $\mapsto$  on }

## Progression



## Regression

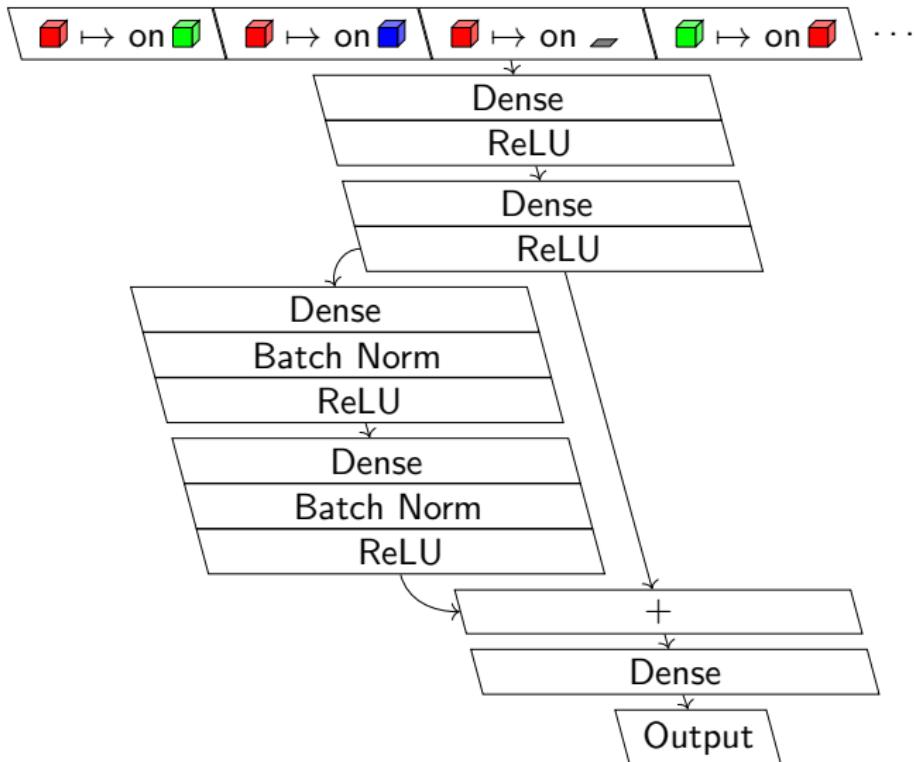


# Heuristic

$$h : S \rightarrow \mathbb{R}_0^+ \cup \{\infty\}$$

$h^*$  := perfect heuristic

# Residual Network (He et al., 2016)



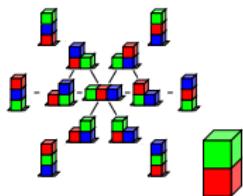
