Planning and Optimization G11. Operator Counting

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December 14, 2022

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G11. Operator Counting

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Introduction

Content of this Course Landmarks Cost Prelude Partitioning **Foundations** Post-Hoc Optimization Logic **Planning** Network Flows Heuristics Operator Constraints Counting Potential Heuristics M. Helmert, G. Röger (Universität Basel) Planning and Optimization December 14, 2022

G11.1 Introduction

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Reminder: Flow Heuristic

In the previous chapter, we used flow constraints to describe how often operators must be used in each plan.

Example (Flow Constraints)

Let Π be a planning problem with operators $\{o_{red}, o_{green}, o_{blue}\}$. The flow constraint for some atom a is the constraint

$$1 + Count_{O_{reen}} = Count_{O_{red}}$$
 if

- ► a is true in the initial state
- ► o_{green} produces a

► a is false in the goal

Ored consumes a

In natural language, the flow constraint expresses that

every plan uses o_{red} once more than o_{green} .

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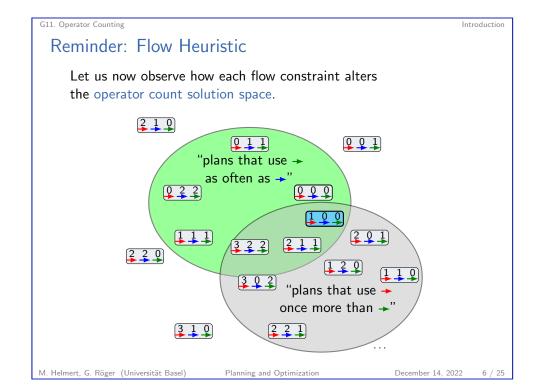
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Operator-counting Framework

G11.2 Operator-counting Framework



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Operator-counting Framework

Operator Counting

Operator counting

- peneralizes this idea to a framework that allows to admissibly combine different heuristics.
- uses linear constraints . . .
- ▶ ... that describe number of occurrences of an operator ...
- ▶ ... and must be satisfied by every plan.
- provides declarative way to describe knowledge about solutions.
- allows reasoning about solutions to derive heuristic estimates.

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Operator-counting Framework

Operator-counting Constraint

Definition (Operator-counting Constraints)

Let Π be a planning task with operators O and let s be a state. Let \mathcal{V} be the set of integer variables Count_o for each $o \in O$.

A linear inequality over \mathcal{V} is called an operator-counting constraint for s if for every plan π for s setting each Count, to the number of occurrences of o in π is a feasible variable assignment.

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Operator-counting Framework

Operator-counting Heuristics

Definition (Operator-counting IP/LP Heuristic)

The operator-counting integer program IP_C for a set C of operator-counting constraints for state s is

Minimize
$$\sum_{o \in O} cost(o) \cdot Count_o$$
 subject to

C and Count_o > 0 for all $o \in O$.

where O is the set of operators.

The IP heuristic h_C^{IP} is the objective value of IP_C, the LP heuristic h_C^{LP} is the objective value of its LP-relaxation.

If the IP/LP is infeasible, the heuristic estimate is ∞ .

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Operator-counting Constraints

- ▶ Adding more constraints can only remove feasible solutions.
- Fewer feasible solutions can only increase the objective value.
- ▶ Higher objective value means better informed heuristic
- ⇒ Have we already seen other operator-counting constraints?

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Operator-counting Framework

Reminder: Minimum Hitting Set for Landmarks

Variables

Non-negative variable Applied, for each operator of

Objective

Minimize $\sum_{o} cost(o) \cdot Applied_{o}$

Subject to

 $\sum_{o \in L} \mathsf{Applied}_o \geq 1 \text{ for all landmarks } L$

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Operator Counting with Disjunctive Action Landmarks

Variables

Non-negative variable Count_o for each operator o

Objective

Minimize $\sum_{o} cost(o) \cdot Count_{o}$

Subject to

$$\sum_{o \in I} \mathsf{Count}_o \ge 1 \text{ for all landmarks } L$$

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Operator-counting Framework

Reminder: Post-hoc Optimization Heuristic

For set of abstractions $\{\alpha_1, \ldots, \alpha_n\}$:

Variables

Non-negative variables X_o for all operators $o \in O$ X_o is cost incurred by operator o

