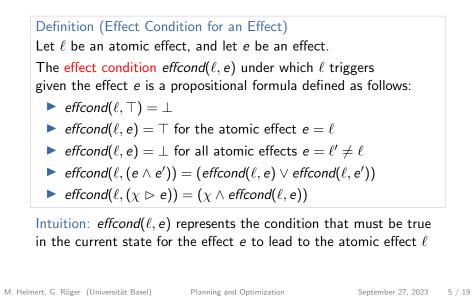


B3.1 Semantics of Effects and Operators

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Semantics of Effects: Effect Conditions



B3. Formal Definition of Planning

Semantics of Effects and Operators

Effect Condition: Example (2)

Example Consider the move operator m_1 from the running example: $eff(m_1) = ((t_1 \rhd \neg t_1) \land (\neg t_1 \rhd t_1)).$ Under which conditions does it set i to true? $effcond(i, eff(m_1)) = effcond(i, ((t_1 \rhd \neg t_1) \land (\neg t_1 \rhd t_1)))$ $= effcond(i, (t_1 \rhd \neg t_1)) \lor$ $effcond(i, (\neg t_1 \rhd t_1))$ $= (t_1 \land effcond(i, \neg t_1)) \lor$ $(\neg t_1 \land effcond(i, t_1))$ $= (t_1 \land \bot) \lor (\neg t_1 \land \bot)$ $\equiv \bot \lor \bot$

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B3. Formal Definition of Planning

Semantics of Effects and Operators

Effect Condition: Example (1)

Example

M. Helme

B3.

Consider the move operator m_1 from the running example: $eff(m_1) = ((t_1 \rhd \neg t_1) \land (\neg t_1 \rhd t_1)).$ Under which conditions does it set t_1 to false?

$$effcond(\neg t_{1}, eff(m_{1})) = effcond(\neg t_{1}, ((t_{1} \rhd \neg t_{1}) \land (\neg t_{1} \rhd t_{1})))$$

$$= effcond(\neg t_{1}, (t_{1} \rhd \neg t_{1})) \lor$$

$$effcond(\neg t_{1}, (\neg t_{1} \rhd t_{1}))$$

$$= (t_{1} \land effcond(\neg t_{1}, \neg t_{1})) \lor$$

$$(\neg t_{1} \land effcond(\neg t_{1}, t_{1}))$$

$$= (t_{1} \land \top) \lor (\neg t_{1} \land \bot)$$

$$\equiv t_{1} \lor \bot$$

$$\equiv t_{1}$$
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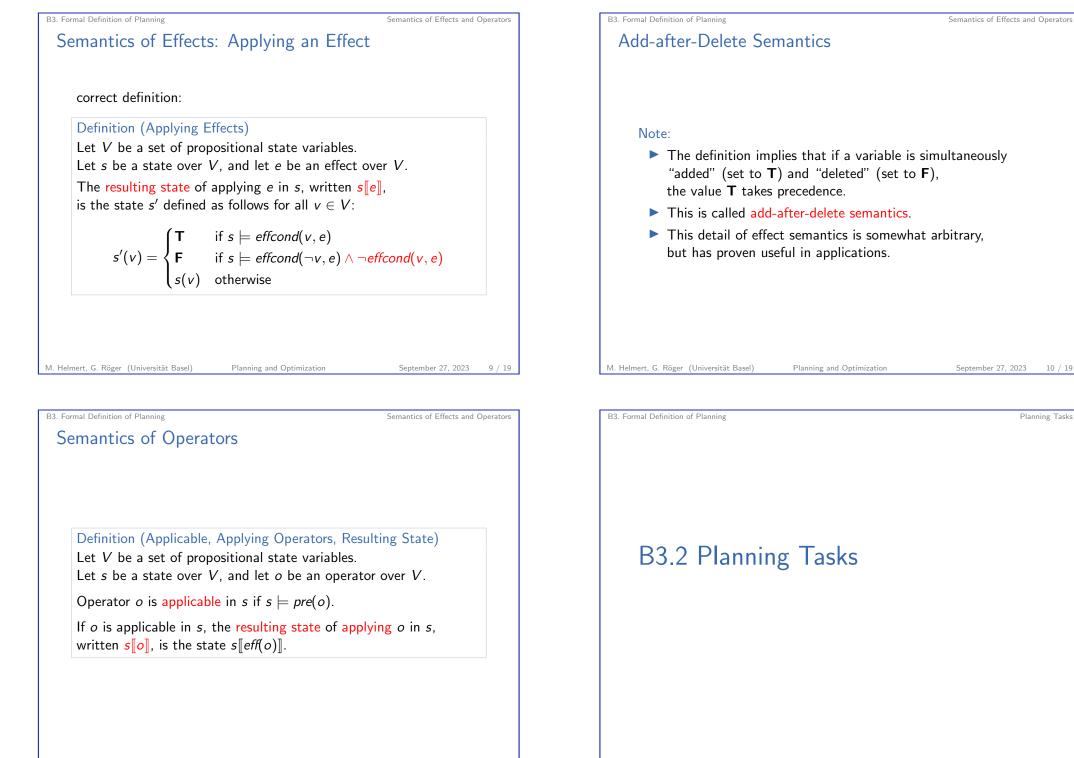
Semantics of Effects: Applying an EffectSemantics of Effects: Applying an EffectGemantics of Effects: Applying an Effectfirst attempt:Definition (Applying Effects)Let V be a set of propositional state variables.Let V be a set of propositional state variables.Let s be a state over V, and let e be an effect over V.The resulting state of applying e in s, written s[[e]],is the state s' defined as follows for all
$$v \in V$$
:s'(v) = $\begin{cases} T & \text{if } s \models effcond(v, e) \\ F & \text{if } s \models effcond(\neg v, e) \land \neg effcond(v, e) \\ s(v) & \text{otherwise} \end{cases}$ What is the problem with this definition?

