

# Planning and Optimization

## G3. Landmarks: Orderings & LM-Count Heuristic

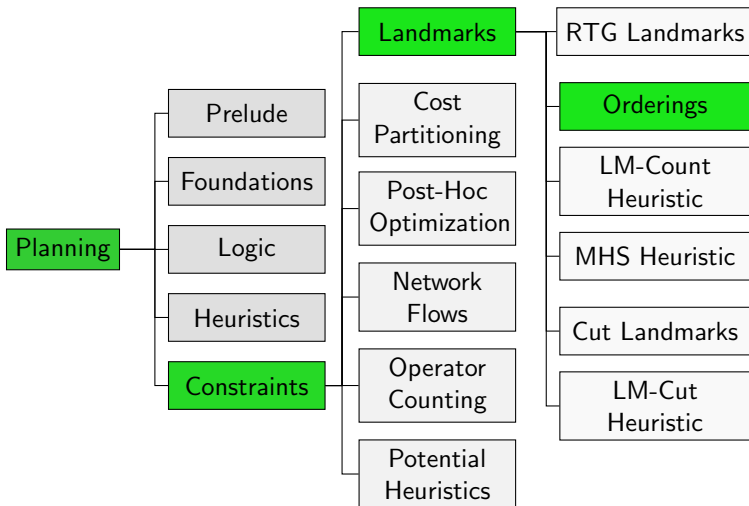
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# Landmark Orderings

# Content of this Course



## Why Landmark Orderings?

- To compute a landmark heuristic estimate for state  $s$  we need landmarks for  $s$ .
- We could invest the time to compute them **for every state from scratch**.
- Alternatively, we can **compute landmarks once** and **propagate** them over operator applications.
- **Landmark orderings** are used to detect landmarks that should be further considered because they (again) need to be satisfied later.
- (We will later see yet another approach, where heuristic computation and landmark computation are integrated  $\rightsquigarrow$  LM-Cut.)

## Example

Consider task  $\langle \{a, b, c, d\}, I, \{o_1, o_2, \dots, o_n\}, d \rangle$  with

- $I(v) = \perp$  for  $v \in \{a, b, c, d\}$ ,
- $o_1 = \langle \top, a \wedge b \rangle$ , and
- $o_2 = \langle a, c \wedge \neg a \wedge \neg b \rangle$ .

You know that  $a, b, c$  and  $d$  are all fact landmarks for  $I$ .

- What landmarks are still required to be made true in state  $I[\langle o_1, o_2 \rangle]$ ?

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- You get the additional information that variable  $a$  must be true immediately before  $d$  is first made true. Any changes?

# Terminology

Let  $\pi = \langle o_1, \dots, o_n \rangle$  be a sequence of operators applicable in state  $I$  and let  $\varphi$  be a formula over the state variables.

- $\varphi$  is **true at time  $i$**  if  $I[\langle o_1, \dots, o_i \rangle] \models \varphi$ .
- Also special case  $i = 0$ :  $\varphi$  is **true at time 0** if  $I \models \varphi$ .
- No formula is true at time  $i < 0$ .
- $\varphi$  is **added at time  $i$**  if it is **true at time  $i$  but not at time  $i - 1$** .
- $\varphi$  is **first added at time  $i$**  if it is **true at time  $i$  but not at any time  $j < i$** .  
We denote this  $i$  by ***first*** $(\varphi, \pi)$ .
- ***last*** $(\varphi, \pi)$  denotes last time in which  $\varphi$  is added in  $\pi$ .

# Landmark Orderings

## Definition (Landmark Orderings)

Let  $\varphi$  and  $\psi$  be formula landmarks. There is

- a **natural ordering** between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow \psi$ ) if in each plan  $\pi$  it holds that  $first(\varphi, \pi) < first(\psi, \pi)$ .  
"  $\varphi$  must be true some time strictly before  $\psi$  is first added'."



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"  $\varphi$  must be true some time strictly before  $\psi$  is first added'."
- a **greedy-necessary ordering** between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow_{gn} \psi$ ) if for every plan  $\pi = \langle o_1, \dots, o_n \rangle$  it holds that  $s[\langle o_1, \dots, o_{first(\psi, \pi)-1} \rangle] \models \varphi$ .  
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"  $\varphi$  must be true immediately before  $\psi$  is first added'."
- a **reasonable ordering** between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow_r \psi$ ) if in each plan  $\pi$  it holds that  $first(\varphi, \pi) \leq last(\psi, \pi)$ .  
"  $\varphi$  must be true some time before  $\psi$  is last added'."

# Natural Orderings

## Definition

There is a **natural ordering** between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow \psi$ ) if in each plan  $\pi$  it holds that  $first(\varphi, \pi) < first(\psi, \pi)$ .

