Planning and Optimization

C2. Progression and Regression Search

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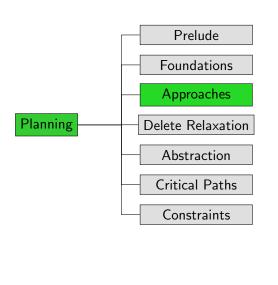
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Introduction

C2.1 Introduction

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C2. Progression and Regression Search

Search Direction

Search direction

- one dimension for classifying search algorithms
- ▶ forward search from initial state to goal based on progression
- backward search from goal to initial state based on regression
- bidirectional search

In this chapter we look into progression and regression planning.

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Progression

C2.2 Progression

Reminder: Interface for Heuristic Search Algorithms

Abstract Interface Needed for Heuristic Search Algorithms

► init()

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→ returns initial state

▶ is_goal(s)

 \rightsquigarrow tests if s is a goal state

 \triangleright succ(s)

 \rightsquigarrow returns all pairs $\langle a, s' \rangle$ with $s \stackrel{a}{\rightarrow} s'$

► cost(a)

 \rightarrow returns cost of action a

► h(s)

 \rightsquigarrow returns heuristic value for state s

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Planning by Forward Search: Progression

Progression: Computing the successor state s[o] of a state swith respect to an operator o.

Progression planners find solutions by forward search:

- start from initial state
- iteratively pick a previously generated state and progress it through an operator, generating a new state
- solution found when a goal state generated

pro: very easy and efficient to implement

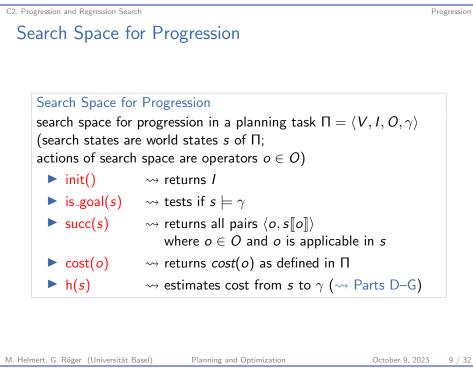
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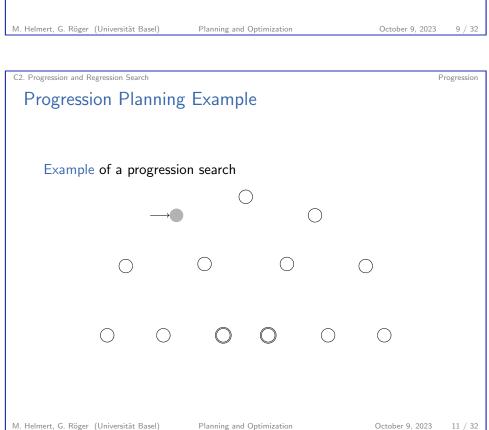
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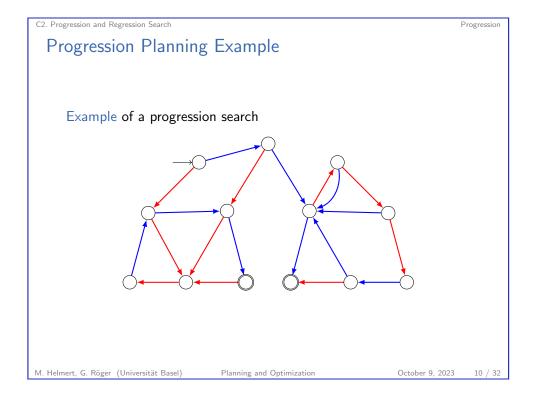
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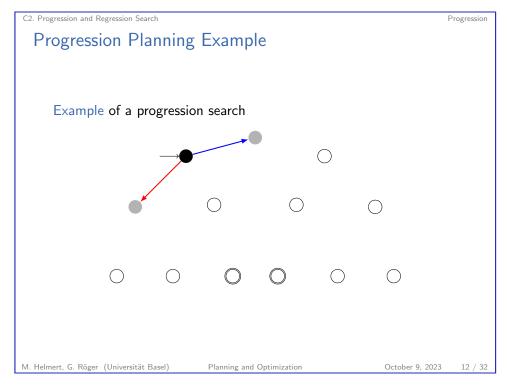
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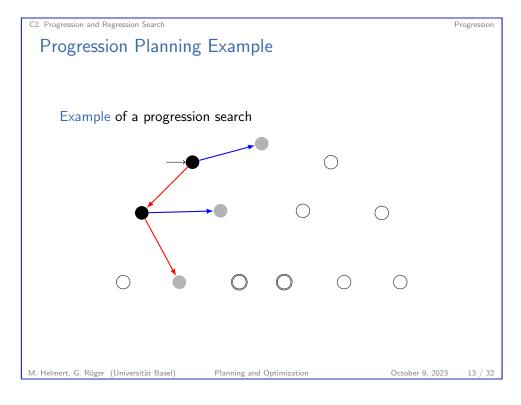
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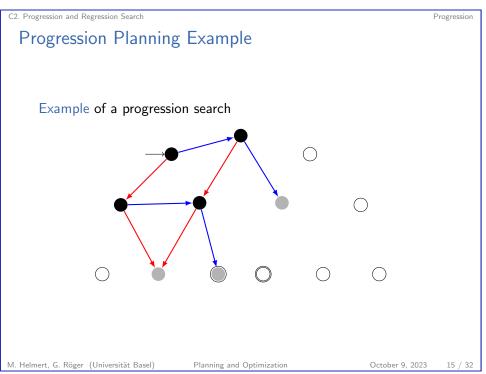


