# Planning and Optimization

G5. Landmarks: Cut Landmarks & LM-Cut Heuristic

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G5.1 i-g Form

G5.2 Cut Landmarks

G5.3 The LM-Cut Heuristic

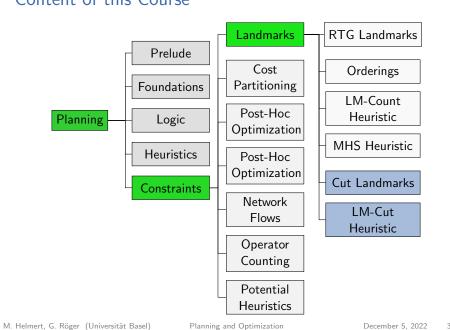
G5.4 Summary

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Content of this Course



# Roadmap for this Chapter

- ► We first introduce a new normal form for delete-free STRIPS tasks that simplifies later definitions.
- ► We then present a method that computes disjunctive action landmarks for such tasks.
- ► We conclude with the LM-cut heuristic that builds on this method.

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G5.1 i-g Form

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# Delete-Free STRIPS Planning Task in i-g Form (1)

In this chapter, we only consider delete-free STRIPS tasks in a special form:

### Definition (i-g Form for Delete-free STRIPS)

A delete-free STRIPS planning task  $\langle V, I, O, \gamma \rangle$  is in i-g form if

- ► V contains atoms i and g
- lnitially exactly i is true: I(v) = T iff v = i
- ightharpoonup g is the only goal atom:  $\gamma = \{g\}$
- ▶ Every action has at least one precondition.

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### Transformation to i-g Form

Every delete-free STRIPS task  $\Pi = \langle V, I, O, \gamma \rangle$  can easily be transformed into an analogous task in i-g form.

- $\triangleright$  If i or g are in V already, rename them everywhere.
- ightharpoonup Add i and g to V.
- Add an operator  $\langle \{i\}, \{v \in V \mid I(v) = \mathbf{T}\}, \{\}, 0 \rangle$ .
- Add an operator  $\langle \gamma, \{g\}, \{\}, 0 \rangle$ .
- ▶ Replace all operator preconditions  $\top$  with i.
- ► Replace initial state and goal.

For the remainder of this chapter, we assume tasks in i-g form.

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# Example: Delete-Free Planning Task in i-g Form

#### Example

Consider a delete-relaxed STRIPS planning  $\langle V, I, O, \gamma \rangle$  with  $V = \{i, a, b, c, d, g\}, I = \{i \mapsto T\} \cup \{v \mapsto F \mid v \in V \setminus \{i\}\}, \gamma = g$ and operators

- $ightharpoonup o_{\text{blue}} = \langle \{i\}, \{a, b\}, \{\}, 4 \rangle,$
- $ightharpoonup o_{green} = (\{i\}, \{a, c\}, \{\}, 5),$
- $ightharpoonup o_{black} = \langle \{i\}, \{b, c\}, \{\}, 3 \rangle,$
- $ightharpoonup o_{red} = (\{b, c\}, \{d\}, \{\}, 2), \text{ and}$
- ightharpoonup  $O_{\text{orange}} = \langle \{a,d\}, \{g\}, \{\}, 0 \rangle$ .

optimal solution to reach g from i:

- ▶ plan: ⟨o<sub>blue</sub>, o<sub>black</sub>, o<sub>red</sub>, o<sub>orange</sub>⟩
- ightharpoonup cost: 4+3+2+0=9 (=  $h^+(I)$  because plan is optimal)

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## G5.2 Cut Landmarks

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G5. Landmarks: Cut Landmarks & LM-Cut Heuristic Content of this Course Prelude RTG Landmarks Landmarks **Foundations** Cost Orderings Partitioning Planning Logic LM-Count Post-Hoc Heuristic Optimization Heuristics MHS Heuristic Network Constraints Flows Cut Landmarks Operator LM-Cut Counting Heuristic Potential Heuristics M. Helmert, G. Röger (Universität Basel) Planning and Optimization December 5, 2022