- We can directly determine natural orderings from the *LM* sets computed from the simplified relaxed task graph.
- For fact landmarks  $v, v'$  with  $v \neq v'$ , if  $n_{v'} \in LM(n_v)$  then  $v' \rightarrow v$ .

# Greedy-necessary Orderings

## Definition

There is a **greedy-necessary ordering** between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow_{\text{gn}} \psi$ ) if in each plan where  $\psi$  is first added at time  $i$ ,  $\varphi$  is true at time  $i - 1$ .

- We can again determine such orderings from the sRTG.
- For an OR node  $n_v$ , we define the set of **first achievers** as  $FA(n_v) = \{n_o \mid n_o \in \text{succ}(n_v) \text{ and } n_v \notin LM(n_o)\}$ .
- Then  $v' \rightarrow_{\text{gn}} v$  if  $n_{v'} \in \text{succ}(n_o)$  for all  $n_o \in FA(n_v)$ .

# Landmark Propagation

## Example Revisited

Consider task  $\langle \{a, b, c, d\}, I, \{o_1, o_2, \dots, o_n\}, d \rangle$  with

- $I(v) = \perp$  for  $v \in \{a, b, c, d\}$ ,
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You know that  $a, b, c$  and  $d$  are all fact landmarks for  $I$ .

- What landmarks are still required to be made true in state  $I[\langle o_1, o_2 \rangle]$ ? **All not achieved yet on the state path**
- You get the additional information that variable  $a$  must be true immediately before  $d$  is first made true. Any changes? **Exploit orderings to determine landmarks that are still required.**

## Example Revisited

Consider task  $\langle \{a, b, c, d\}, I, \{o_1, o_2, \dots, o_n\}, d \rangle$  with

- $I(v) = \perp$  for  $v \in \{a, b, c, d\}$ ,
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- There is another path to the same state where  $b$  was never true. What now?

## Example Revisited

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- You get the additional information that variable  $a$  must be true immediately before  $d$  is first made true. Any changes? **Exploit orderings to determine landmarks that are still required.**
- There is another path to the same state where  $b$  was never true. What now? **Exploit information from multiple paths.**



## Context in Search

A landmark graph captures all known landmark information for a current state.

### LM-BFS algorithm

```
graphs[init()] := compute_landmark_graph(init())
open.insert(init())
while open ≠ ∅ do
    s = open.pop()
    if is_goal(s) then return extract_plan(s);
     $\mathcal{G} = \textit{graphs}[s]$ 
    foreach  $\langle a, s' \rangle \in \textit{succ}(s)$  do
         $\mathcal{G}' := \textit{progress\_landmark\_graph}(\mathcal{G}, a, s')$ 
         $\mathcal{G}'' := \textit{merge\_landmark\_graphs}(\textit{graphs}[s'], \mathcal{G}')$ 
         $\textit{graphs}[s'] := \textit{extend\_landmark\_graph}(\mathcal{G}'', s')$ 
    open.insert(s')
```

# Landmark Graph

We combine all known landmark information for the current state in a landmark graph.

## Definition (Landmark Graph)

Let  $\Pi$  be a planning task,  $s$  be a state of  $\Pi$  and  $\mathcal{L}$  be a set of formula landmarks for the initial state with set of orderings  $\mathcal{O}$ .

A **landmark graph** for state  $s$  is a triple  $\mathcal{G} = \langle \mathcal{L}^+, \mathcal{L}^-, \mathcal{O} \rangle$ , where  $\mathcal{L}^+, \mathcal{L}^- \subseteq \mathcal{L}$  and

- $\mathcal{L}^+$  contains landmarks that were already true in all considered paths to  $s$  and
- $\mathcal{L}^-$  contains landmarks for  $s$  that are not true in  $s$ .

# Initial Landmark Graph

## LM-BFS algorithm

```
graphs[init()] := compute_landmark_graph(init())  
open.insert(init())  
while open ≠ ∅ do  
  s = open.pop()  
  if is_goal(s) then return extract_plan(s);  
   $\mathcal{G} = \textit{graphs}[s]$   
  foreach  $\langle a, s' \rangle \in \textit{succ}(s)$  do  
     $\mathcal{G}' := \textit{progress\_landmark\_graph}(\mathcal{G}, a, s')$   
     $\mathcal{G}'' := \textit{merge\_landmark\_graphs}(\textit{graphs}[s'], \mathcal{G}')$   
     $\textit{graphs}[s'] := \textit{extend\_landmark\_graph}(\mathcal{G}'', s')$   
    open.insert(s')
```