Objective

Minimize $\sum_{o \in O} X_o$

Subject to

$$\sum\nolimits_{o \in O: o \text{ relev. for } \alpha} {X_o \ge h^\alpha (s)} \quad \text{for } \alpha \in \{\alpha_1, \dots, \alpha_n\}$$

$$X_o \ge 0 \qquad \text{for all } o \in O$$

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Operator-counting Framework

Operator Counting with Post-hoc Optimization Constraints

For set of abstractions $\{\alpha_1, \ldots, \alpha_n\}$:

Variables

Non-negative variables $Count_o$ for all operators $o \in O$ $Count_o \cdot cost(o)$ is cost incurred by operator o

Objective

Minimize $\sum_{o \in O} cost(o) \cdot Count_o$

Subject to

$$\sum\nolimits_{o \in O:o \text{ relev. for } \alpha} cost(o) \cdot \mathsf{Count}_o \geq h^{\alpha}(s) \quad \text{for } \alpha \in \{\alpha_1, \dots, \alpha_n\}$$
$$cost(o) \cdot \mathsf{Count}_o \geq 0 \qquad \text{for all } o \in O$$

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G11. Operator Counting Operator-counting Framework Example $\frac{2}{1} \frac{1}{0}$ 1 1 2 0 0 0"plans that use → at least once' 121 0 0 1 1 3 1 100 2 2 0 1 2 0 "plans where → and → "plans that use cost 4 or more together once more than →" 3 1 0 M. Helmert, G. Röger (Universität Basel) December 14, 2022

Operator-counting Framework

Further Examples?

- ▶ The definition of operator-counting constraints can be extended to groups of constraints and auxiliary variables.
- ▶ With this extended definition we could also cover more heuristics, e.g., the perfect relaxation heuristic h^+

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G11.3 Properties

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Properties

Properties

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Admissibility

Theorem (Operator-counting Heuristics are Admissible)

The IP and the IP heuristic are admissible.

Proof.

Let C be a set of operator-counting constraints for state s and π be an optimal plan for s. The number of operator occurrences of π are a feasible solution for C. As the IP/LP minimizes the total plan cost, the objective value cannot exceed the cost of π and is therefore an admissible estimate.

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Dominance

Theorem

Let C and C' be sets of operator-counting constraints for s and let $C \subseteq C'$. Then $IP_C \le IP_{C'}$ and $LP_C \le LP_{C'}$.

Proof.

Every feasible solution of C' is also feasible for C. As the LP/IP is a minimization problem, the objective value subject to C can therefore not be larger than the one subject to C'.

Adding more constraints can only improve the heuristic estimate.

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Properties

Heuristic Combination

Operator counting as heuristic combination

- Multiple operator-counting heuristics can be combined by computing h_C^{LP}/h_C^{IP} for the union of their constraints.
- ► This is an admissible combination.
 - ▶ Never worse than maximum of individual heuristics
 - Sometimes even better than their sum
- ► We already know a way of admissibly combining heuristics: cost partitioning.
 - ⇒ How are they related?

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Properties

Connection to Cost Partitioning

Theorem

Let C_1, \ldots, C_n be sets of operator-counting constraints for s and $C = \bigcup_{i=1}^n C_i$. Then h_C^{LP} is the optimal general cost partitioning over the heuristics h_C^{LP} .

Proof Sketch.

In LP_C, add variables Count_o^i and $\mathsf{constraints}\ \mathsf{Count}_o = \mathsf{Count}_o^i$ for all operators o and $1 \le i \le n$. Then replace Count_o^i by Count_o^i in C_i .

Dualizing the resulting LP shows that h_C^{LP} computes a cost partitioning. Dualizing the component heuristics of that cost partitioning shows that they are h_C^{LP} .

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Properties

Comparison to Optimal Cost Partitioning

- some heuristics are more compact if expressed as operator counting
- ▶ some heuristics cannot be expressed as operator counting
- operator counting IP even better than optimal cost partitioning
- Cost partitioning maximizes, so heuristics must be encoded perfectly to guarantee admissibility.
 Operator counting minimizes, so missing information just makes the heuristic weaker.

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Summa

G11.4 Summary

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Summary

- ▶ Many heuristics can be formulated in terms of operator-counting constraints.
- ▶ The operator counting heuristic framework allows to combine the constraints and to reason on the entire encoded declarative knowledge.
- ► The heuristic estimate for the combined constraints can be better than the one of the best ingredient heuristic but never worse.
- ► Operator counting is equivalent to optimal general cost partitioning over individual constraints.

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