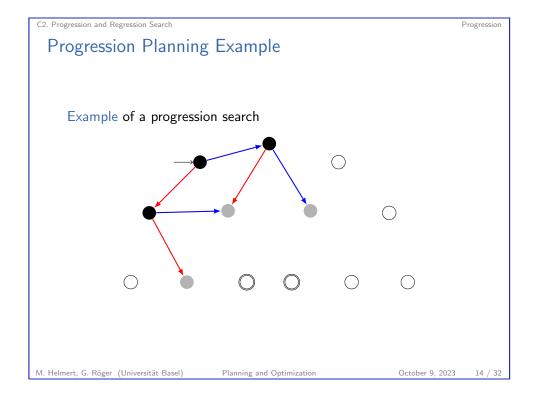


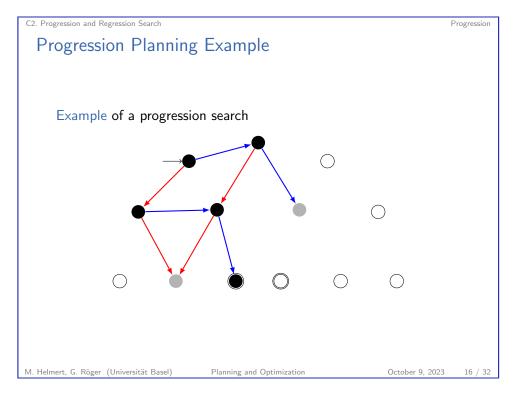












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C2.3 Regression

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Forward Search vs. Backward Search

Searching planning tasks in forward vs. backward direction is not symmetric:

- forward search starts from a single initial state; backward search starts from a set of goal states
- when applying an operator o in a state s in forward direction, there is a unique successor state s': if we just applied operator o and ended up in state s', there can be several possible predecessor states s
- → in most natural representation for backward search in planning, each search state corresponds to a set of world states

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Planning by Backward Search: Regression

Regression: Computing the possible predecessor states regr(S', o)of a set of states S' ("subgoal") given the last operator othat was applied.

→ formal definition in next chapter

Regression planners find solutions by backward search:

- start from set of goal states
- iteratively pick a previously generated subgoal (state set) and regress it through an operator, generating a new subgoal
- solution found when a generated subgoal includes initial state

pro: can handle many states simultaneously

con: basic operations complicated and expensive

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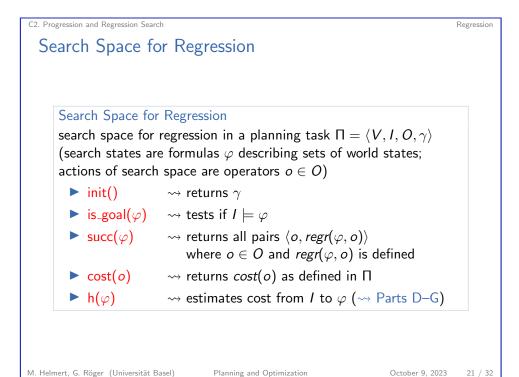
Search Space Representation in Regression Planners

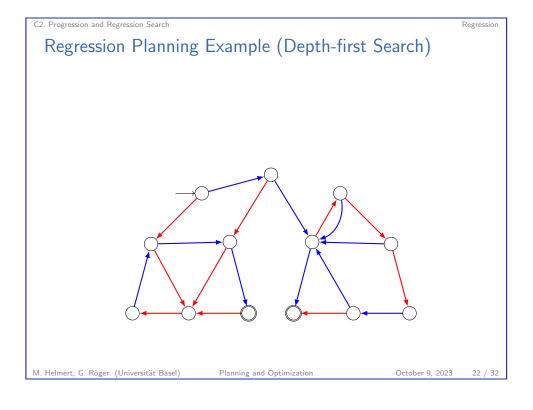
identify state sets with logical formulas (again):