Introduction  
oooo

Background  
oooo

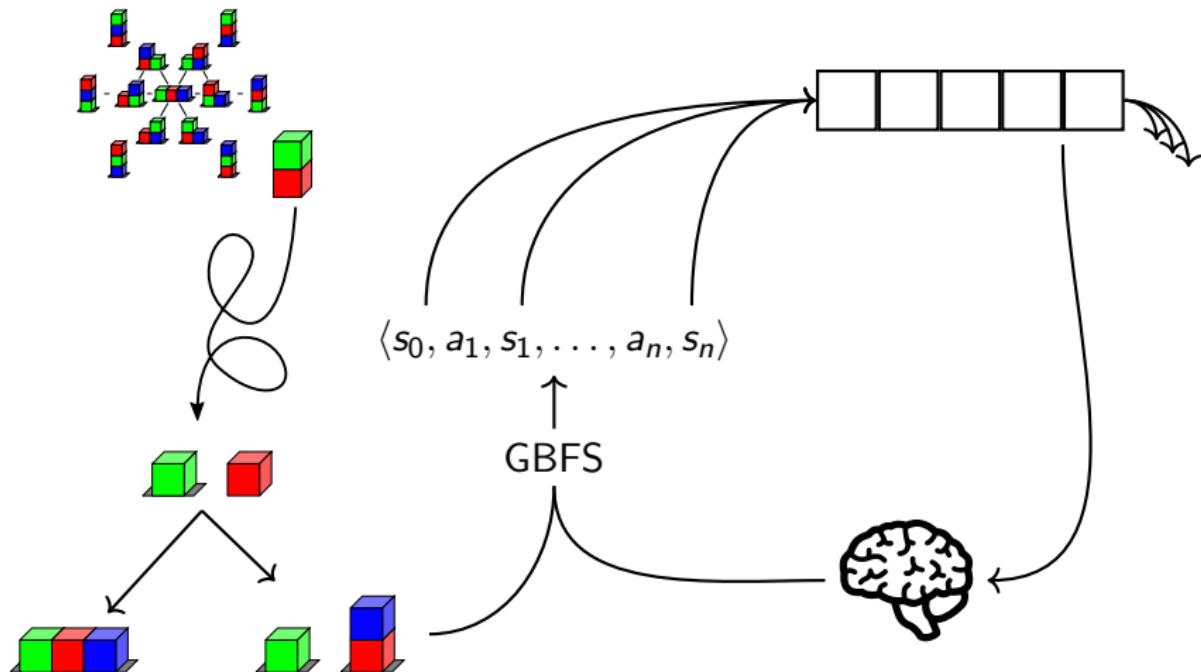
Framework  
●○○

Experiemts  
oooooo

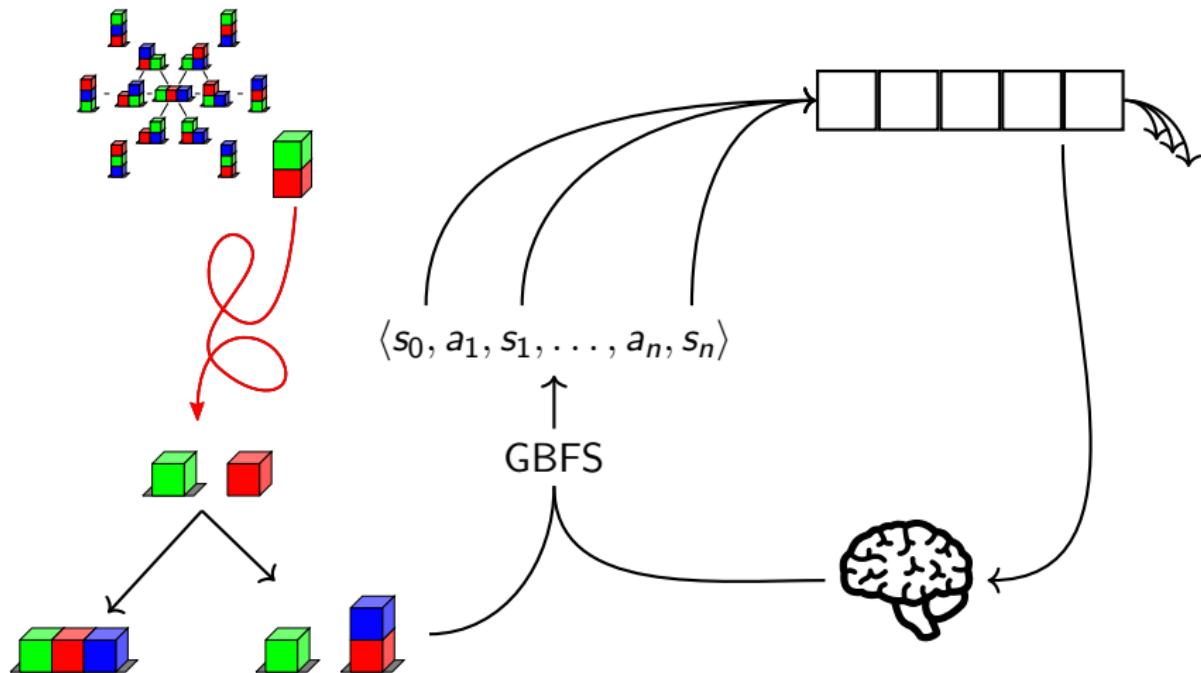
# Goal-Distance Estimator



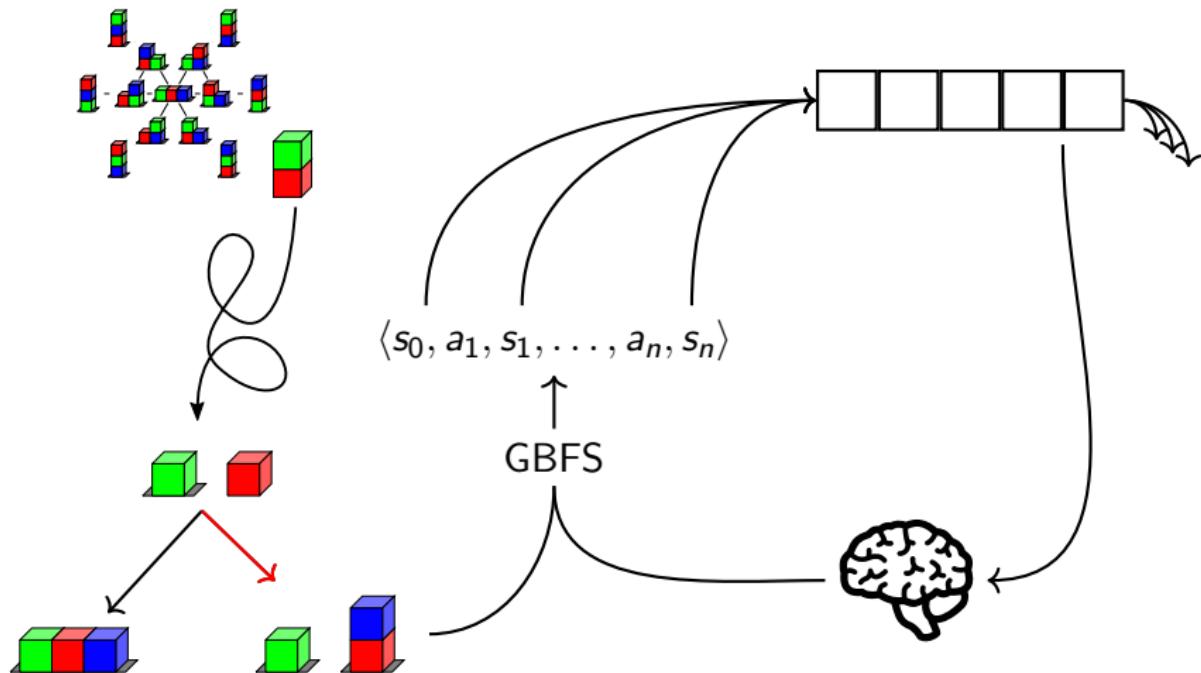