Compute  $\mathcal{L}$  and  $\mathcal{O}$  and return

$\langle \{\lambda \in \mathcal{L} \mid \textit{init}() \models \lambda\}, \{\lambda \in \mathcal{L} \mid \textit{init}() \not\models \lambda\}, \mathcal{O} \rangle$

# Progression for a Transition

## LM-BFS algorithm

```
graphs[init()] := compute_landmark_graph(init())  
open.insert(init())  
while open ≠ ∅ do  
    s = open.pop()  
    if is_goal(s) then return extract_plan(s);  
     $\mathcal{G} = \text{graphs}[s]$   
    foreach  $\langle a, s' \rangle \in \text{succ}(s)$  do  
         $\mathcal{G}' := \text{progress\_landmark\_graph}(\mathcal{G}, a, s')$   
         $\mathcal{G}'' := \text{merge\_landmark\_graphs}(\text{graphs}[s'], \mathcal{G}')$   
        graphs[s'] := extend_landmark_graph( $\mathcal{G}''$ , s')  
        open.insert(s')
```

# Progression for a Transition

```
progress_landmark_graph( $\langle \mathcal{L}^+, \mathcal{L}^-, \mathcal{O} \rangle, a, s'$ )
```

```
 $accept := \{ \varphi \in \mathcal{L}^- \mid s' \models \varphi \}$ 
```

```
 $\mathcal{L}'^+ := \mathcal{L}^+ \cup accept$ 
```

```
 $\mathcal{L}'^- := \mathcal{L}^- \setminus accept$ 
```

```
return  $\langle \mathcal{L}'^+, \mathcal{L}'^-, \mathcal{O} \rangle$ 
```

# Exploit Information from Multiple Paths

## LM-BFS algorithm

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graphs[init()] := compute_landmark_graph(init())  
open.insert(init())  
while open ≠ ∅ do  
    s = open.pop()  
    if is_goal(s) then return extract_plan(s);  
     $\mathcal{G} = \textit{graphs}[s]$   
    foreach  $\langle a, s' \rangle \in \textit{succ}(s)$  do  
         $\mathcal{G}' := \textit{progress\_landmark\_graph}(\mathcal{G}, a, s')$   
         $\mathcal{G}'' := \textit{merge\_landmark\_graphs}(\textit{graphs}[s'], \mathcal{G}')$   
         $\textit{graphs}[s'] := \textit{extend\_landmark\_graph}(\mathcal{G}'', s')$   
        open.insert(s')
```

# Exploit Information from Multiple Paths

```
merge_landmark_graphs( $\langle \mathcal{L}_1^+, \mathcal{L}_1^-, \mathcal{O} \rangle, \langle \mathcal{L}_2^+, \mathcal{L}_2^-, \mathcal{O} \rangle$ )
```

```
 $\mathcal{L}^+ := \mathcal{L}_1^+ \cap \mathcal{L}_2^+$ 
```

```
 $\mathcal{L}^- := \mathcal{L}_1^- \cup \mathcal{L}_2^-$ 
```

```
return  $\langle \mathcal{L}^+, \mathcal{L}^-, \mathcal{O} \rangle$ 
```

# Exploit Ordering Information

## LM-BFS algorithm

```
graphs[init()] := compute_landmark_graph(init())  
open.insert(init())  
while open ≠ ∅ do  
    s = open.pop()  
    if is_goal(s) then return extract_plan(s);  
     $\mathcal{G} = \textit{graphs}[s]$   
    foreach  $\langle a, s' \rangle \in \textit{succ}(s)$  do  
         $\mathcal{G}' := \textit{progress\_landmark\_graph}(\mathcal{G}, a, s')$   
         $\mathcal{G}'' := \textit{merge\_landmark\_graphs}(\textit{graphs}[s'], \mathcal{G}')$   
         $\textit{graphs}[s'] := \textit{extend\_landmark\_graph}(\mathcal{G}'', s')$   
        open.insert(s')
```

How do we define  $\textit{graphs}[s']$  if we encounter  $s'$  for the first time?



# Exploit Ordering Information

## LM-BFS algorithm

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     $\textit{graphs}[s'] := \textit{extend\_landmark\_graph}(\mathcal{G}'', s')$   
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```

## Exploit Ordering Information

