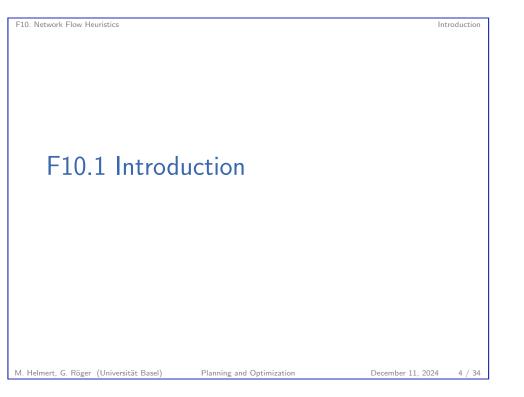
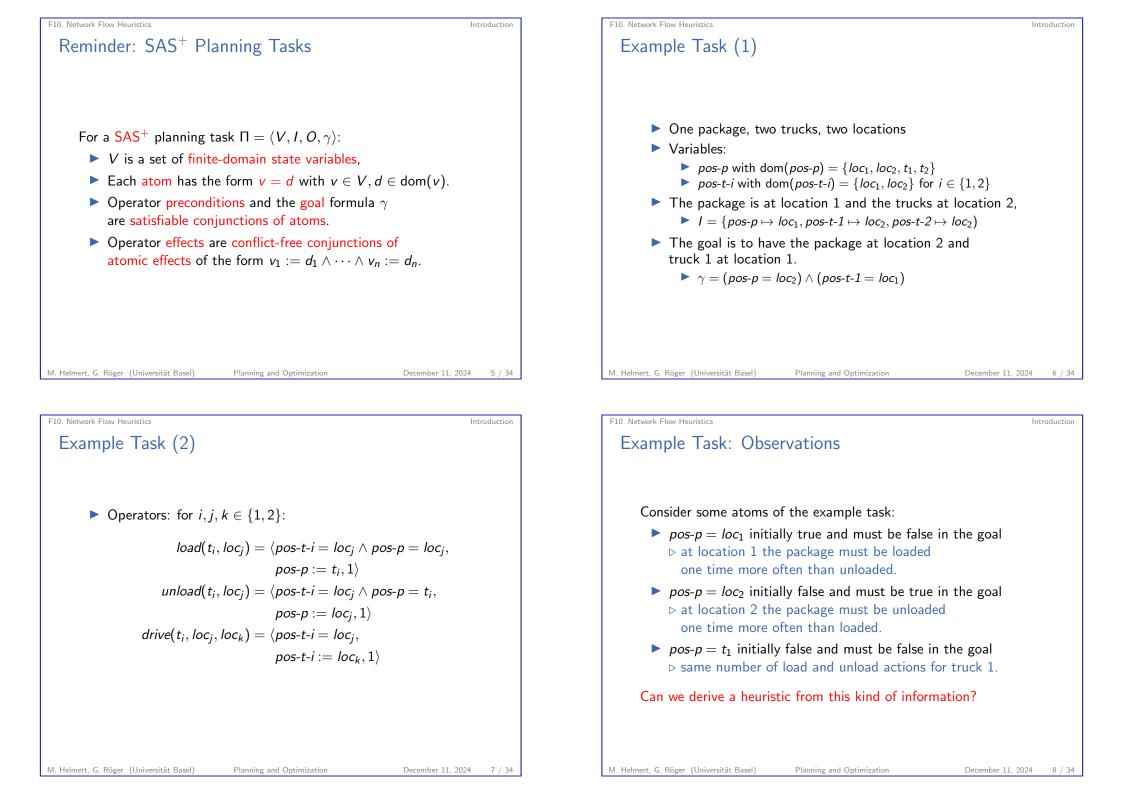
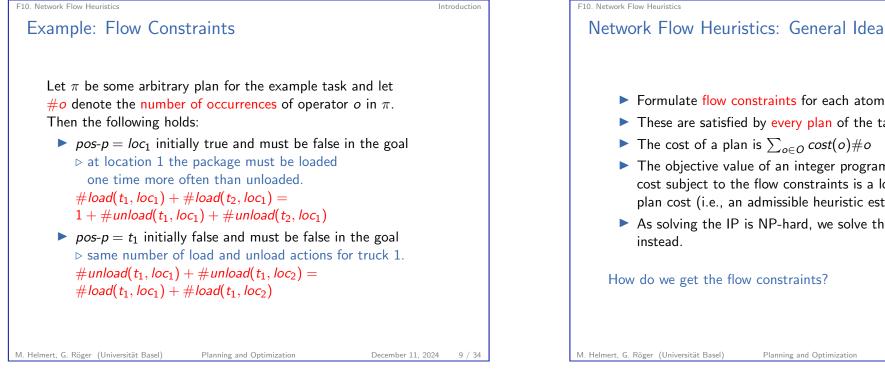