# Goal-Distance Estimator



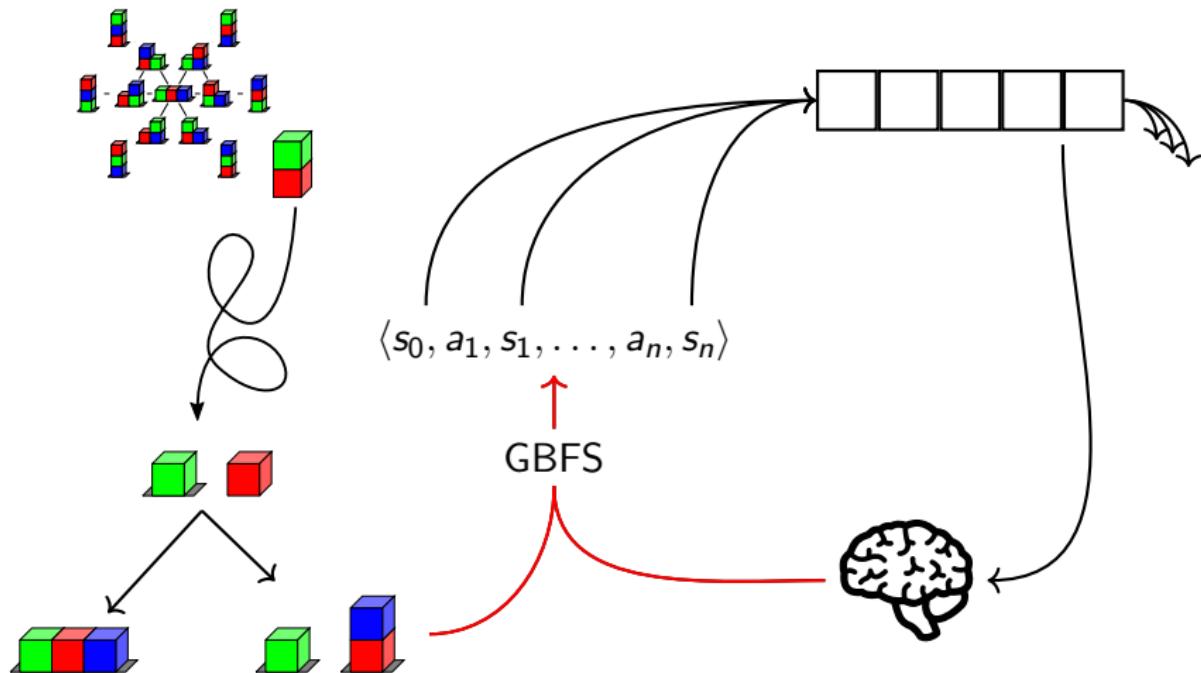
# Goal-Distance Estimator



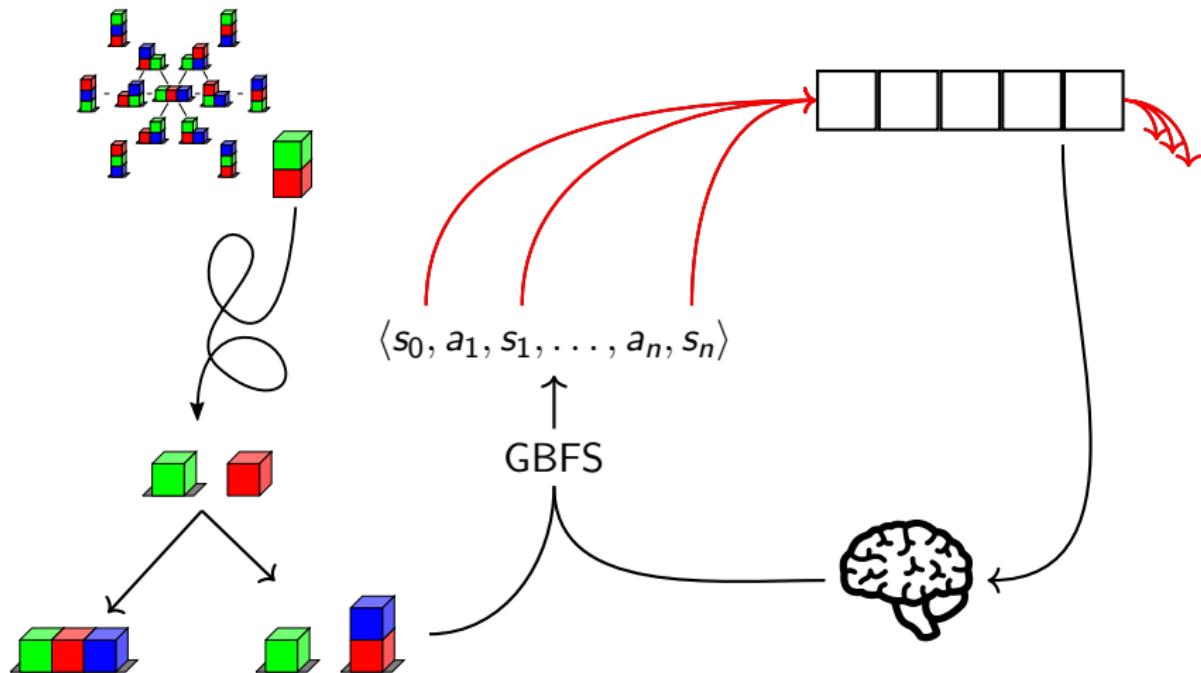
# Goal-Distance Estimator



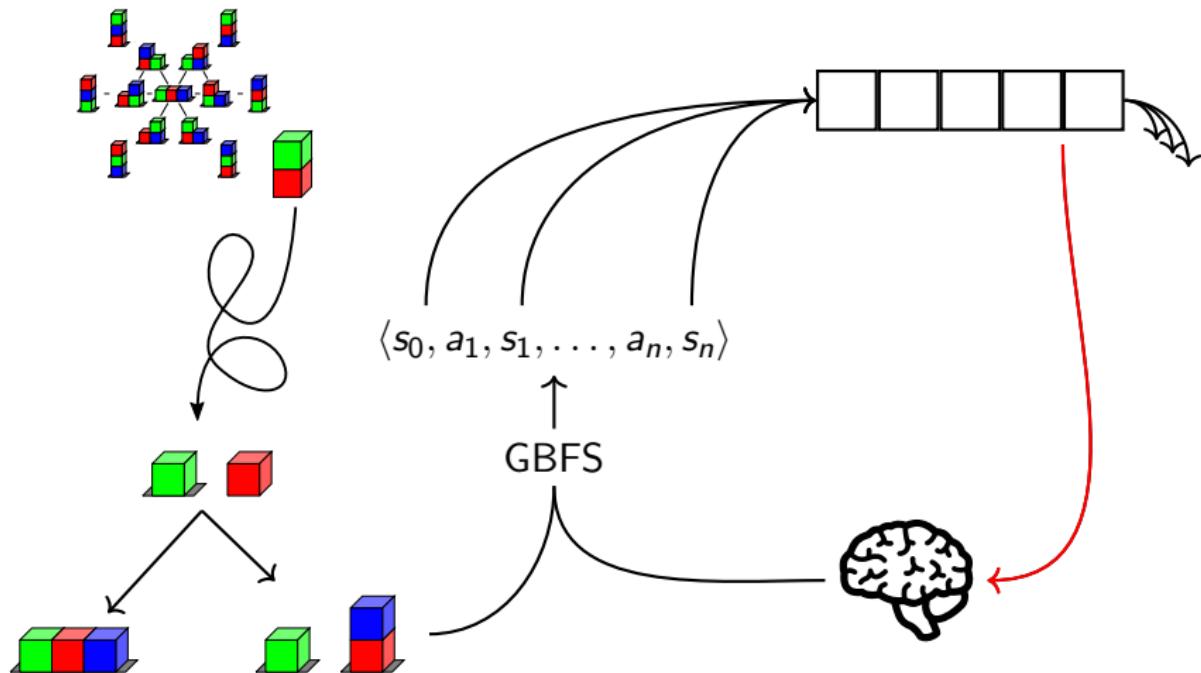
