

# Planning and Optimization

## F3. Landmarks: Orderings & LM-Count Heuristic

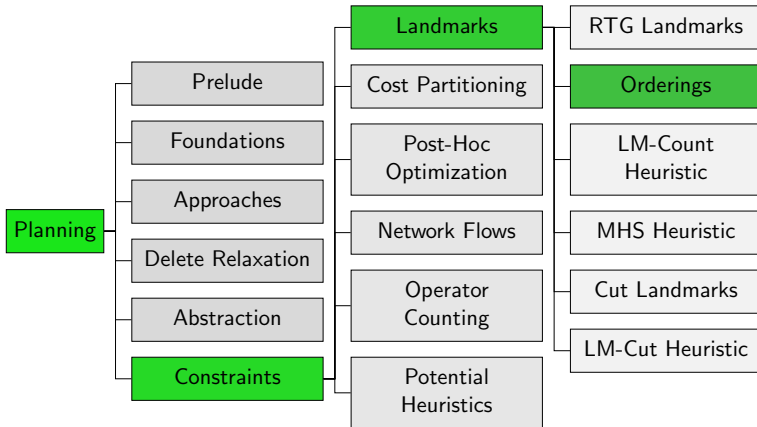
Malte Helmert and Gabriele Röger

Universität Basel

December 2, 2024

# Landmark Orderings

# Content of the Course



## Why Landmark Orderings?

- To compute a landmark heuristic estimate for state  $s$  we need landmarks for  $s$ .
- We could invest the time to compute them **for every state from scratch**.
- Alternatively, we can **compute landmarks once** and **propagate** them over operator applications.
- **Landmark orderings** are used to detect landmarks that should be further considered because they (again) need to be satisfied later.
- (We will later see yet another approach, where heuristic computation and landmark computation are integrated  $\rightsquigarrow$  LM-Cut.)

## Example

Consider task  $\langle \{a, b, c, d\}, I, \{o_1, o_2, \dots, o_n\}, d \rangle$  with

- $I(v) = \perp$  for  $v \in \{a, b, c, d\}$ ,
- $o_1 = \langle \top, a \wedge b \rangle$ , and
- $o_2 = \langle a, c \wedge \neg a \wedge \neg b \rangle$  (plus some more operators).

You know that  $a, b, c$  and  $d$  are all fact landmarks for  $I$ .

- What landmarks are still required to be made true in state  $I[\langle o_1, o_2 \rangle]$ ?

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- What landmarks are still required to be made true in state  $I[\langle o_1, o_2 \rangle]$ ?
- You get the additional information that variable  $a$  must be true immediately before  $d$  is first made true. Any changes?

# Terminology

Let  $\pi = \langle o_1, \dots, o_n \rangle$  be a sequence of operators applicable in state  $I$  and let  $\varphi$  be a formula over the state variables.

- $\varphi$  is **true at time  $i$**  if  $I[\langle o_1, \dots, o_i \rangle] \models \varphi$ .
- Also special case  $i = 0$ :  $\varphi$  is **true at time 0** if  $I \models \varphi$ .
- No formula is true at time  $i < 0$ .
- $\varphi$  is **added at time  $i$**  if it is **true at time  $i$  but not at time  $i - 1$** .
- $\varphi$  is **first added at time  $i$**  if it is **true at time  $i$  but not at any time  $j < i$** .  
We denote this  $i$  by ***first*** $(\varphi, \pi)$ .
- ***last*** $(\varphi, \pi)$  denotes the last time in which  $\varphi$  is added in  $\pi$ .