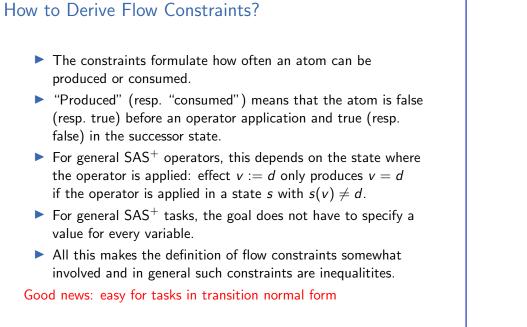
Planning and Optimi December 11, 2024 — F10. Ne				
F10.1 Introduction	ı			
F10.2 Transition Normal Form				
F10.3 Flow Heuristic				
F10.4 Summary				
M. Helmert, G. Röger (Universität Basel)	Planning and Optimization	December 11, 2024	2 / 34	







F10. Network Flow Heuristics



Planning and Optimization

M. Helmert, G	. Röger (Universität Basel)	Planning and Optimization	December 11, 2024	10 / 3
Hov	w do we get the flow	w constraints?		
	cost subject to the plan cost (i.e., an	e flow constraints is a lo admissible heuristic esti is NP-hard, we solve the	wer bound on the mate).	
		n is ∑ <sub>o∈O</sub> cost(o)#o ue of an integer program	that minimizes this	
		d by every plan of the ta		
		onstraints for each atom.		

# F10.2 Transition Normal Form

Planning and Optimization

Introduction

10 / 34

11 / 34

These are related to the variables that occur in conditions and effects of the task.

### Definition $(vars(\varphi), vars(e))$

For a logical formula  $\varphi$  over finite-domain variables V, vars( $\varphi$ ) denotes the set of finite-domain variables occurring in  $\varphi$ .

For an effect e over finite-domain variables V, vars(e) denotes the set of finite-domain variables occurring in e.

Planning and Optimization

M. Helmert, G. Röger (Universität Basel)

December 11, 2024

Transition Normal Form

F10. Network Flow Heuristics

#### Converting Operators to TNF: Multiplying Out Converting Operators to TNF: Violations Solution 1: multiplying out • While there exists an operator *o* and a variable There are two ways in which an operator o can violate TNF: $v \in vars(eff(o))$ with $v \notin vars(pre(o))$ : ▶ There exists a variable $v \in vars(pre(o)) \setminus vars(eff(o))$ . For each $d \in \text{dom}(v)$ , add a new operator that is like o • There exists a variable $v \in vars(eff(o)) \setminus vars(pre(o))$ . but with the additional precondition v = d. Remove the original operator. The first case is easy to address: if v = d is a precondition 2 Repeat the previous step until no more such variables exist. with no effect on v, just add the effect v := d. The second case is more difficult: if we have the effect v := dProblem: but no precondition on v, how can we add a precondition on v $\blacktriangleright$ If an operator *o* has *n* such variables, each with *k* values without changing the meaning of the operator? in its domain, this introduces $k^n$ variants of o. ▶ Hence, this is an exponential transformation.

13 / 34

Transition Normal Form

## Transition Normal Form

Definition (Transition Normal Form) A SAS<sup>+</sup> planning task  $\Pi = \langle V, I, O, \gamma \rangle$ 

is in transition normal form (TNF) if

- ▶ for all  $o \in O$ , vars(pre(o)) = vars(eff(o)), and
- $\blacktriangleright$  vars( $\gamma$ ) = V.

In words, an operator in TNF must mention the same variables in the precondition and effect, and a goal in TNF must mention all variables (= specify exactly one goal state).