# Goal-Distance Estimator



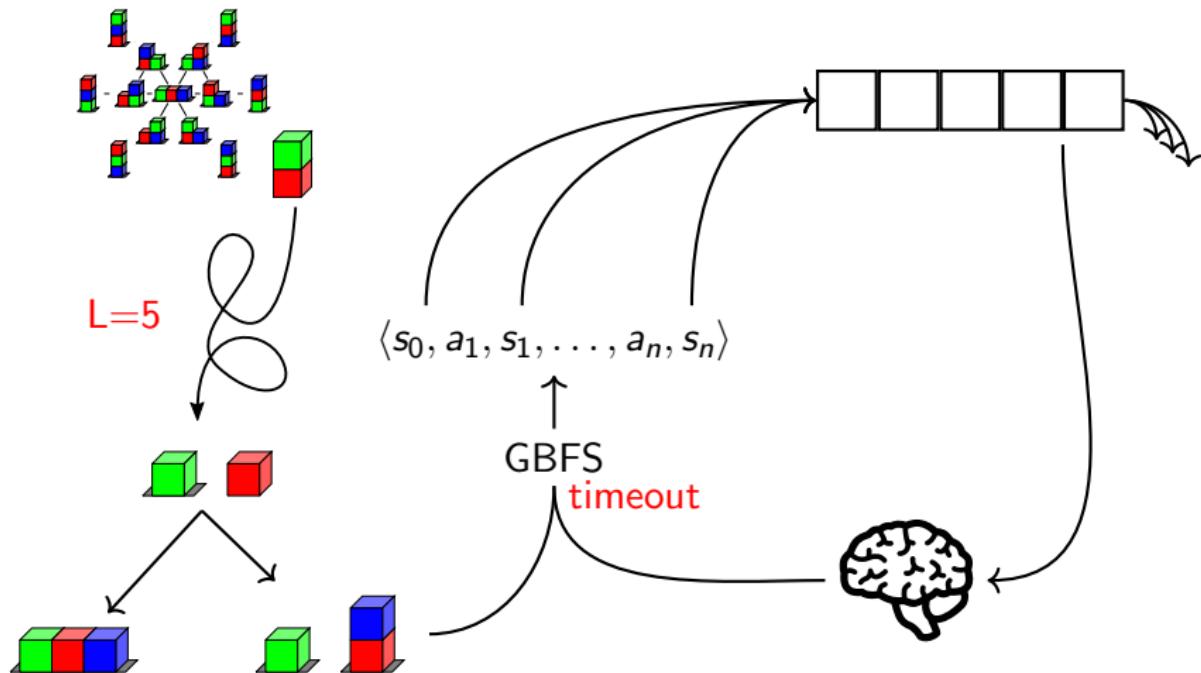
# Goal-Distance Estimator



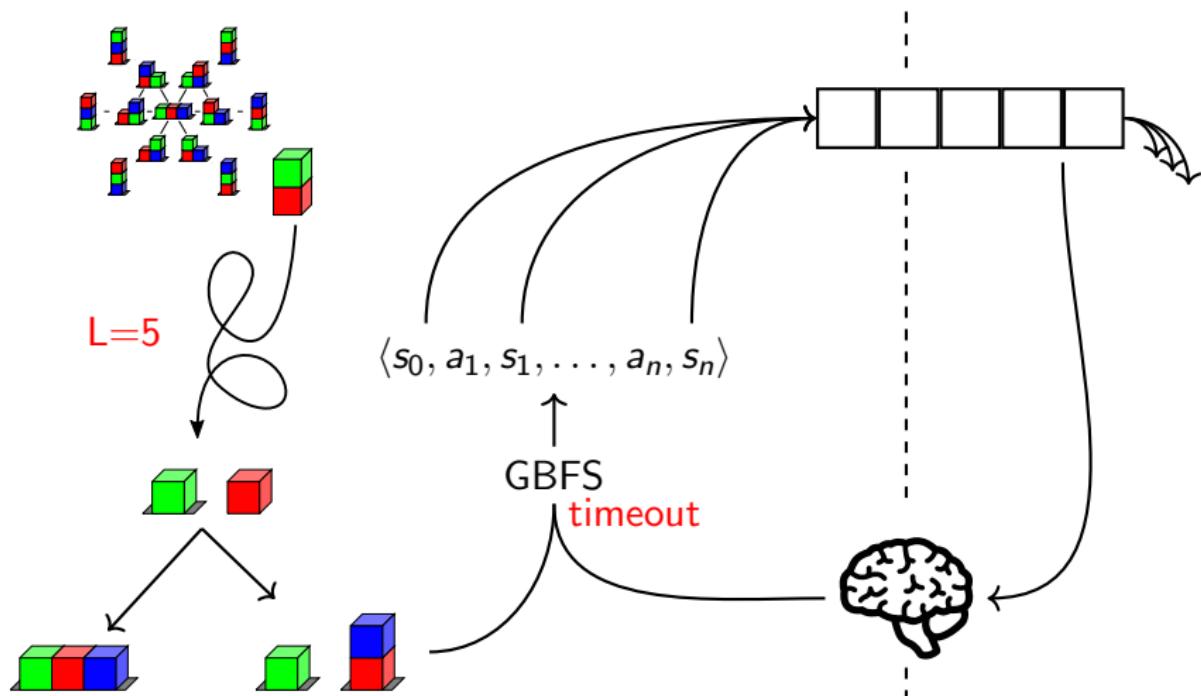
# Goal-Distance Estimator



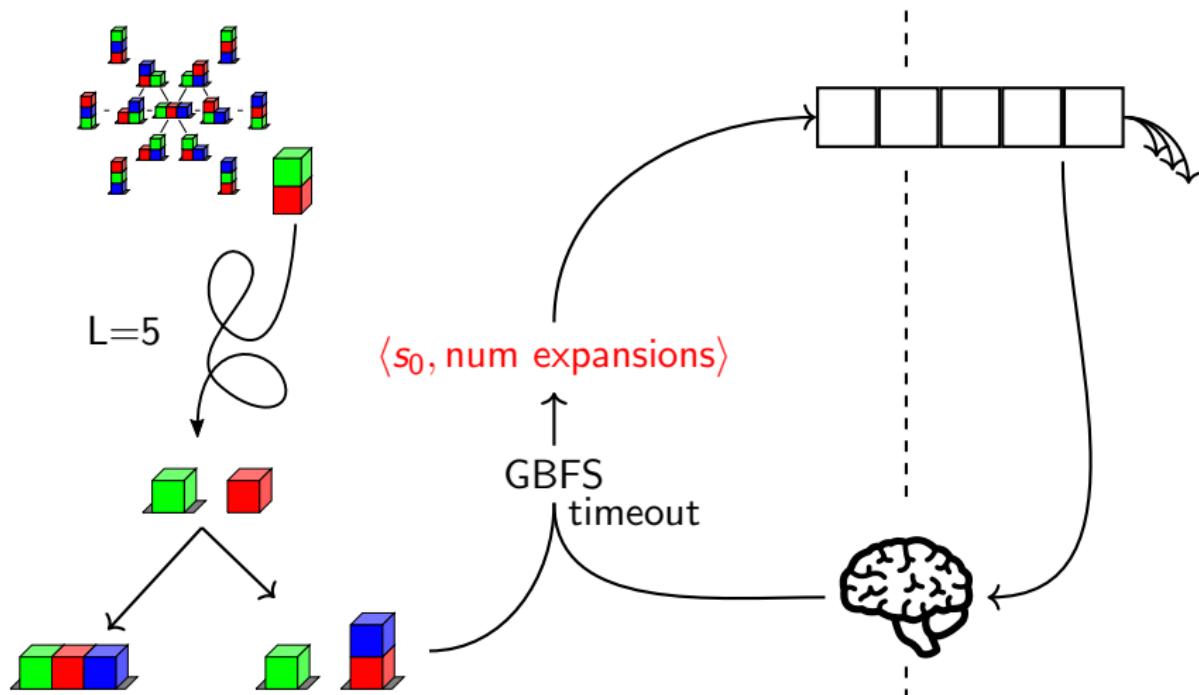
