

Planning and Optimization

G1. Constraints: Introduction

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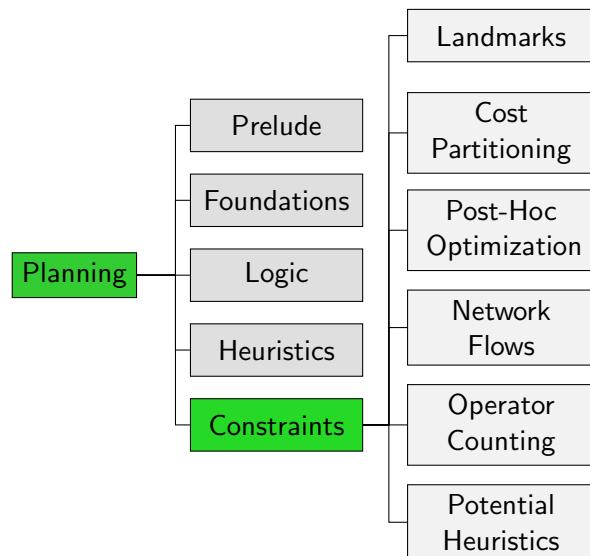
November 28, 2022 — G1. Constraints: Introduction

G1.1 Constraint-based Heuristics

G1.2 Multiple Heuristics

G1.3 Summary

Content of this Course



G1.1 Constraint-based Heuristics

Coming Up with Heuristics in a Principled Way

General Procedure for Obtaining a Heuristic

Solve a simplified version of the problem.

Major ideas for heuristics in the planning literature:

- ▶ delete relaxation
- ▶ abstraction
- ▶ **landmarks**
- ▶ critical paths
- ▶ **network flows**
- ▶ **potential heuristic**

Landmarks, network flows and potential heuristics are based on **constraints** that can be specified for a planning task.

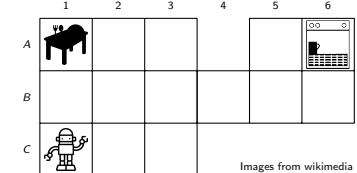
Constraints

Some heuristics exploit **constraints** that describe something that holds in every solution of the task.

For instance, every solution is such that

- ▶ a variable takes a certain value in at least one visited state.
(a **fact landmark** constraint)

Constraints: Example



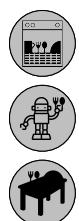
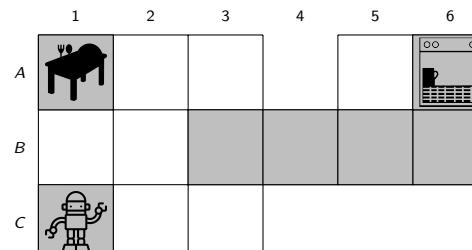
Images from wikipedia

FDR planning task $\langle V, I, O, \gamma \rangle$ with

- ▶ $V = \{robot-at, dishes-at\}$ with
 - ▶ $\text{dom}(robot-at) = \{A1, \dots, C3, B4, A5, \dots, B6\}$
 - ▶ $\text{dom}(dishes-at) = \{\text{Table}, \text{Robot}, \text{Dishwasher}\}$
- ▶ $I = \{robot-at \mapsto C1, dishes-at \mapsto \text{Table}\}$
- ▶ operators
 - ▶ move-x-y to move from cell x to adjacent cell y
 - ▶ pickup dishes, and
 - ▶ load dishes into the dishwasher.
- ▶ $\gamma = (robot-at = B6) \wedge (dishes-at = \text{Dishwasher})$

Fact Landmarks: Example

Which values do *robot-at* and *dishes-at* take in every solution?



- ▶ $robot-at = C1, dishes-at = \text{Table}$ (initial state)
- ▶ $robot-at = B6, dishes-at = \text{Dishwasher}$ (goal state)
- ▶ $robot-at = A1, robot-at = B3, robot-at = B4, robot-at = B5, robot-at = A6, dishes-at = \text{Robot}$

Constraints

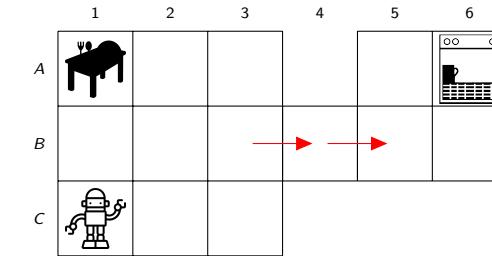
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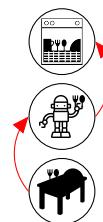
- ▶ a variable takes some value in at least one visited state.
(a **fact landmark** constraint)
- ▶ an action must be applied.
(an **action landmark** constraint)

Action Landmarks: Example

Which actions must be applied in every solution?



