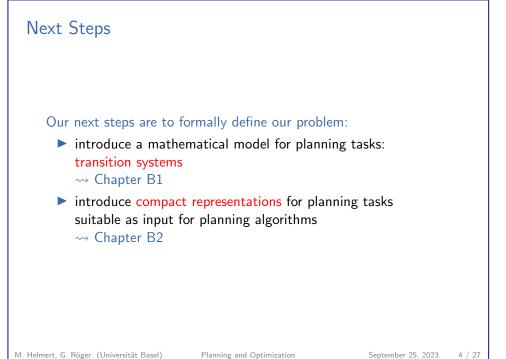


Planning and Optim September 25, 2023 — B1. Tr	ization ransition Systems and Proposition	nal Logic	
B1.1 Transition S	ystems		
B1.2 Example: B	locks World		
B1.3 Reminder: F	Propositional Logic		
B1.4 Summary			
M. Helmert, G. Röger (Universität Basel)	Planning and Optimization	September 25, 2023	2 / 27



5 / 27

7 / 27

Transition Systems

B1.1 Transition Systems

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B1. Transition Systems and Propositional Logic

Transition Systems

Definition (Transition System)

A transition system is a 6-tuple $\mathcal{T} = \langle S, L, c, T, s_0, S_{\star} \rangle$ where

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- ► *S* is a finite set of states,
- L is a finite set of (transition) labels,
- ▶ $c: L \to \mathbb{R}_0^+$ is a label cost function,
- $T \subseteq S \times L \times S$ is the transition relation,
- $s_0 \in S$ is the initial state, and
- $S_{\star} \subseteq S$ is the set of goal states.

We say that \mathcal{T} has the transition $\langle s, \ell, s' \rangle$ if $\langle s, \ell, s' \rangle \in \mathcal{T}$.

We also write this as $s \xrightarrow{\ell} s'$, or $s \rightarrow s'$ when not interested in ℓ .

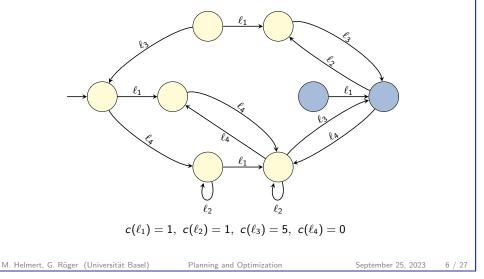
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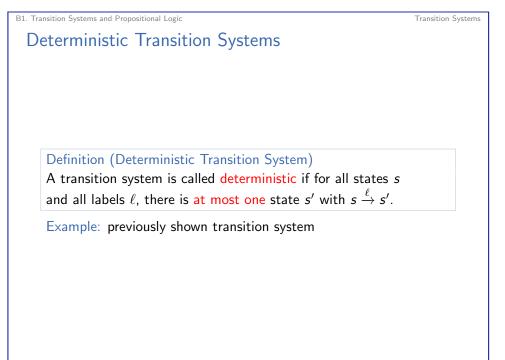
Note: Transition systems are also called state spaces.