# Landmark Orderings

## Definition (Landmark Orderings)

Let  $\varphi$  and  $\psi$  be formula landmarks. There is

- a **natural ordering** between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow \psi$ ) if in each plan  $\pi$  it holds that  $first(\varphi, \pi) < first(\psi, \pi)$ .  
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“ $\varphi$  must be true some time strictly before  $\psi$  is first added.”
- a **greedy-necessary ordering** between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow_{gn} \psi$ ) if for every plan  $\pi = \langle o_1, \dots, o_n \rangle$  it holds that  $s[\langle o_1, \dots, o_{first(\psi, \pi)-1} \rangle] \models \varphi$ .  
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“ $\varphi$  must be true immediately before  $\psi$  is first added.”
- a **weak ordering** between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow_w \psi$ ) if in each plan  $\pi$  it holds that  $first(\varphi, \pi) < last(\psi, \pi)$ .  
“ $\varphi$  must be true some time before  $\psi$  is last added.”

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# Natural Orderings

## Definition

There is a **natural ordering** between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow \psi$ ) if in each plan  $\pi$  it holds that  $first(\varphi, \pi) < first(\psi, \pi)$ .

- We can directly determine natural orderings from the *LM* sets computed from the simplified relaxed task graph.
- For fact landmarks  $v, v'$  with  $v \neq v'$ , if  $n_{v'} \in LM(n_v)$  then  $v' \rightarrow v$ .

# Greedy-necessary Orderings

## Definition

There is a **greedy-necessary ordering** between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow_{\text{gn}} \psi$ ) if in each plan where  $\psi$  is first added at time  $i$ ,  $\varphi$  is true at time  $i - 1$ .

- We can again determine such orderings from the sRTG.
- For an OR node  $n_v$ , we define the set of **first achievers** as  $FA(n_v) = \{n_o \mid n_o \in \text{succ}(n_v) \text{ and } n_v \notin LM(n_o)\}$ .
- Then  $v' \rightarrow_{\text{gn}} v$  if  $n_{v'} \in \text{succ}(n_o)$  for all  $n_o \in FA(n_v)$ .

# Landmark Propagation

## Example Revisited

Consider task  $\langle \{a, b, c, d\}, I, \{o_1, o_2, \dots, o_n\}, d \rangle$  with

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- What landmarks are still required to be made true in state  $I[\langle o_1, o_2 \rangle]$ ? **All not achieved yet on the state path**
- You get the additional information that variable  $a$  must be true immediately before  $d$  is first made true. Any changes? **Exploit orderings to determine landmarks that are still required.**

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- There is another path to the same state where  $b$  was never true. What now? **Exploit information from multiple paths.**



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- Past landmarks are important for inferring which orderings are still relevant, future landmarks are relevant for the heuristic estimates.
- Since the exact sets are defined over **all** paths between certain states, we use approximations.

# Landmark State

## Definition

Let  $\mathcal{L}_I$  be a set of formula landmarks for the initial state.

A **landmark state**  $\mathbb{L}$  is  $\perp$  or a pair  $\langle \mathcal{L}_{\text{past}}, \mathcal{L}_{\text{fut}} \rangle$  such that  $\mathcal{L}_{\text{fut}} \cup \mathcal{L}_{\text{past}} = \mathcal{L}_I$ .

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$\mathbb{L}$  is **valid** in state  $s$  if

- $\mathbb{L} = \perp$  and  $\Pi$  has no  $s$ -plan, or
- $\mathbb{L} = \langle \mathcal{L}_{\text{past}}, \mathcal{L}_{\text{fut}} \rangle$  with  $\mathcal{L}_{\text{past}} \supseteq \mathcal{L}_{\text{past}}^*$  and  $\mathcal{L}_{\text{fut}} \subseteq \mathcal{L}_{\text{fut}}^*$ .