- ▶ pickup
- ▶ load
- ▶ move-B3-B4
- ▶ move-B4-B5



Constraints

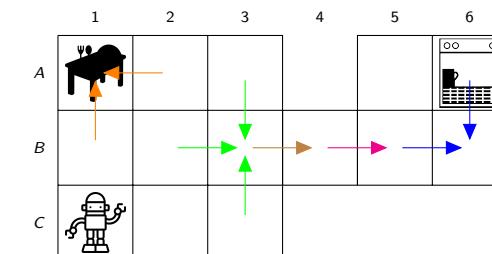
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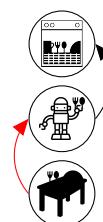
- ▶ a variable takes some **value** in at least one visited state.
(a **fact landmark** constraint)
- ▶ an action must be applied.
(an **action landmark** constraint)
- ▶ at least one action from a set of actions must be applied.
(a **disjunctive action landmark** constraint)

Disjunctive Action Landmarks: Example

Which set of actions is such that at least one must be applied?



- ▶ {pickup}
- ▶ {load}
- ▶ {move-B3-B4}
- ▶ {move-B4-B5}
- ▶ {move-A6-B6, move-B5-B6}
- ▶ {move-A3-B3, move-B2-B3, move-C3-B3}
- ▶ {move-B1-A1, move-A2-A1}
- ▶ ...



Constraints

Some heuristics exploit **constraints** that describe something that holds in every solution of the task.

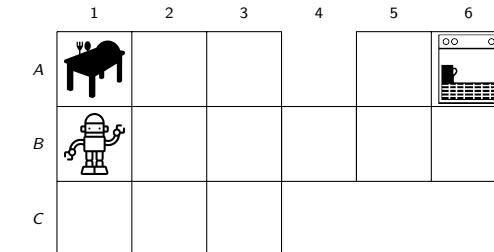
For instance, every solution is such that

- ▶ a variable takes some value in at least one visited state.
(a **fact landmark** constraint)
- ▶ at least one action from a set of actions must be applied.
(a **disjunctive action landmark** constraint)
- ▶ fact consumption and production is “balanced”.
(a **network flow** constraint)

Network Flow: Example

Consider the fact $\text{robot-at} = B2$.

How often are actions used that enter this cell?



Answer: as often as actions that leave this cell

If Count_o denotes how often operator o is applied, we have:

$$\begin{aligned} \text{Count}_{\text{move-A1-B1}} + \text{Count}_{\text{move-B2-B1}} + \text{Count}_{\text{move-C1-B1}} = \\ \text{Count}_{\text{move-B1-A1}} + \text{Count}_{\text{move-B1-B2}} + \text{Count}_{\text{move-B1-C1}} \end{aligned}$$

G1.2 Multiple Heuristics

Combining Admissible Heuristics Admissibly

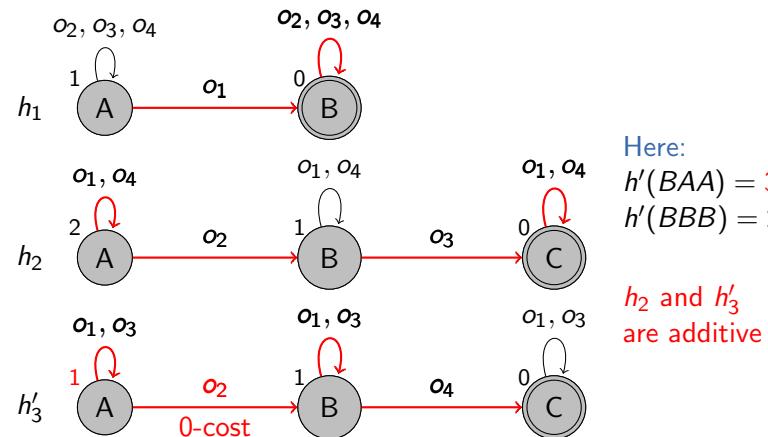
Major ideas to combine heuristics admissibly:

- ▶ maximize
- ▶ canonical heuristic (for abstractions)
- ▶ **minimum hitting set** (for landmarks)
- ▶ **cost partitioning**
- ▶ **operator counting**

Often computed as solution to a **(integer) linear program**.

Combining Heuristics Admissibly: Example

Let $h' = h_1 + h_2 + h'_3$, where $h'_3 = h^{v3}$ assuming $\text{cost}_3(o_2) = 0$.



Here:
 $h'(BAA) = 3$
 $h'(BBB) = 2$
 h_2 and h'_3 are additive

Consider solution $\langle o_1, o_2, o_3, o_4 \rangle$

Cost partitioning

Using the cost of every operator only in one heuristic is called a **zero-one cost partitioning**.

More generally, heuristics are additive if all operator costs are distributed in a way that the sum of the individual costs is no larger than the cost of the operator.

This can also be expressed as a constraint, the **cost partitioning constraint**:

$$\sum_{i=1}^n \text{cost}_i(o) \leq \text{cost}(o) \text{ for all } o \in O$$

(more details later)

G1.3 Summary

Summary

- ▶ Landmarks and network flows are **constraints** that describe something that holds in every solution of the task.
- ▶ Heuristics can be combined admissibly if the **cost partitioning constraint** is satisfied.