# Goal-Distance Estimator



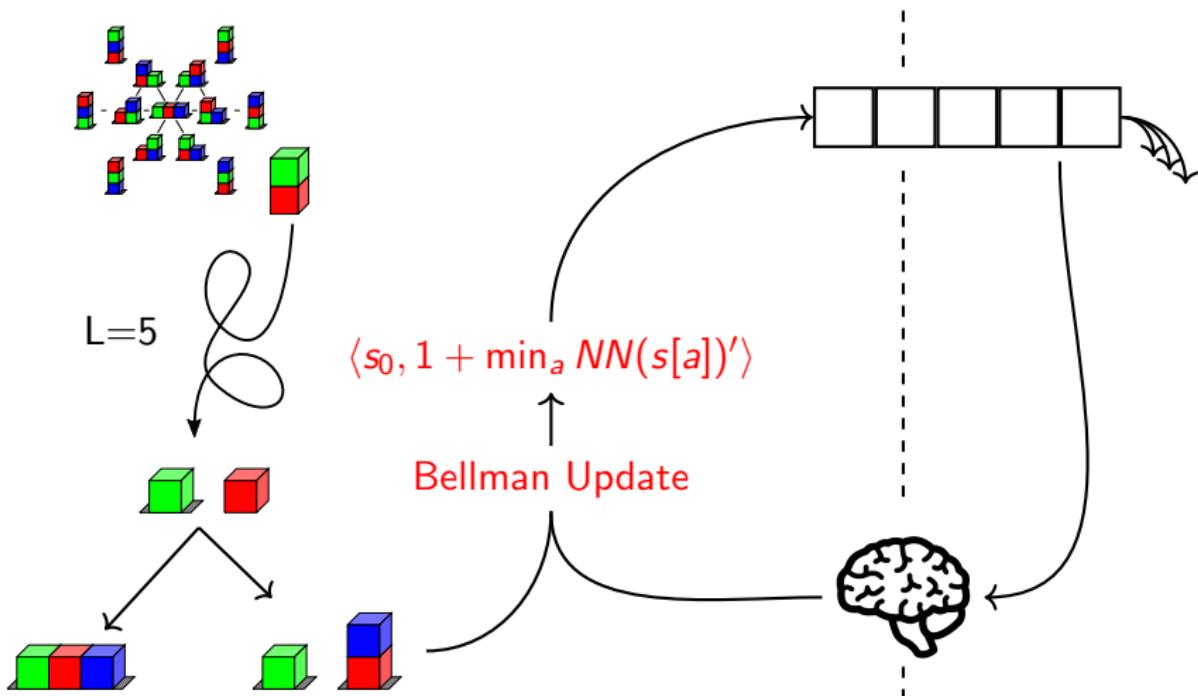
# Goal-Distance Estimator



# Search-Space-Size Estimator



# Approximate Value Iteration



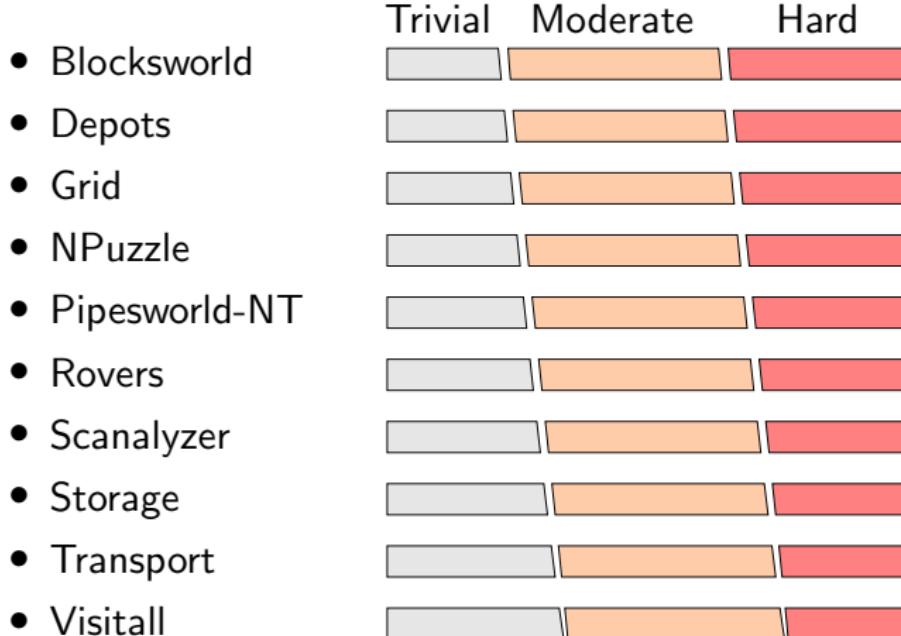
# Algorithms

- $h^{GD}$  Goal-Distance Estimator
- $h^{SE}$  Search-Space-Size Estimator
- $h^{AVI}$  Approximate value iteration
- $h^{SL}$  Ferber, Helmert, and Hoffmann (2020)
- $h^{HGN}$  Shen, Trevizan, and Thiébaux (2020)
- $h^{FF}$  Hoffmann and Nebel (2001)
- *LAMA* Richter and Westphal (2010)