## Context in Search: LM-BFS Algorithm

```
 $\mathbb{L}(\text{init}), \mathcal{L}_I, \mathcal{O}_I := \text{compute\_landmark\_info}(\text{init}())$   
if  $h(\text{init}(), \mathbb{L}(\text{init})) < \infty$  then  
     $\text{open.insert}(\langle \text{init}(), 0, h(\text{init}(), \mathbb{L}(\text{init})) \rangle)$   
while  $\text{open} \neq \emptyset$  do  
     $\langle s, g, v \rangle = \text{open.pop}()$   
    if  $v < h(s, \mathbb{L}(s))$  then  
         $\text{open.insert}(\langle s, g, h(s, \mathbb{L}(s)) \rangle)$   
    else if  $g < \text{distances}(s)$  then  
         $\text{distances}(s) := g$   
    if  $\text{is\_goal}(s)$  then return  $\text{extract\_plan}(s)$ ;  
    foreach  $\langle a, s' \rangle \in \text{succ}(s)$  do  
         $\mathbb{L}' := \text{progress\_landmark\_state}(\mathbb{L}(s), \langle s, a, s' \rangle)$   
         $\mathbb{L}(s') := \text{merge\_landmark\_states}(\mathbb{L}(s'), \mathbb{L}')$   
        if  $\mathbb{L}(s') \neq \perp$  and  $h(s', \mathbb{L}(s')) < \infty$  then  
             $\text{open.insert}(\langle s', g + \text{cost}(a), h(s', \mathbb{L}(s')) \rangle)$ 
```

$\mathbb{L}(s) := \langle \mathcal{L}_I, \emptyset \rangle$  and  $\text{distances}(s) := \infty$  if read before set.



## Context: Exploit Information from Multiple Paths

```
 $\mathbb{L}(\text{init}), \mathcal{L}_I, \mathcal{O}_I := \text{compute\_landmark\_info}(\text{init}())$   
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$\mathbb{L}(s) := \langle \mathcal{L}_I, \emptyset \rangle$  and  $\text{distances}(s) := \infty$  if read before set.

## Merging Landmark States

Merging combines the information from two landmark states.

```
merge_landmark_states( $\mathbb{L}, \mathbb{L}'$ )
```

```
if  $\mathbb{L} = \perp$  or  $\mathbb{L}' = \perp$  then return  $\perp$ ;
```

```
 $\langle \mathcal{L}_{\text{past}}, \mathcal{L}_{\text{fut}} \rangle := \mathbb{L}$ 
```

```
 $\langle \mathcal{L}'_{\text{past}}, \mathcal{L}'_{\text{fut}} \rangle := \mathbb{L}'$ 
```

```
return  $\langle \mathcal{L}_{\text{past}} \cap \mathcal{L}'_{\text{past}}, \mathcal{L}_{\text{fut}} \cup \mathcal{L}'_{\text{fut}} \rangle$ 
```

### Theorem

*If  $\mathbb{L}$  and  $\mathbb{L}'$  are valid in a state  $s$  then also  $\text{merge\_landmark\_states}(\mathbb{L}, \mathbb{L}')$  is valid in  $s$ .*

## Context: Progression for a Transition

```
 $\mathbb{L}(\text{init}), \mathcal{L}_I, \mathcal{O}_I := \text{compute\_landmark\_info}(\text{init}())$   
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## Progressing Landmark States

- If we expand a state  $s$  with transition  $\langle s, o, s' \rangle$ , we use **progression** to determine a landmark state for  $s'$  from the one we know for  $s$ .

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- If we expand a state  $s$  with transition  $\langle s, o, s' \rangle$ , we use **progression** to determine a landmark state for  $s'$  from the one we know for  $s$ .
- We will only introduce progression methods that preserve the validity of landmark states.
- Since every progression method gives a valid landmark state, we can merge results from different methods into a valid landmark state.

# Basic Progression

## Definition (Basic Progression)

Basic progression maps landmark state  $\langle \mathcal{L}_{\text{past}}, \mathcal{L}_{\text{fut}} \rangle$  and transition  $\langle s, o, s' \rangle$  to landmark state  $\langle \mathcal{L}_{\text{past}} \cup \mathcal{L}_{\text{add}}, \mathcal{L}_{\text{fut}} \setminus \mathcal{L}_{\text{add}} \rangle$ , where  $\mathcal{L}_{\text{add}} = \{ \varphi \in \mathcal{L}_I \mid s \not\models \varphi \text{ and } s' \models \varphi \}$ .