```
extend_landmark_graph( $\langle \mathcal{L}^+, \mathcal{L}^-, \mathcal{O} \rangle, s'$ )
```

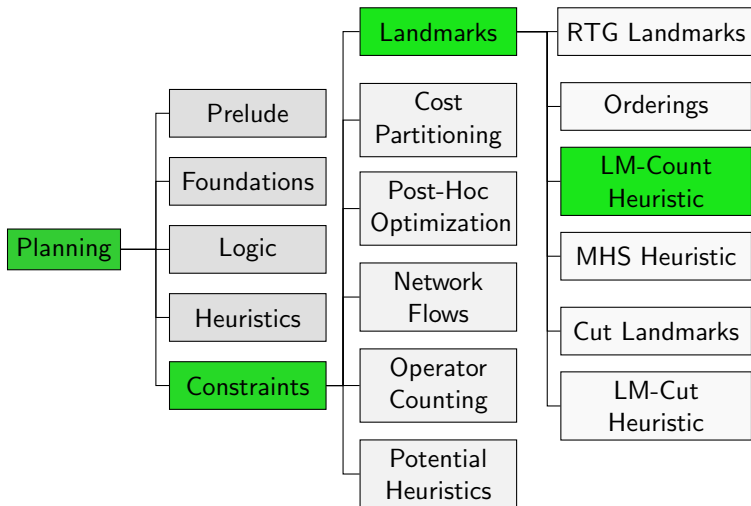
$$\mathcal{L}_G := \{\varphi \in \mathcal{L}^+ \mid s' \not\models \varphi \text{ and } \varphi \text{ is implied by goal}\}$$
$$\mathcal{L}_{gn} := \{\varphi \in \mathcal{L}^+ \mid s' \not\models \varphi \text{ and } \exists \psi \rightarrow_{gn} \psi \in \mathcal{O} : \psi \notin \mathcal{L}^+\}$$
$$\mathcal{L}_r := \{\varphi \in \mathcal{L}^+ \mid \exists \psi \rightarrow_r \varphi \in \mathcal{O} \text{ with } \psi \notin \mathcal{L}^+\}$$
$$\mathcal{L}'^- := \mathcal{L}^- \cup \mathcal{L}_G \cup \mathcal{L}_{gn} \cup \mathcal{L}_r$$

```
return  $\langle \mathcal{L}^+, \mathcal{L}'^-, \mathcal{O} \rangle$ 
```

- $\mathcal{L}_G$ : “currently false but must be true in the goal”
- $\mathcal{L}_{gn}$ : “currently false but must be true immediately before some unachieved landmark becomes true”
- $\mathcal{L}_r$ : “must again become true after some unachieved landmark became true”

# Landmark-count Heuristic

# Content of this Course



## Landmark-count Heuristic

The landmark-count heuristic counts the landmarks that still have to be achieved.

### Definition (LM-count Heuristic)

Let  $\Pi$  be a planning task,  $s$  be a state and  $\mathcal{G} = \langle \mathcal{L}^+, \mathcal{L}^-, \mathcal{O} \rangle$  be a landmark graph for  $s$ .

The **LM-count heuristic** for  $s$  and  $\mathcal{G}$  is

$$h_{\mathcal{L}}^{\text{LM-count}}(\mathcal{G}) = |\mathcal{L}^-|.$$

In the original work, the set  $\mathcal{L}^-$  was determined without considering information from multiple paths.

# LM-count Heuristic is Path-dependent

- LM-count heuristic gives estimates for landmark graphs, which depend on the considered paths.
- Search algorithms need estimates for states.
- $\rightsquigarrow$  we use estimate from the **current** landmark graph.
- $\rightsquigarrow$  heuristic estimate for a state is **not well-defined**.

# LM-count Heuristic is Inadmissible

## Example

Consider STRIPS planning task  $\Pi = \langle \{a, b\}, \emptyset, \{o\}, \{a, b\} \rangle$  with  $o = \langle \emptyset, \{a, b\}, \emptyset, 1 \rangle$ . Let  $\mathcal{L} = \{a, b\}$  and  $\mathcal{O} = \emptyset$ .

The estimate for the initial state is  $h^{\text{LM-count}}(\langle \emptyset, \{a, b\}, \emptyset \rangle) = 2$  while  $h^*(I) = 1$ .

$\rightsquigarrow h^{\text{LM-count}}$  is **inadmissible**.

## LM-count Heuristic: Comments

- LM-Count alone is not a particularly informative heuristic.
- On the positive side, it complements  $h^{FF}$  very well.
- For example, the LAMA planning system alternates between expanding a state with minimal  $h^{FF}$  and minimal  $h^{LM-count}$  estimate.
- There is an admissible variant of the heuristic based on operator cost partitioning.



# Summary

# Summary

- We can propagate landmark sets over action applications.
- Landmark orderings can be useful for detecting when a landmark that has already been achieved should be further considered.
- We can combine the landmark information from several paths to the same state.
- The LM-count heuristic counts how many landmarks still need to be satisfied.
- The LM-count heuristic is inadmissible (but there is an admissible variant).