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Planning and Optimization



Planning Tasks

Planning Tasks

Definition (Planning Task)

A (propositional) planning task is a 4-tuple $\Pi = \langle V, I, O, \gamma \rangle$ where

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- V is a finite set of propositional state variables,
- \blacktriangleright *I* is an interpretation of *V* called the initial state.
- \triangleright O is a finite set of operators over V, and
- \triangleright γ is a formula over V called the goal.

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B3. Formal Definition of Planning Planning Tasks Mapping Planning Tasks to Transition Systems Definition (Transition System Induced by a Planning Task) The planning task $\Pi = \langle V, I, O, \gamma \rangle$ induces the transition system $\mathcal{T}(\Pi) = \langle S, L, c, T, s_0, S_{\star} \rangle$, where \triangleright S is the set of all states over V. \blacktriangleright L is the set of operators O, \triangleright c(o) = cost(o) for all operators $o \in O$. $T = \{ \langle s, o, s' \rangle \mid s \in S, o \text{ applicable in } s, s' = s \llbracket o \rrbracket \},$ \blacktriangleright $s_0 = I$, and $\triangleright \ S_{\star} = \{ s \in S \mid s \models \gamma \}.$

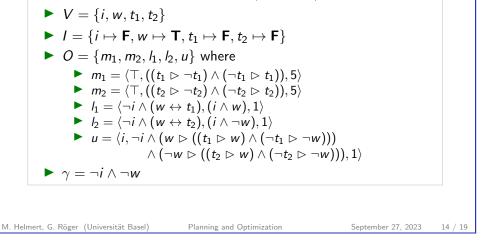
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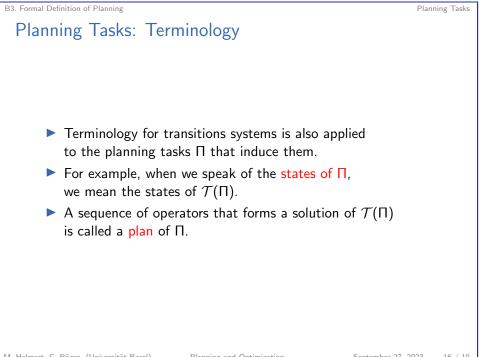
B3. Formal Definition of Planning

Running Example: Planning Task

Example

From the previous chapter, we see that the running example can be represented by the task $\Pi = \langle V, I, O, \gamma \rangle$ with





Planning Tasks

Satisficing and Optimal Planning

By planning, we mean the following two algorithmic problems:

Definition (Satisficing Planning)

Definition (Optimal Planning)

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B3. Formal Definition of Planning

Summary

- Planning tasks compactly represent transition systems and are suitable as inputs for planning algorithms.
- A planning task consists of a set of state variables and an initial state, operators and goal over these state variables.
- We gave formal definitions for these concepts.
- In satisficing planning, we must find a solution for a planning task (or show that no solution exists).
- In optimal planning, we must additionally guarantee that generated solutions are of minimal cost.

B3.3 Summary

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Summary

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