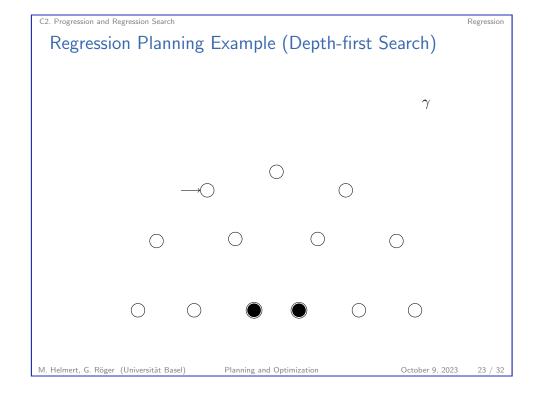
- each search state corresponds to a set of world states ("subgoal")
- each search state is represented by a logical formula: φ represents $\{s \in S \mid s \models \varphi\}$
- many basic search operations like detecting duplicates are NP-complete or coNP-complete

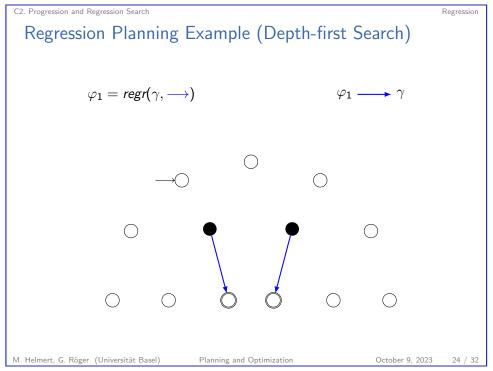
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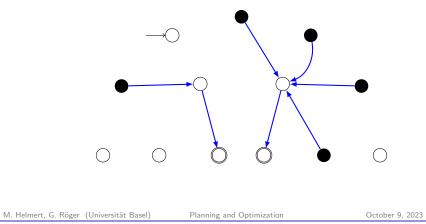


Regression Planning Example (Depth-first Search)

$$\varphi_1 = regr(\gamma, \longrightarrow)$$

$$\varphi_2 = regr(\varphi_1, \longrightarrow)$$

$$\varphi_2 \longrightarrow \varphi_1 \longrightarrow \gamma$$



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Regression for STRIPS Tasks

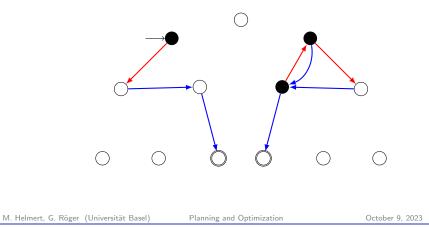
C2.4 Regression for STRIPS Tasks

Regression Planning Example (Depth-first Search)

$$\varphi_{1} = regr(\gamma, \longrightarrow) \qquad \varphi_{3} \longrightarrow \varphi_{2} \longrightarrow \varphi_{1} \longrightarrow \gamma$$

$$\varphi_{2} = regr(\varphi_{1}, \longrightarrow)$$

$$\varphi_{3} = regr(\varphi_{2}, \longrightarrow), I \models \varphi_{3}$$



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Regression for STRIPS Tasks

Regression for STRIPS Planning Tasks

Regression for STRIPS planning tasks is much simpler than the general case:

- \triangleright Consider subgoal φ that is conjunction of atoms $a_1 \wedge \cdots \wedge a_n$ (e.g., the original goal γ of the planning task).
- First step: Choose an operator o that deletes no a_i.
- **Second step**: Remove any atoms added by o from φ .
- ▶ Third step: Conjoin pre(o) to φ .
- \sim Outcome of this is regression of φ w.r.t. o. It is again a conjunction of atoms.

optimization: only consider operators adding at least one ai

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Regression for STRIPS Tasks

STRIPS Regression

Definition (STRIPS Regression)

Let $\varphi = \varphi_1 \wedge \cdots \wedge \varphi_n$ be a conjunction of atoms, and let o be a STRIPS operator which adds the atoms a_1, \ldots, a_k and deletes the atoms d_1, \ldots, d_l .

The STRIPS regression of φ with respect to o is

$$\mathit{sregr}(arphi, o) := egin{cases} \bot & \mathsf{if} \ arphi_i = d_j \ \mathsf{for} \ \mathsf{some} \ i, j \ pre(o) \land \bigwedge(\{arphi_1, \ldots, arphi_n\} \setminus \{a_1, \ldots, a_k\}) \ & \mathsf{else} \end{cases}$$

Note: $sregr(\varphi, o)$ is again a conjunction of atoms, or \bot .

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Regression for STRIPS Tasks

Does this Capture the Idea of Regression?

For our definition to capture the concept of regression, it must have the following property:

Regression Property

For all sets of states described by a conjunction of atoms φ , all states s and all STRIPS operators o,

$$s \models sregr(\varphi, o)$$
 iff $s[o] \models \varphi$.

This is indeed true. We do not prove it now because we prove this property for general regression (not just STRIPS) later.

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C2.5 Summary

C2. Progression and Regression Search

Summary

- ▶ Progression search proceeds forward from the initial state.
- In progression search, the search space is identical to the state space of the planning task.
- ▶ Regression search proceeds backwards from the goal.
- Each search state corresponds to a set of world states, for example represented by a formula.
- ► Regression is simple for STRIPS operators.
- ▶ The theory for general regression is more complex. This is the topic of the following chapter.

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