# Benchmarks (Ferber, Helmert, and Hoffmann, 2020)

- Blocksworld
- Depots
- Grid
- NPuzzle
- Pipesworld-NT
- Rovers
- Scanalyzer
- Storage
- Transport
- Visitall

# Benchmarks (Ferber, Helmert, and Hoffmann, 2020)



# Coverage (Moderate Tasks)

Domain	$h^{GD}$	$h^{SE}$	$h^{AVI}$
blocks	<b>18.0</b>	0.0	0.0
depots	<b>60.3</b>	32.7	54.7
grid	<b>100.0</b>	<b>100.0</b>	51.0
npuzzle	<b>28.0</b>	0.0	1.0
pipes-nt	57.8	<b>68.4</b>	50.2
rovers	<b>48.2</b>	21.8	45.0
scanalyzer	33.3	<b>70.7</b>	67.3
storage	<b>89.0</b>	57.5	69.5
transport	<b>100.0</b>	<b>100.0</b>	87.5
visitall	<b>55.3</b>	0.0	0.0

# Coverage (Moderate Tasks)

Domain	$h^{GD}$	$h^{SE}$	$h^{AVI}$	$h^{SL}$	$h^{HGN}$
blocks	18.0	0.0	0.0	80.4	<b>100.0</b>
depots	60.3	32.7	54.7	<b>90.3</b>	0.0
grid	<b>100.0</b>	<b>100.0</b>	51.0	93.0	0.0
npuzzle	<b>28.0</b>	0.0	1.0	0.0	0.3
pipes-nt	57.8	68.4	50.2	<b>92.2</b>	7.6
rovers	<b>48.2</b>	21.8	45.0	26.0	14.0
scanalyzer	33.3	70.7	67.3	<b>82.7</b>	11.0
storage	<b>89.0</b>	57.5	69.5	24.5	0.0
transport	<b>100.0</b>	<b>100.0</b>	87.5	99.2	94.7
visitall	55.3	0.0	0.0	0.0	<b>100.0</b>

# Coverage (Moderate Tasks)

Domain	$h^{GD}$	$h^{SE}$	$h^{AVI}$	$h^{SL}$	$h^{HGN}$	$h^{FF}$	$LAMA$
blocks	18.0	0.0	0.0	80.4	<b>100.0</b>	98.8	<b>100.0</b>
depots	60.3	32.7	54.7	<b>90.3</b>	0.0	98.0	<b>100.0</b>
grid	<b>100.0</b>	<b>100.0</b>	51.0	93.0	0.0	96.0	<b>100.0</b>
npuzzle	<b>28.0</b>	0.0	1.0	0.0	0.3	97.5	<b>100.0</b>
pipes-nt	57.8	68.4	50.2	<b>92.2</b>	7.6	82.4	<b>99.4</b>
rovers	<b>48.2</b>	21.8	45.0	26.0	14.0	84.2	<b>100.0</b>
scanalyzer	33.3	70.7	67.3	<b>82.7</b>	11.0	98.3	<b>100.0</b>
storage	<b>89.0</b>	57.5	69.5	24.5	0.0	<b>48.0</b>	<b>38.5</b>
transport	<b>100.0</b>	<b>100.0</b>	87.5	99.2	94.7	98.5	<b>100.0</b>
visitall	55.3	0.0	0.0	0.0	<b>100.0</b>	93.3	<b>100.0</b>

# Coverage (Hard Tasks)

Domain	$h^{GD}$	$h^{SE}$	$h^{AVI}$	$h^{SL}$	$h^{HGN}$	$h^{FF}$	$LAMA$
blocks	0.0	0.0	0.0	0.0	<b>50.0</b>	61.6	<b>96.8</b>
depots	8.3	4.3	12.9	<b>35.4</b>	0.0	36.0	<b>82.6</b>
grid	87.8	<b>95.0</b>	70.5	60.2	0.0	53.2	<b>100.0</b>
npuzzle	0.0	0.0	0.0	0.0	0.0	33.2	<b>86.5</b>
pipes-nt	23.4	19.1	8.0	<b>48.7</b>	0.0	27.4	<b>69.3</b>
rovers	2.8	0.8	<b>6.5</b>	1.5	0.3	13.9	<b>100.0</b>
scanalyzer	3.3	0.0	<b>60.7</b>	60.0	0.0	98.0	<b>100.0</b>
storage	<b>27.2</b>	13.2	15.8	0.0	0.0	<b>13.8</b>	<b>11.5</b>
transport	0.0	0.0	<b>2.4</b>	0.0	0.0	0.0	<b>92.8</b>
visitall	28.0	0.0	0.0	0.0	<b>100.0</b>	74.0	<b>100.0</b>

