Planning and Optimization B2. Introduction to Planning Tasks

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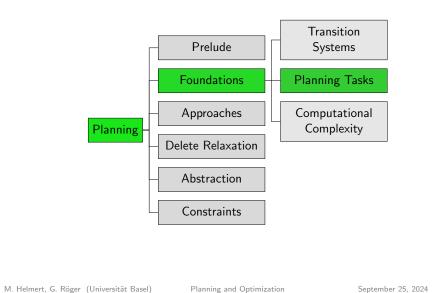
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Content of the Course



B2. Introduction to Planning Tasks

Introduction

B2.1 Introduction

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B2. Introduction to Planning Tasks

Introduction

The State Explosion Problem

- We saw in blocks world:
 n blocks → number of states exponential in n
- ► same is true everywhere we look
- known as the state explosion problem

To represent transitions systems compactly, need to tame these exponentially growing aspects:

- states
- goal states
- transitions

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Compact Descriptions of Transition Systems

How to specify huge transition systems without enumerating the states?

- represent different aspects of the world in terms of different (propositional) state variables
- ▶ individual state variables are atomic propositions→ a state is an interpretation of state variables
- n state variables induce 2ⁿ states
 → exponentially more compact than "flat" representations

Example: n^2 variables suffice for blocks world with n blocks

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State Variables

B2.2 State Variables

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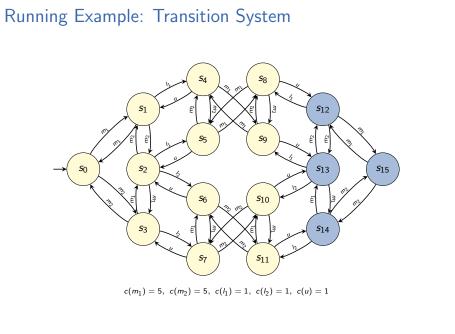
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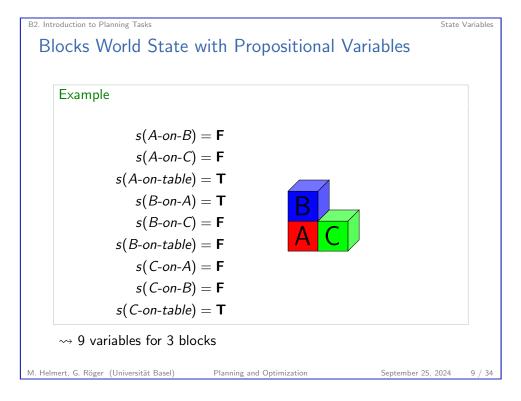
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State Variables



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Definition (Propositional State Variable)
A propositional state variable is a symbol X.
Let V be a finite set of propositional state variables.
A state s over V is an interpretation of V, i.e., a truth assignment $s:V\to \{\mathbf{T},\mathbf{F}\}$.

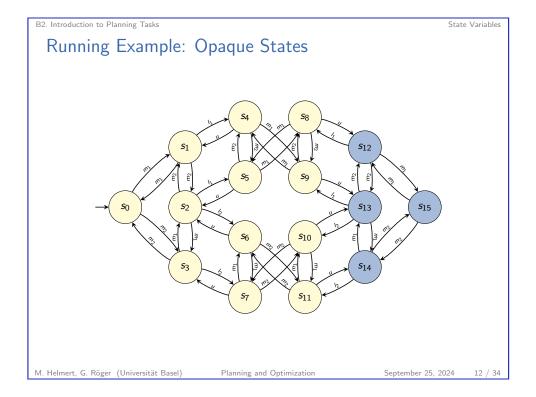
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Propositional State Variables

▶ In the running example, we describe 16 states with 4 propositional state variables (2⁴ = 16).

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B2.3 State Formulas

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State Variables

Running Example: Intuition

Intuition: delivery task with 2 trucks, 1 package, locations *L* and *R* transition labels:

- $ightharpoonup m_1/m_2$: move first/second truck
- I_1/I_2 : load package into first/second truck
- ▶ u: unload package from a truck

state variables:

- $ightharpoonup t_1$ true if first truck is at location L (else at R)
- $ightharpoonup t_2$ true if second truck is at location L (else at R)
- i true if package is inside a truck
- w encodes where exactly the package is:
 - if *i* is true, *w* true if package in first truck
 - if i is false, w true if package at location L

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State Formulas

Representing Sets of States

How do we compactly represent sets of states, for example the set of goal states?

Idea: formula φ over the state variables represents the models of φ .

Definition (State Formula)

Let ${\it V}$ be a finite set of propositional state variables.

A formula over V is a propositional logic formula using V as the set of atomic propositions.

