Planning and Optimization
B2. Introduction to Planning Tasks

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## B2.1 Introduction

- We saw in blocks world:
$n$ blocks $\rightsquigarrow$ number of states exponential in $n$
- same is true everywhere we look
- known as the state explosion problem

To represent transitions systems compactly, need to tame these exponentially growing aspects:

- states
- goal states
- transitions

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$c\left(m_{1}\right)=5, c\left(m_{2}\right)=5, c\left(l_{1}\right)=1, c\left(l_{2}\right)=1, c(u)=1$

How to specify huge transition systems without enumerating the states?

- represent different aspects of the world
in terms of different (propositional) state variables
- individual state variables are atomic propositions
$\rightsquigarrow$ a state is an interpretation of state variables
- $n$ state variables induce $2^{n}$ states
$\rightsquigarrow$ exponentially more compact than "flat" representations
Example: $n^{2}$ variables suffice for blocks world with $n$ blocks


## Example

$$
\begin{aligned}
s(A-o n-B) & =\mathbf{F} \\
s(A-o n-C) & =\mathbf{F} \\
s(A-o n-t a b l e) & =\mathbf{T} \\
s(B-o n-A) & =\mathbf{T} \\
s(B \text {-on- } C) & =\mathbf{F} \\
s(B-o n-t a b l e) & =\mathbf{F} \\
s(C-o n-A) & =\mathbf{F} \\
s(C \text {-on- } B) & =\mathbf{F} \\
s(C \text {-on-table }) & =\mathbf{T}
\end{aligned}
$$

$\rightsquigarrow 9$ variables for 3 blocks
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## Definition (Propositional State Variable)

A propositional state variable is a symbol $X$.
Let $V$ be a finite set of propositional state variables.
A state $s$ over $V$ is an interpretation of $V$, i.e.,
a truth assignment $s: V \rightarrow\{\mathbf{T}, \mathbf{F}\}$.
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- In the running example, we describe 16 states with 4 propositional state variables $\left(2^{4}=16\right)$.

State Variables
Running Example: Opaque States



Intuition: delivery task with 2 trucks, 1 package, locations $L$ and $R$ transition labels:

- $m_{1} / m_{2}$ : move first/second truck
$\rightarrow I_{1} / I_{2}$ : load package into first/second truck
- $u$ : unload package from a truck
state variables:
- $t_{1}$ true if first truck is at location $L$ (else at $R$ )
$\rightarrow t_{2}$ true if second truck is at location $L$ (else at $R$ )
$\rightarrow i$ true if package is inside a truck
- w encodes where exactly the package is:
- if $i$ is true, $w$ true if package in first truck
- if $i$ is false, $w$ true if package at location $L$
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## B2.4 Operators and Effects

How do we compactly represent transitions?
Definition (Operator)
An operator o over state variables $V$ is an object with three properties:

- a precondition pre(o), a formula over $V$
- an effect eff(o) over $V$, defined later in this chapter
- a cost $\operatorname{cost}(o) \in \mathbb{R}_{0}^{+}$

Idea: one operator $o$ for each transition label $\ell$, describing
Notes:

- Operators are also called actions.
- Operators are often written as triples $\langle\operatorname{pre}(o), \operatorname{eff}(o), \operatorname{cost}(o)\rangle$.
- This can be abbreviated to pairs $\langle$ pre(o), eff(o) $\rangle$ when the cost of the operator is irrelevant.


Running Example: Operator Preconditions

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Syntax of Effects

## Definition (Effect)

Effects over propositional state variables $V$ are inductively defined as follows:

- $T$ is an effect (empty effect).
- If $v \in V$ is a propositional state variable,
then $v$ and $\neg v$ are effects (atomic effect).
- If $e$ and $e^{\prime}$ are effects, then ( $e \wedge e^{\prime}$ ) is an effect (conjunctive effect).
- If $\chi$ is a formula over $V$ and $e$ is an effect, then $(\chi \triangleright e)$ is an effect (conditional effect).

We may omit parentheses when this does not cause ambiguity.
Example: we will later see that $\left(\left(e \wedge e^{\prime}\right) \wedge e^{\prime \prime}\right)$ behaves identically to $\left(e \wedge\left(e^{\prime} \wedge e^{\prime \prime}\right)\right)$ and will write this as $e \wedge e^{\prime} \wedge e^{\prime \prime}$.
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Running Example: Operator Effects

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## Running Example: Operator Effects

$$
\begin{aligned}
\operatorname{eff}(u)=\neg i & \wedge\left(w \triangleright\left(\left(t_{1} \triangleright w\right) \wedge\left(\neg t_{1} \triangleright \neg w\right)\right)\right) \\
& \wedge\left(\neg w \triangleright\left(\left(t_{2} \triangleright w\right) \wedge\left(\neg t_{2} \triangleright \neg w\right)\right)\right)
\end{aligned}
$$



## B2.5 Summary

- Propositional state variables let us compactly describe properties of large transition systems.
- A state is an assignment to a set of state variables.
- Sets of states are represented as formulas over state variables.
- Operators describe when (precondition), how (effect) and at which cost the state of the world can be changed.
- Effects are structured objects including empty, atomic, conjunctive and conditional effects.