B1. Transition Systems and Propositional Logic

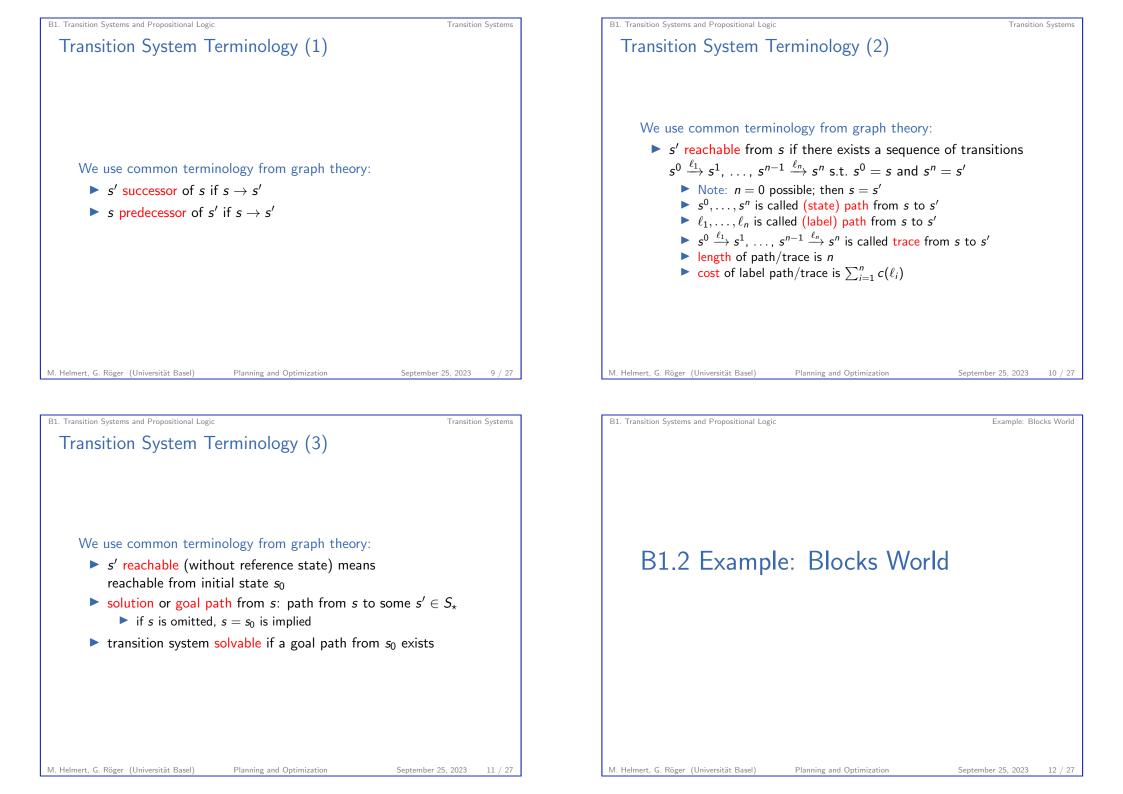
Transition System Example

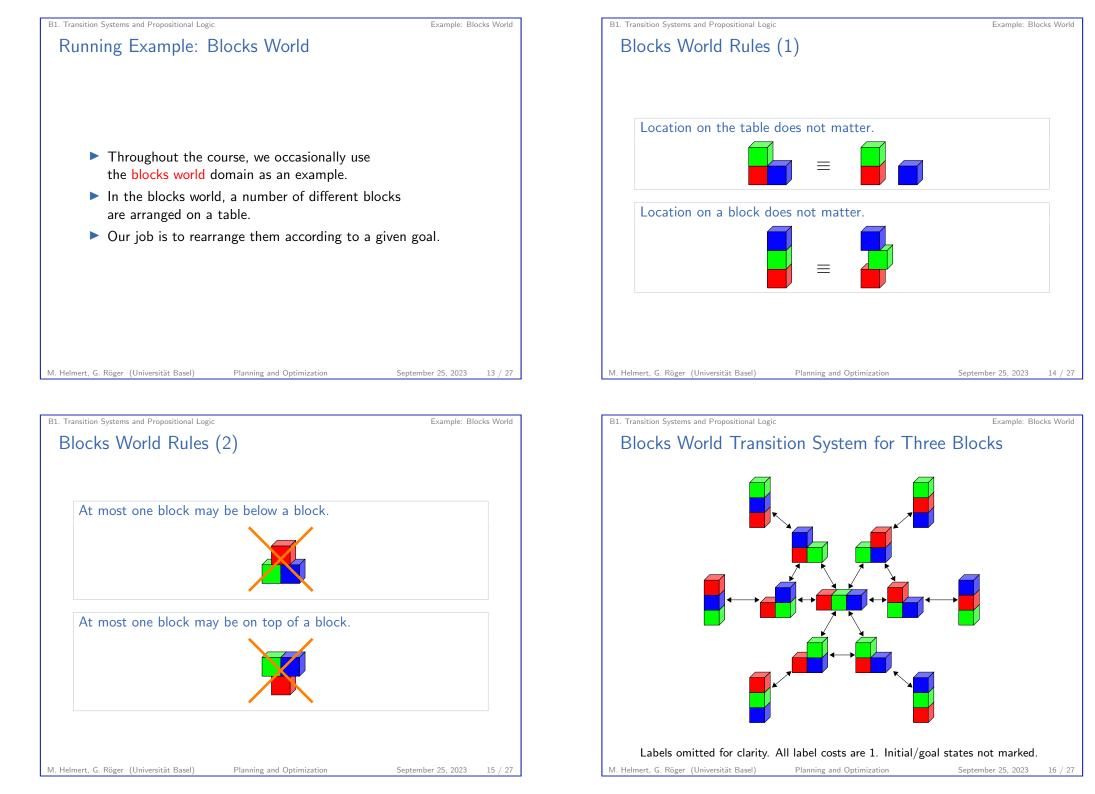
Transition systems are often depicted as directed arc-labeled graphs with decorations to indicate the initial state and goal states.





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B1. Transition Systems and	Propositional Logic
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Blocks World Computational Properties

blocks	states	blocks	states
1	1	10	58941091
2	3	11	824073141
3	13	12	12470162233
4	73	13	202976401213
5	501	14	3535017524403
6	4051	15	65573803186921
7	37633	16	1290434218669921
8	394353	17	26846616451246353
9	4596553	18	588633468315403843

Finding solutions is possible in linear time in the number of blocks: move everything onto the table, then construct the goal configuration.

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Finding a shortest solution is NP-complete given a compact description of the problem.