“Extend the past with all landmarks added in  $s'$  and remove them from the future.”

# Goal Progression

## Definition (Goal Progression)

Let  $\gamma$  be the goal of the task.

Goal progression maps landmark state  $\langle \mathcal{L}_{\text{past}}, \mathcal{L}_{\text{fut}} \rangle$  and transition  $\langle s, o, s' \rangle$  to landmark state  $\langle \mathcal{L}_I, \mathcal{L}_{\text{goal}} \rangle$ , where  $\mathcal{L}_{\text{goal}} = \{ \varphi \in \mathcal{L}_I \mid \gamma \models \varphi \text{ and } s' \not\models \varphi \}$ .

“All landmarks that must be true in the goal but are false in  $s'$  must be achieved in the future.”



# Weak Ordering Progression

$\varphi \rightarrow_w \psi$ : “ $\varphi$  must be true some time before  $\psi$  is last added.”

## Definition (Weak Ordering Progression)

The weak ordering progression maps landmark state  $\langle \mathcal{L}_{\text{past}}, \mathcal{L}_{\text{fut}} \rangle$  and transition  $\langle s, o, s' \rangle$  to landmark state  $\langle \mathcal{L}_I, \{ \psi \mid \exists \varphi \rightarrow_w \psi : \varphi \notin \mathcal{L}_{\text{past}} \} \rangle$ .

“Landmark  $\psi$  must be added in the future because we haven’t done something that must be done before  $\psi$  is last added.”

# Greedy-necessary Ordering Progression

$\varphi \rightarrow_{\text{gn}} \psi$ : “ $\varphi$  must be true immediately before  $\psi$  is first added.”

## Definition (Greedy-necessary Ordering Progression)

The greedy necessary ordering progression maps landmark state  $\langle \mathcal{L}_{\text{past}}, \mathcal{L}_{\text{fut}} \rangle$  and transition  $\langle s, o, s' \rangle$  to landmark state

- $\perp$  if there is a  $\varphi \rightarrow_{\text{gn}} \psi \in \mathcal{O}_I$  with  $\psi \notin \mathcal{L}_{\text{past}}, s \not\models \varphi$  and  $s' \models \psi$ , and
- $\langle \mathcal{L}_I, \{\varphi \mid s' \not\models \varphi \text{ and } \exists \varphi \rightarrow_{\text{gn}} \psi \in \mathcal{O}_I : \psi \notin \mathcal{L}_{\text{past}}, s' \models \psi\} \rangle$  otherwise.

“Landmark  $\psi$  has not been true, yet, and  $\varphi$  must be true immediately before it becomes true. Since  $\varphi$  is currently false, we must make it true in the future (before making  $\psi$  true).”

# Natural Ordering Progression

$\varphi \rightarrow \psi$ :  $\varphi$  must be true some time strictly before  $\psi$  is first added.

## Definition (Natural Ordering Progression)

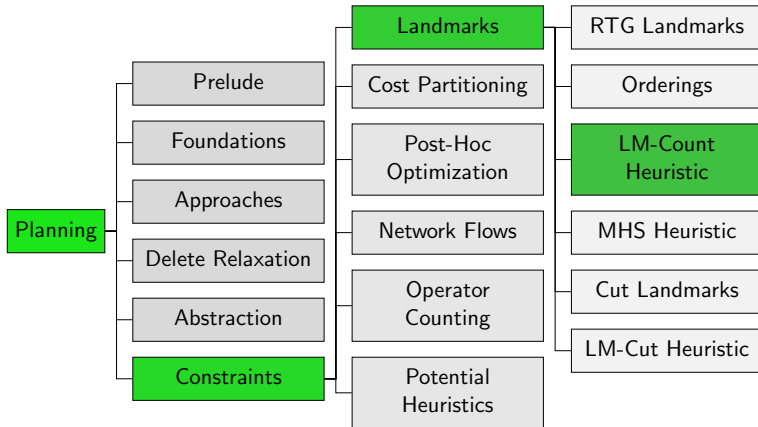
The natural ordering progression maps landmark state  $\langle \mathcal{L}_{\text{past}}, \mathcal{L}_{\text{fut}} \rangle$  and transition  $\langle s, o, s' \rangle$  to landmark state