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Cut Landmarks

### Justification Graphs

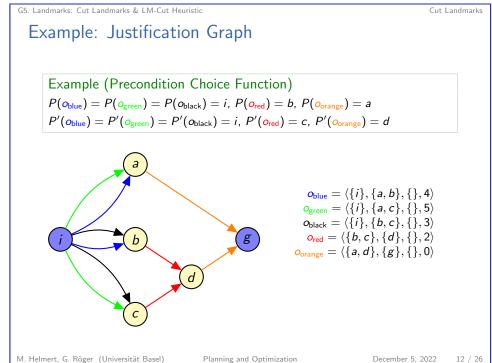
#### Definition (Precondition Choice Function)

A precondition choice function (pcf)  $P: O \rightarrow V$  for a delete-free STRIPS task  $\Pi = \langle V, I, O, \gamma \rangle$  in i-g form maps each operator to one of its preconditions (i.e.  $P(o) \in pre(o)$  for all  $o \in O$ ).

### Definition (Justification Graphs)

Let P be a pcf for  $\langle V, I, O, \gamma \rangle$  in i-g form. The justification graph for P is the directed, edge-labeled graph  $J = \langle V, E \rangle$ , where

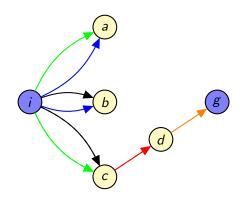
- $\triangleright$  the vertices are the variables from V, and
- ▶ E contains an edge  $P(o) \xrightarrow{o} a$  for each  $o \in O$ ,  $a \in add(o)$ .



### Cuts

### Definition (Cut)

A cut in a justification graph is a subset C of its edges such that all paths from i to g contain an edge from C.



 $o_{\text{blue}} = \langle \{i\}, \{a, b\}, \{\}, 4 \rangle$  $o_{green} = \langle \{i\}, \{a, c\}, \{\}, 5 \rangle$ 

 $o_{\mathsf{black}} = \langle \{i\}, \{b, c\}, \{\}, 3 \rangle$ 

 $o_{\text{red}} = \langle \{b, c\}, \{d\}, \{\}, 2 \rangle$ 

 $o_{\text{orange}} = \langle \{a, d\}, \{g\}, \{\}, 0 \rangle$ 

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# Cuts are Disjunctive Action Landmarks

#### Theorem (Cuts are Disjunctive Action Landmarks)

Let P be a pcf for  $\langle V, I, O, \gamma \rangle$  (in i-g form) and C be a cut in the justification graph for P.

The set of edge labels from C (formally  $\{o \mid \langle v, o, v' \rangle \in C\}$ ) is a disjunctive action landmark for I.

#### Proof idea:

- ▶ The justification graph corresponds to a simpler problem where some preconditions (those not picked by the pcf) are ignored.
- Cuts are landmarks for this simplified problem.
- ► Hence they are also landmarks for the original problem.

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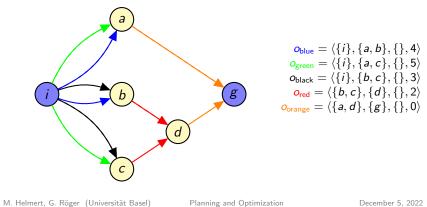
### Example: Cuts in Justification Graphs

### Example (Landmarks)

$$\blacktriangleright L_1 = \{ \underbrace{o_{\text{orange}}} \} \text{ (cost} = 0 \}$$

$$L_3 = \{ o_{\text{red}} \} \text{ (cost } = 2 )$$

$$lacksquare$$
  $L_4 = \{o_{\mathsf{green}}, o_{\mathsf{blue}}\} \; (\mathsf{cost} = 4)$ 



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## Power of Cuts in Justification Graphs

- ▶ Which landmarks can be computed with the cut method?
- ▶ all interesting ones!

#### Proposition (perfect hitting set heuristics)

Let  $\mathcal{L}$  be the set of all "cut landmarks" of a given planning task with initial state I. Then  $h^{MHS}(\mathcal{L}) = h^+(I)$ .

 $\rightsquigarrow$  Hitting set heuristic for  $\mathcal{L}$  is perfect.

#### Proof idea:

▶ Show 1:1 correspondence of hitting sets H for  $\mathcal{L}$  and plans, i.e., each hitting set for  $\mathcal{L}$  corresponds to a plan, and vice versa.