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September 25, 2023 17 / 27

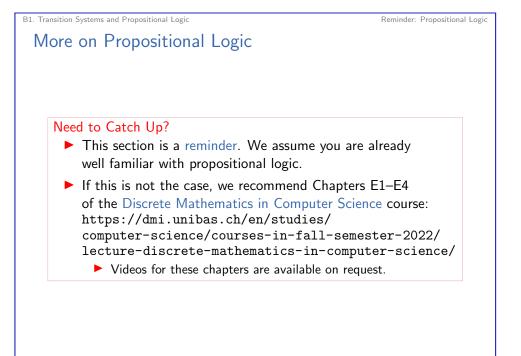
B1. Transition Systems and Propositional Logic

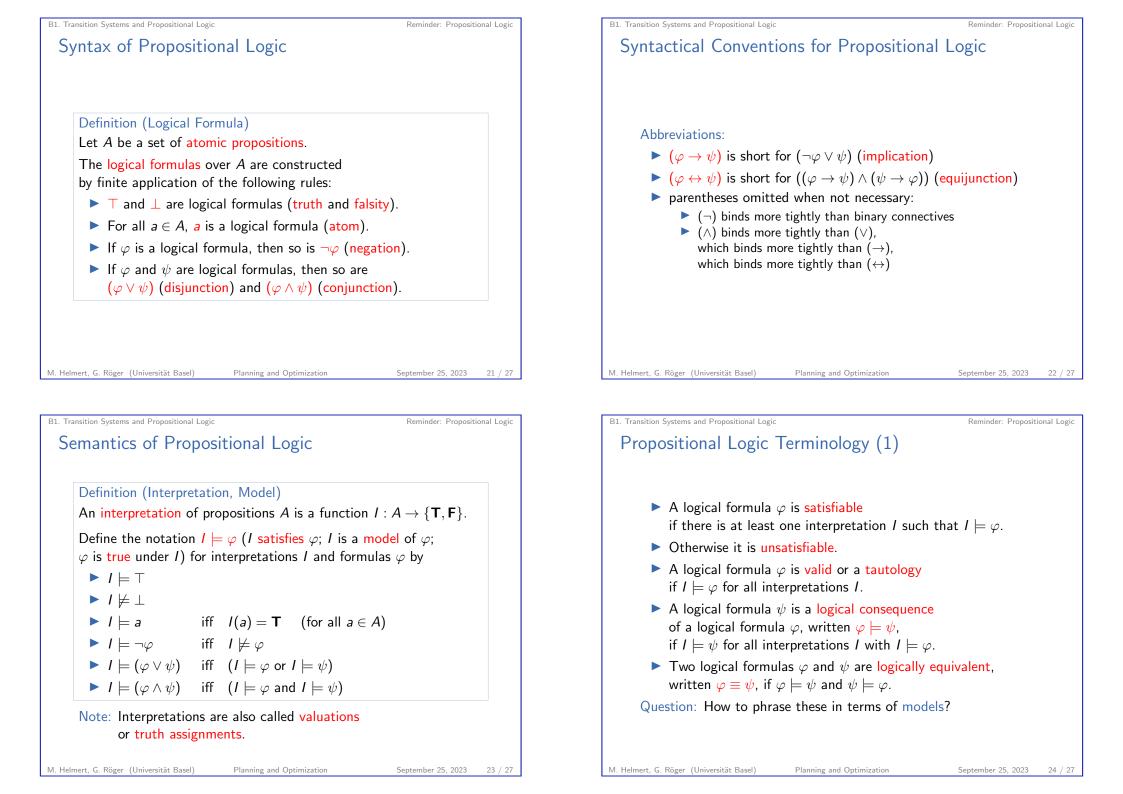
Reminder: Propositional Logic

Example: Blocks World

B1.3 Reminder: Propositional Logic

B1. Transition Systems and Propositional Lo	gic	Example: Blo	cks Wo
The Need for Com	pact Descriptions		
	e blocks world example tha	,	5
	large to be directly used	as inputs	
to planning algo		c	
	ed compact descriptions of	-	•
	, we will use propositional		
	pressing information about las over <i>n</i> state variables.	2" states	
as logical formu	las over <i>Il state vallables</i> .		





Reminder: Propositional Logic

September 25, 2023

25 / 27

Summarv

Propositional Logic Terminology (2)

- A logical formula that is a proposition *a* or a negated proposition ¬*a* for some atomic proposition *a* ∈ *A* is a literal.
- A formula that is a disjunction of literals is a clause. This includes unit clauses ℓ consisting of a single literal and the empty clause ⊥ consisting of zero literals.
- A formula that is a conjunction of literals is a monomial. This includes unit monomials ℓ consisting of a single literal and the empty monomial ⊤ consisting of zero literals.

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Normal forms:

- negation normal form (NNF)
- conjunctive normal form (CNF)
- disjunctive normal form (DNF)

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B1. Transition Systems and Propositional Logic

Summary

- Transition systems are (typically huge) directed graphs that encode how the state of the world can change.
- Propositional logic allows us to compactly describe complex information about large sets of interpretations as logical formulas.

B1.4	Summar	у		
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Summarv

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Planning and Optimization

September 25, 2023 27 / 27