Planning and Optimization

M. Helmert, G. Röger (Universität Basel)

F10. Network Flow Heuristics

December 11, 2024 14 / 34

Transition Normal Form

Transition Normal Form

## Converting Operators to TNF: Auxiliary Values

#### Solution 2: auxiliary values

- For every variable v, add a new auxiliary value u to its domain.
- Por every variable v and value d ∈ dom(v) \ {u}, add a new operator to change the value of v from d to u at no cost: (v = d, v := u, 0).
- For all operators o and all variables v ∈ vars(eff(o)) \ vars(pre(o)), add the precondition v = u to pre(o).

#### **Properties:**

- Transformation can be computed in linear time.
- Due to the auxiliary values, there are new states and transitions in the induced transition system, but all path costs between original states remain the same.

Planning and Optimization

M. Helmert, G. Röger (Universität Basel)

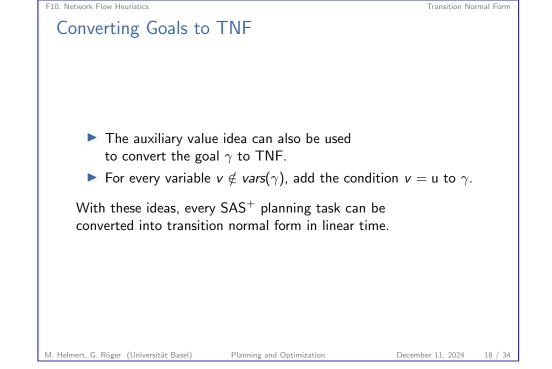
December 11, 2024 17 / 34

Transition Normal Form

F10. Network Flow Heuristics TNF for Example Task (1)

The example task is not in transition normal form:

- Load and unload operators have preconditions on the position of some truck but no effect on this variable.
- ▶ The goal does not specify a value for variable *pos-t-2*.



F10. Network Flow Heuristics

## TNF for Example Task (2)

Operators in transition normal form: for  $i, j, k \in \{1, 2\}$ :

```
\begin{split} \textit{load}(t_i,\textit{loc}_j) &= \langle\textit{pos-t-i} = \textit{loc}_j \land \textit{pos-p} = \textit{loc}_j,\\ \textit{pos-p} &:= t_i \land \textit{pos-t-i} := \textit{loc}_j, 1 \rangle\\ \textit{unload}(t_i,\textit{loc}_j) &= \langle\textit{pos-t-i} = \textit{loc}_j \land \textit{pos-p} = t_i,\\ \textit{pos-p} &:= \textit{loc}_j \land \textit{pos-t-i} := \textit{loc}_j, 1 \rangle\\ \textit{drive}(t_i,\textit{loc}_j,\textit{loc}_k) &= \langle\textit{pos-t-i} = \textit{loc}_j,\\ \textit{pos-t-i} := \textit{loc}_k, 1 \rangle \end{split}
```

Planning and Optimization

20 / 34

Transition Normal Form

21 / 34

23 / 34

Flow Heuristic

## TNF for Example Task (3)

To bring the goal in normal form,

- ▶ add an additional value **u** to dom(*pos-t-2*)
- add zero-cost operators
  - $o_1 = \langle pos-t-2 = loc_1, pos-t-2 := \mathbf{u}, \mathbf{0} \rangle$  and  $o_2 = \langle pos-t-2 = loc_2, pos-t-2 := \mathbf{u}, \mathbf{0} \rangle$
- Add *pos-t-2* =  $\mathbf{u}$  to the goal:  $\gamma = (pos-p = loc_2) \land (pos-t-1 = loc_1) \land (pos-t-2 = \mathbf{u})$

Planning and Optimization

M. Helmert, G. Röger (Universität Basel)

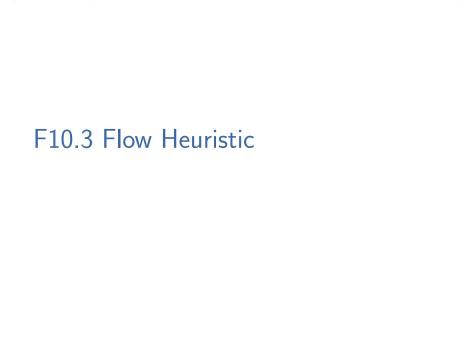
December 11, 2024

F10. Network Flow Heuristics Notation

> ► In SAS<sup>+</sup> tasks, states are variable assignments, conditions are conjunctions over atoms, and effects are conjunctions of atomic effects.