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# G5.3 The I M-Cut Heuristic

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The LM-Cut Heuristic

### LM-Cut Heuristic: Motivation

- In general, there are exponentially many pcfs, hence computing all relevant landmarks is not tractable.
- ► The LM-cut heuristic is a method that chooses pcfs and computes cuts in a goal-oriented way.
- ► As a side effect, it computes a
  - $\triangleright$  a cost partitioning over multiple instances of  $h^{\text{max}}$  that is also
  - a saturated cost partitioning over disjunctive action landmarks. → next week

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The LM-Cut Heuristic

### LM-Cut Heuristic

### h<sup>LM-cut</sup>: Helmert & Domshlak (2009)

Initialize  $h^{LM-cut}(I) := 0$ . Then iterate:

- ① Compute  $h^{\text{max}}$  values of the variables. Stop if  $h^{\text{max}}(g) = 0$ .
- 2 Compute justification graph G for the P that chooses preconditions with maximal  $h^{max}$  value
- **3** Determine the goal zone  $V_g$  of G that consists of all nodes that have a zero-cost path to g.
- Ompute the cut L that contains the labels of all edges  $\langle v, o, v' \rangle$  such that  $v \notin V_g$ ,  $v' \in V_g$  and v can be reached from i without traversing a node in  $V_{\sigma}$ . It is guaranteed that cost(L) > 0.
- **1** Increase  $h^{LM-cut}(I)$  by cost(L).
- **1** Decrease cost(o) by cost(L) for all  $o \in L$ .

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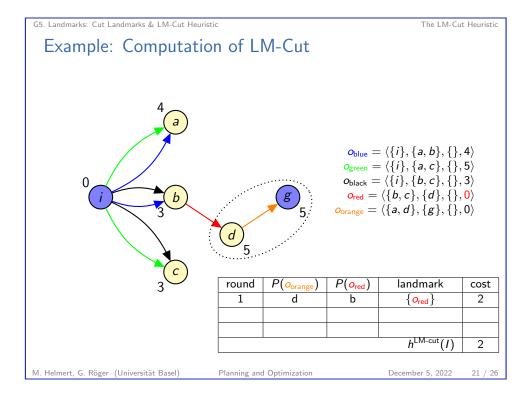
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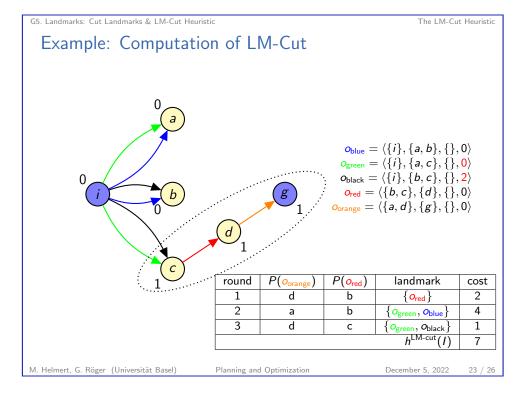
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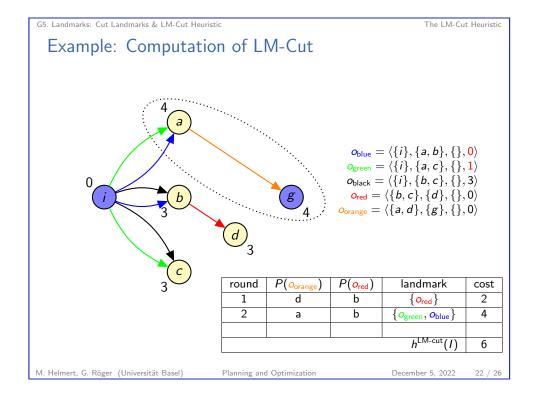
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The LM-Cut Heuristic

# Properties of LM-Cut Heuristic

#### Theorem

Let  $\langle V, I, O, \gamma \rangle$  be a delete-free STRIPS task in i-g normal form. The LM-cut heuristic is admissible:  $h^{LM-cut}(I) \leq h^*(I)$ .

Proof omitted.

If  $\Pi$  is not delete-free, we can compute  $h^{\text{LM-cut}}$  on  $\Pi^+$ . Then  $h^{\text{LM-cut}}$  is bounded by  $h^+$ .

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G5.4 Summary

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# Summary

- ► Cuts in justification graphs are a general method to find disjunctive action landmarks.
- ► The minimum hitting set over all cut landmarks is a perfect heuristic for delete-free planning tasks.
- ► The LM-cut heuristic is an admissible heuristic based on these ideas.

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