- $\perp$  if there is a  $\varphi \rightarrow \psi \in \mathcal{O}_I$  with  $\varphi \notin \mathcal{L}_{\text{past}}$  and  $s' \models \psi$ , and
- $\langle \mathcal{L}_I, \emptyset \rangle$  otherwise.

Not (yet) useful: All known methods only find natural orderings that are true for every applicable operator sequence, so the interesting first case never happens in LM-BFS.

# Landmark-count Heuristic

# Content of the Course



# Landmark-count Heuristic

The landmark-count heuristic counts the landmarks that still have to be achieved.

## Definition (LM-count Heuristic)

Let  $\Pi$  be a planning task,  $s$  be a state and  $\mathbb{L} = \langle \mathcal{L}_{\text{past}}, \mathcal{L}_{\text{fut}} \rangle$  be a valid landmark state for  $s$ .

The **LM-count heuristic** for  $s$  and  $\mathbb{L}$  is

$$h^{\text{LM-count}}(s, \mathbb{L}) = \begin{cases} \infty & \text{if } \mathbb{L} = \perp, \\ |\mathcal{L}_{\text{fut}}| & \text{otherwise} \end{cases}$$

In the original work,  $\mathcal{L}_{\text{fut}}$  was determined without considering information from multiple paths and could not detect dead-ends.

# LM-count Heuristic is Path-dependent

- LM-count heuristic gives estimates for landmark states, which depend on the considered paths.
- Search algorithms need estimates for states.
- $\rightsquigarrow$  we use estimate from the **current** landmark state.
- $\rightsquigarrow$  heuristic estimate for a state is **not well-defined**.

# LM-count Heuristic is Inadmissible

## Example

Consider STRIPS planning task  $\Pi = \langle \{a, b\}, I, \{o\}, \{a, b\} \rangle$  with  $I = \emptyset$ ,  $o = \langle \emptyset, \{a, b\}, \emptyset, 1 \rangle$ . Let  $\mathcal{L} = \{a, b\}$  and  $\mathcal{O} = \emptyset$ .

Landmark state  $\langle \emptyset, \mathcal{L} \rangle$  for the initial state is valid and the estimate is  $h^{\text{LM-count}}(I, \langle \emptyset, \{a, b\} \rangle) = 2$  while  $h^*(I) = 1$ .

$\rightsquigarrow h^{\text{LM-count}}$  is **inadmissible**.



## LM-count Heuristic: Comments

- LM-Count alone is not a particularly informative heuristic.
- On the positive side, it complements  $h^{FF}$  very well.
- For example, the LAMA planning system alternates between expanding a state with minimal  $h^{FF}$  and minimal  $h^{LM-count}$  estimate.
- The LM-sum heuristic is a cost-aware variant of the heuristic that sums up the costs of the cheapest achiever (= operator that adds the fact landmark) of each landmark.
- There is an admissible variant of the heuristic based on operator cost partitioning.

# Summary

## Summary

- We can propagate landmark sets over action applications.
- Landmark orderings can be useful for detecting when a landmark that has already been achieved should be further considered.
- We can combine the landmark information from several paths to the same state.
- The LM-count heuristic counts how many landmarks still need to be satisfied.
- The LM-count heuristic is inadmissible (but there is an admissible variant).