- ▶ In the following, we use a unifying notation to express that an atom is true in a state/entailed by a condition/ made true by an effect.
- For state s, we write  $(v = d) \in s$  to express that s(v) = d.
- For a conjunction of atoms  $\varphi$ , we write  $(v = d) \in \varphi$  to express that  $\varphi$  has a conjunct v = d (or alternatively  $\varphi \models v = d$ ).
- For effect e, we write  $(v = d) \in e$  to express that e contains the atomic effect v := d.

Planning and Optimization



Planning and Optimization

M. Helmert, G. Röger (Universität Basel)

F10. Network Flow Heuristics

December 11, 2024 22 / 34

Flow Heuristic

# F10. Network Flow Heuristics Flow Heuristic Flow Constraints (1) A flow constraint for an atom relates how often it can be produced to how often it can be consumed. Let *o* be an operator in transition normal form. Then: • o produces atom a iff $a \in eff(o)$ and $a \notin pre(o)$ . • o consumes atom a iff $a \in pre(o)$ and $a \notin eff(o)$ . Otherwise o is neutral wrt. atom a. → State-independent Planning and Optimization December 11, 2024 24 / 34

#### F10. Network Flow Heuristics

Flow Heuristic

## Flow Constraints (2)

A flow constraint for an atom relates how often it can be produced to how often it can be consumed.

The constraint depends on the current state *s* and the goal  $\gamma$ . If  $\gamma$  mentions all variables (as in TNF), the following holds:

- If a ∈ s and a ∈ γ then atom a must be equally often produced and consumed.
- Analogously for  $a \notin s$  and  $a \notin \gamma$ .
- If a ∈ s and a ∉ γ then a must be consumed one time more often than it is produced.
- If a ∉ s and a ∈ γ then a must be produced one time more often than it is consumed.

Planning and Optimization

M. Helmert, G. Röger (Universität Basel)

F10. Network Flow Heuristics

December 11, 2024 25 / 34

Flow Heuristic

Flow Constraints (3)

Definition (Flow Constraint) Let  $\Pi = \langle V, I, O, \gamma \rangle$  be a task in transition normal form. The flow constraint for atom *a* in state *s* is

$$[a \in s] + \sum_{o \in O: a \in eff(o)} \mathsf{Count}_o = [a \in \gamma] + \sum_{o \in O: a \in pre(o)} \mathsf{Count}_o$$

- Count<sub>o</sub> is an LP variable for the number of occurrences of operator o.
- Neutral operators either appear on both sides or on none.

#### F10. Network Flow Heuristics

## Iverson Bracket

The dependency on the current state and the goal can concisely be expressed with lverson brackets:

#### Definition (Iverson Bracket)

Let P be a logical proposition (= some statement that can be evaluated to true or false). Then

 $[P] = \begin{cases} 1 & \text{if } P \text{ is true} \\ 0 & \text{if } P \text{ is false.} \end{cases}$ 

Planning and Optimization

Example:  $[2 \neq 3] = 1$ 

M. Helmert, G. Röger (Universität Basel)

December 11, 2024

F10. Network Flow Heuristics Flow Heuristic Definition (Flow Heuristic) Let  $\Pi = \langle V, I, O, \gamma \rangle$  be a SAS<sup>+</sup> task in transition normal form and let  $A = \{(v = d) \mid v \in V, d \in dom(v)\}$  be the set of atoms of  $\Pi$ . The flow heuristic  $h^{flow}(s)$  is the objective value of the following LP or  $\infty$  if the LP is infeasible: minimize  $\sum_{o \in O} cost(o) \cdot Count_o$  subject to  $[a \in s] + \sum_{o \in O: a \in eff(o)} Count_o = [a \in \gamma] + \sum_{o \in O: a \in pre(o)} Count_o$  for all  $a \in A$  $Count_o \ge 0$  for all  $o \in O$ 

Planning and Optimization

26 / 34

