







G12. Potential Heuristics

Reminder: Transition Normal Form

In this chapter, we consider SAS^+ tasks in transition normal form.

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- ► A TNF operator mentions the same variables in the precondition and in the effect.
- ► A TNF goal specifies a value for every variable.

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G12. Potential Heuristics Introduction Idea **•** Define simple numerical state features f_1, \ldots, f_n . Consider heuristics that are linear combinations of features: $h(s) = w_1 f_1(s) + \cdots + w_n f_n(s)$ with weights (potentials) $w_i \in \mathbb{R}$ heuristic very fast to compute if feature values are Planning and Optimization

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Introduction

5 / 20

Material Value of a Chess Position

G12. Potential Heuristics



G12. Potential Heuristics Potential Heuristics G12.2 Potential Heuristics

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Definition

Definition (Feature)

A (state) feature for a planning task is a numerical function defined on the states of the task: $f: S \to \mathbb{R}$.

Definition (Potential Heuristic)

A potential heuristic for a set of features $\mathcal{F} = \{f_1, \ldots, f_n\}$ is a heuristic function h defined as a linear combination of the features:

$$h(s) = w_1 f_1(s) + \cdots + w_n f_n(s)$$

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with weights (potentials) $w_i \in \mathbb{R}$.

Many possibilities \Rightarrow need some restrictions

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9 / 20

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Example: Atomic Features

Example

Consider a planning task Π with state variables v_1 and v_2 and dom (v_1) = dom (v_2) = { d_1, d_2, d_3 }. The set

 $\mathcal{F} = \{ f_{v_i=d_i} \mid i \in \{1, 2\}, j \in \{1, 2, 3\} \}$

is the set of atomic features of Π and the function

$$h(s) = 3f_{v_1=d_1} + 0.5f_{v_1=d_2} - 2f_{v_1=d_3} + 2.5f_{v_2=d_1}$$

is a potential heuristic for \mathcal{F} .

The heuristic estimate for a state $s = \{v_1 \mapsto d_2, v_2 \mapsto d_1\}$ is

 $h(s) = 3 \cdot 0 + 0.5 \cdot 1 - 2 \cdot 0 + 2.5 \cdot 1 = 3.$

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Features for SAS⁺ Planning Tasks

Which features are good for planning?

Atomic features test if some atom is true in a state:

Definition (Atomic Feature) Let v = d be an atom of a FDR planning task.

The atomic feature $f_{y=d}$ is defined as:

 $f_{v=d}(s) = [(v=d) \in s] = \begin{cases} 1 & \text{if variable } v \text{ has value } d \text{ in state } s \\ 0 & \text{otherwise} \end{cases}$

Offer good tradeoff between computation time and guidance

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Potential Heuristics

10 / 20



G12. Potential Heuristics Potential Heuristics Admissible and Consistent Potential Heuristics We achieve admissibility through goal-awareness and consistency Goal-awareness $\sum_{a \in a} w_a = 0$ Consistency $\sum_{a \in s} w_a - \sum_{a \in s'} w_a \leq cost(o) \quad \text{for all transitions } s \xrightarrow{o} s'$ One constraint transition per transition. Can we do this more compactly? M. Helmert, G. Röger (Universität Basel) Planning and Optimization December 14, 2022 13 / 20



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Admissible and Consistent Potential Heuristics





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Well-Informed Potential Heuristics

What do we mean by the best potential heuristic? Different possibilities, e.g., the potential heuristic that

- maximizes heuristic value of a given state s (e.g., initial state)
- maximizes average heuristic value of all states (including unreachable ones)
- maximizes average heuristic value of some sample states
- minimizes estimated search effort

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Summary

17 / 20

December 14, 2022

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Theorem

Potential and Flow Heuristic

Then $h^{\text{maxpot}}(s) = h^{flow}(s)$.

equals the flow heuristic.

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features

constraints

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Summary

For state s, let $h^{maxpot}(s)$ denote the maximal heuristic value

Proof idea: compare dual of $h^{flow}(s)$ LP to potential heuristic

If we optimize the potentials for a given state then for this state it

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Potential heuristics are computed as a weighted sum of state

Admissibility and consistency can be encoded compactly in

potential heuristic wrt some objective

approximations of h^{flow} .

Potential heuristics can be used as fast admissible

▶ With linear programming, we can efficiently compute the best

constraints optimized for state *s*.

of all admissible and consistent atomic potential heuristics in s.

G12.3 Summary

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18 / 20

Summar

20 / 20