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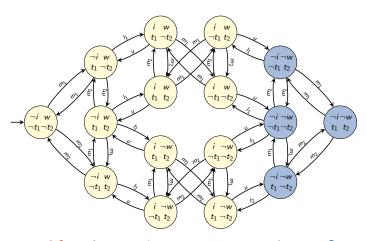
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Running Example: Representing Goal States



goal formula $\gamma = \neg i \land \neg w$ represents goal states S_{\star}

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Operators and Effects

B2.4 Operators and Effects

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Operators and Effects

Operators Representing Transitions

How do we compactly represent transitions?

- most complex aspect of a planning task
- central concept: operators

Idea: one operator o for each transition label ℓ , describing

▶ in which states s a transition $s \xrightarrow{\ell} s'$ exists (precondition)

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- ▶ how state s' differs from state s (effect)
- ightharpoonup what the cost of ℓ is

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Operators and Effects

Syntax of Operators

Definition (Operator)

An operator o over state variables V is an object with three properties:

- ightharpoonup a precondition pre(o), a formula over V
- ▶ an effect eff(o) over V, defined later in this chapter
- ightharpoonup a cost $cost(o) \in \mathbb{R}_0^+$

Notes:

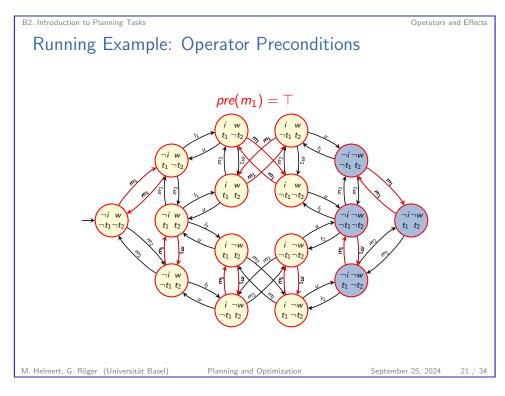
- ► Operators are also called actions.
- ▶ Operators are often written as triples $\langle pre(o), eff(o), cost(o) \rangle$.
- This can be abbreviated to pairs $\langle pre(o), eff(o) \rangle$ when the cost of the operator is irrelevant.

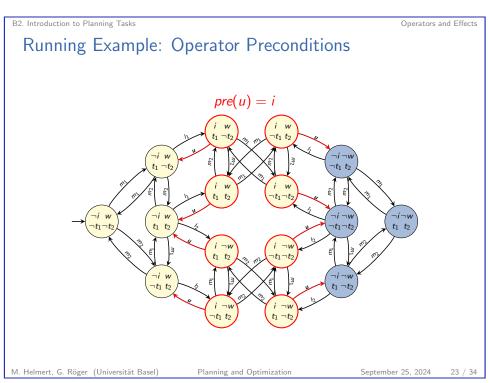
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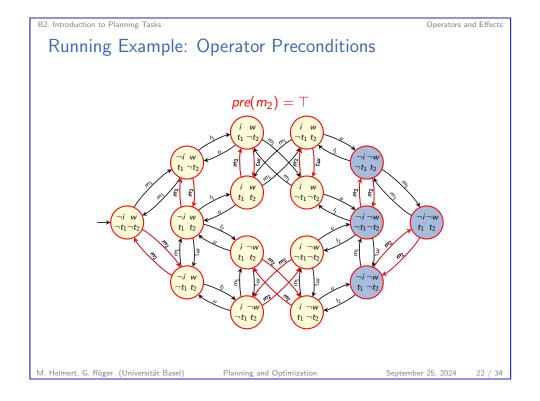
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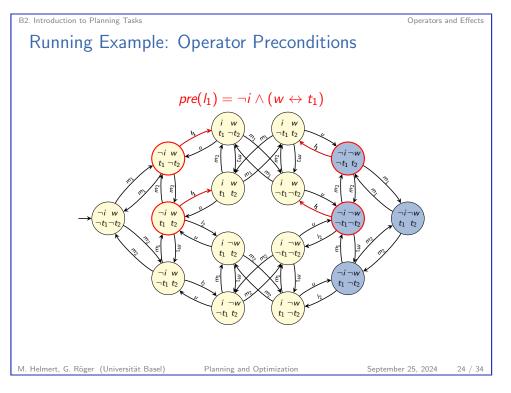
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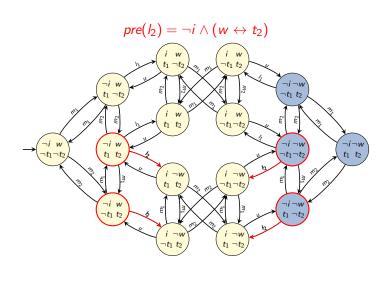








Running Example: Operator Preconditions



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Effects: Intuition

Intuition for effects:

- ► The empty effect T changes nothing.
- ► Atomic effects can be understood as assignments that update the value of a state variable.
 - \triangleright v means "v := \mathbf{T} "
 - $ightharpoonup \neg v \text{ means "} v := \mathbf{F}$ "
- A conjunctive effect $e = (e' \wedge e'')$ means that both subeffects e and e' take place simultaneously.
- A conditional effect $e = (\chi \triangleright e')$ means that subeffect e'takes place iff χ is true in the state where e takes place.