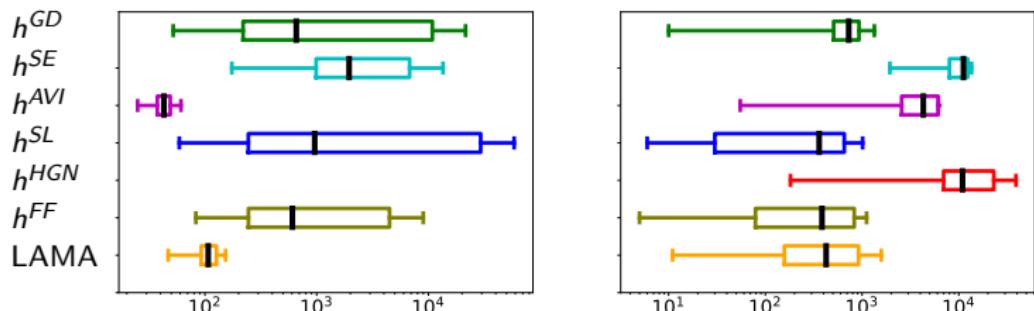
Introduction  
○○○○

Background  
○○○○

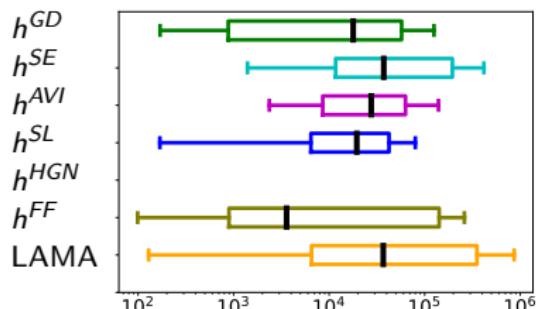
Framework  
○○○

Experiments  
○○○○●○

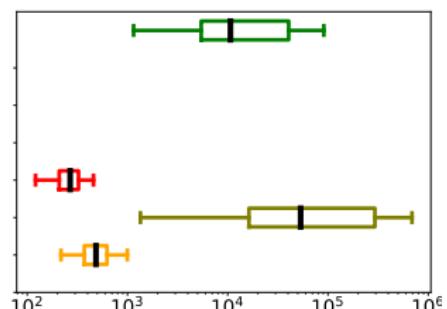
# Expansions



(a) Grid



(b) Scalyzer



(c) Storage

(d) Visitall

# Conclusion

- three new per-instance heuristics
- large scale comparison to previous work
  - trained heuristics highly complementary
  - in general, model-based heuristics win
  - all our heuristics superior in Storage



Paper &  
Supplement

# References I

- Agostinelli, F.; McAleer, S.; Shmakov, A.; and Baldi, P. 2019. Solving the Rubik's cube with deep reinforcement learning and search. Nature Machine Intelligence, 1: 356–363.
- Ferber, P.; Helmert, M.; and Hoffmann, J. 2020. Neural Network Heuristics for Classical Planning: A Study of Hyperparameter Space. In De Giacomo, G., ed., Proceedings of the 24th European Conference on Artificial Intelligence (ECAI 2020), 2346–2353. IOS Press.
- He, K.; Zhang, X.; Ren, S.; and Sun, J. 2016. Deep Residual Learning for Image Recognition. In Proceedings of the 2016 IEEE Conference on Computer Vision and Pattern Recognition, 770–778. IEEE Computer Society.
- Helmert, M. 2009. Concise Finite-Domain Representations for PDDL Planning Tasks. Artificial Intelligence, 173: 503–535.
- Hoffmann, J.; and Nebel, B. 2001. The FF Planning System: Fast Plan Generation Through Heuristic Search. Journal of Artificial Intelligence Research, 14: 253–302.

## References II

- Karia, R.; and Srivastava, S. 2021. Learning Generalized Relational Heuristic Networks for Model-Agnostic Planning. In Leyton-Brown, K.; and Mausam, eds., Proceedings of the Thirty-Fifth AAAI Conference on Artificial Intelligence (AAAI 2021), 8064–8073. AAAI Press.
- Richter, S.; and Westphal, M. 2010. The LAMA Planner: Guiding Cost-Based Anytime Planning with Landmarks. Journal of Artificial Intelligence Research, 39: 127–177.
- Shen, W.; Trevizan, F.; and Thiébaut, S. 2020. Learning Domain-Independent Planning Heuristics with Hypergraph Networks. In Beck, J. C.; Karpas, E.; and Sohrabi, S., eds., Proceedings of the Thirtieth International Conference on Automated Planning and Scheduling (ICAPS 2020), 574–584. AAAI Press.
- Silver, D.; Huang, A.; Maddison, C. J.; Guez, A.; Sifre, L.; van den Driessche, G.; Schrittwieser, J.; Antonoglou, I.; Panneershelvam, V.; Lanctot, M.; Dieleman, S.; Grewe, D.; Nham, J.; Kalchbrenner, N.; Sutskever, I.; Lillicrap, T.; Leach, M.; Kavukcuoglu, K.; Graepel, T.; and Hassabis, D. 2016. Mastering the Game of Go with Deep Neural Networks and Tree Search. Nature, 529(7587): 484–489.

## References III

- Silver, D.; Hubert, T.; Schrittwieser, J.; Antonoglou, I.; Lai, M.; Guez, A.; Lanctot, M.; Sifre, L.; Kumaran, D.; Graepel, T.; Lillicrap, T.; Simonyan, K.; and Hassabis, D. 2018. A general reinforcement learning algorithm that masters chess, shogi, and Go through self-play. Science, 362(6419): 1140–1144.
- Silver, D.; Schrittwieser, J.; Simonyan, K.; Antonoglou, I.; Huang, A.; Guez, A.; Hubert, T.; Baker, L.; Lai, M.; Bolton, A.; Chen, Y.; Lillicrap, T.; Hui, F.; Sifre, L.; van den Driessche, G.; Graepel, T.; and Hassabis, D. 2017. Mastering the Game of Go Without Human Knowledge. Nature, 550(7676): 354–359.