

C2. Progression and Regression Search Introduction and Regression Search Introduction and Regression Search Introduction

C2.1 Introduction

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Search Direction

 \triangleright init() \rightsquigarrow returns initial state \triangleright is goal(s) \rightsquigarrow tests if s is a goal state

 \triangleright cost(a) \rightsquigarrow returns cost of action a

Planning by Forward Search: Progression

with respect to an operator o.

▶ start from initial state

Reminder: Interface for Heuristic Search Algorithms

Abstract Interface Needed for Heuristic Search Algorithms

▶ succ(s) \rightarrow returns all pairs $\langle a, s' \rangle$ with $s \stackrel{a}{\rightarrow} s'$

 \triangleright h(s) \rightsquigarrow returns heuristic value for state s

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C2. Progression and Regression Search Progression

Progression: Computing the successor state s of a state s

▶ iteratively pick a previously generated state and progress it

Progression planners find solutions by forward search:

through an operator, generating a new state ▶ solution found when a goal state generated

pro: very easy and efficient to implement

Search direction

- \triangleright one dimension for classifying search algorithms
- ▶ forward search from initial state to goal based on progression
- ▶ backward search from goal to initial state based on regression
- \blacktriangleright bidirectional search

In this chapter we look into progression and regression planning.

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Forward Search vs. Backward Search

Searching planning tasks in forward vs. backward direction is not symmetric:

- \triangleright forward search starts from a single initial state; backward search starts from a set of goal states
- \blacktriangleright when applying an operator o in a state s in forward direction, there is a unique successor state s' ;

if we just applied operator o and ended up in state s' , there can be several possible predecessor states s

 \rightarrow in most natural representation for backward search in planning, each search state corresponds to a set of world states

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C2. Progression and Regression Search Regression Search Regression C2. Progression Regression Regression Planning Example (Depth-first Search) $\varphi_1 = \text{regr}(\gamma, \longrightarrow) \qquad \varphi_3 \longrightarrow \varphi_2 \longrightarrow \varphi_1 \longrightarrow \gamma$ $\varphi_2 = \mathit{regr}(\varphi_1, {\longrightarrow})$ $\varphi_3 = \mathit{regr}(\varphi_2, \longrightarrow), I \models \varphi_3$ \bigcirc M. Helmert, G. Röger (Universität Basel) Planning and Optimization Cortober 9, 2024 26 / 32

Regression for STRIPS Planning Tasks

c2. Progression and Regression Search Regression for STRIPS Tasks

Regression for STRIPS planning tasks is much simpler than the general case:

- ▶ Consider subgoal φ that is conjunction of atoms $a_1 \wedge \cdots \wedge a_n$ (e.g., the original goal γ of the planning task).
- First step: Choose an operator o that deletes no a_i .
- ▶ Second step: Remove any atoms added by o from φ .
- \blacktriangleright Third step: Conjoin pre(o) to φ .
- \rightarrow Outcome of this is regression of φ w.r.t. o. It is again a conjunction of atoms.

optimization: only consider operators adding at least one a_i

STRIPS Regression

Definition (STRIPS Regression) Let $\varphi = \varphi_1 \wedge \cdots \wedge \varphi_n$ be a conjunction of atoms, and let o be a STRIPS operator which adds the atoms a_1, \ldots, a_k and deletes the atoms d_1, \ldots, d_l . The STRIPS regression of φ with respect to φ is

 $\mathit{sregr}(\varphi,o) := \begin{cases} \bot & \text{if } \varphi_i = d_j \text{ for some } i,j \end{cases}$ $\mathsf{pre}(o) \land \bigwedge (\{\varphi_1, \ldots, \varphi_n\} \setminus \{ \pmb{a}_1, \ldots, \pmb{a}_k \})$ else

C2. Progression and Regression Search Summary Summary Summary Summary Summary Summary Summary Summary Summary

Note: sregr(φ , o) is again a conjunction of atoms, or \perp .

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Does this Capture the Idea of Regression?

For our definition to capture the concept of regression, it must have the following property:

Regression Property

For all sets of states described by a conjunction of atoms φ , all states s and all STRIPS operators o,

 $s \models \text{sregr}(\varphi, o)$ iff $s[\![o]\!] \models \varphi$.

This is indeed true. We do not prove it now because we prove this property for general regression (not just STRIPS) later.

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