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Syntax of Effects

Definition (Effect)

Effects over propositional state variables Vare inductively defined as follows:

- ► ⊤ is an effect (empty effect).
- ▶ If $v \in V$ is a propositional state variable. then v and $\neg v$ are effects (atomic effect).
- ▶ If e and e' are effects, then $(e \land e')$ is an effect (conjunctive effect).
- ▶ If χ is a formula over V and e is an effect, then $(\chi \triangleright e)$ is an effect (conditional effect).

We may omit parentheses when this does not cause ambiguity.

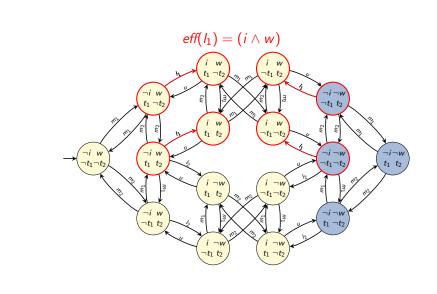
Example: we will later see that $((e \land e') \land e'')$ behaves identically to $(e \wedge (e' \wedge e''))$ and will write this as $e \wedge e' \wedge e''$.

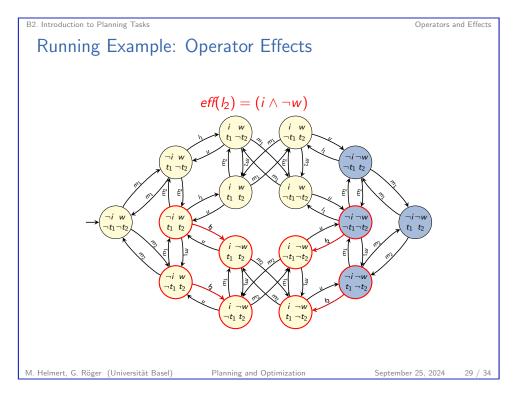
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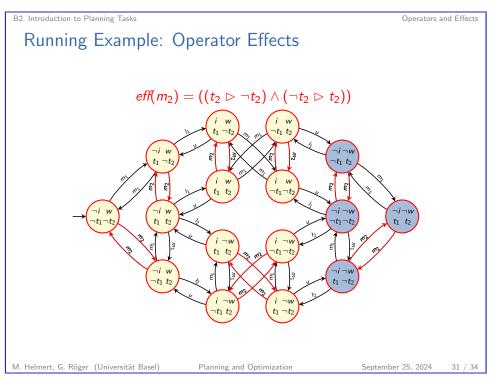
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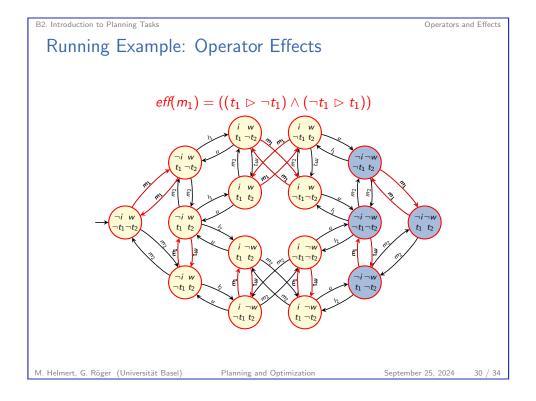
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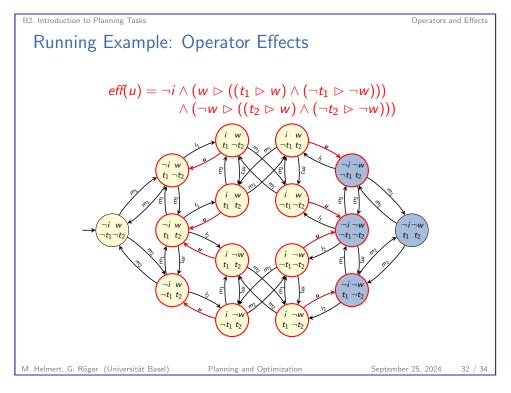
B2. Introduction to Planning Tasks Running Example: Operator Effects











B2. Introduction to Planning Tasks Summar

B2.5 Summary

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Summary

- ▶ Propositional state variables let us compactly describe properties of large transition systems.
- A state is an assignment to a set of state variables.
- ► Sets of states are represented as formulas over state variables.
- ▶ Operators describe when (precondition), how (effect) and at which cost the state of the world can be changed.
- ► Effects are structured objects including empty, atomic, conjunctive and conditional effects.

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