

Planning and Optimization

E3. Landmarks: LM-Cut Heuristic

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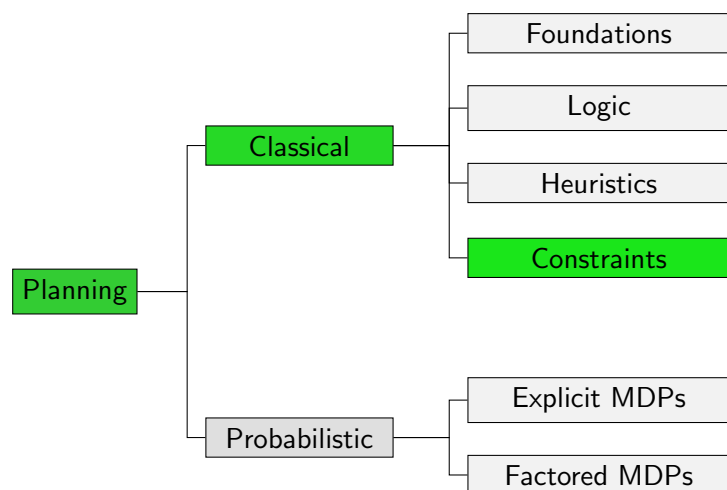
E3.1 i-g Form

E3.2 Cut Landmarks

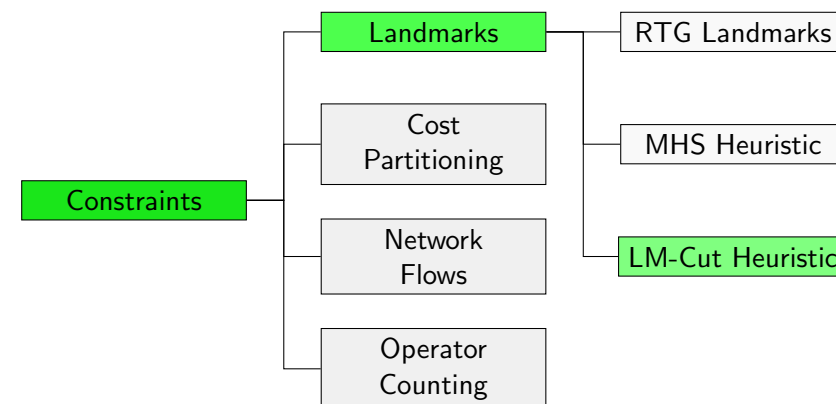
E3.3 The LM-Cut Heuristic

E3.4 Summary & Outlook

Content of this Course



Content of this Course: Constraints



Roadmap for this Chapter

- ▶ We first introduce a new **normal form** for **delete-free STRIPS tasks** that simplifies later definitions.
- ▶ We then present a method that **computes disjunctive action landmarks** for such tasks.
- ▶ We conclude with the **LM-cut heuristic** that builds on this method.

E3.1 i-g Form

Delete-Free STRIPS Planning Task in i-g Form (1)

In this chapter, we only consider **delete-free** STRIPS tasks in a special form:

Definition (i-g Form for Delete-free STRIPS)

A delete-free STRIPS planning task $\langle V, I, O, \gamma \rangle$ is in **i-g form** if

- ▶ V contains atoms i and g
- ▶ Initially exactly i is true: $I(v) = \mathbf{T}$ iff $v = i$
- ▶ g is the only goal atom: $\gamma = \{g\}$
- ▶ Every action has at least one precondition.

Transformation to i-g Form

Every delete-free STRIPS task $\Pi = \langle V, I, O, \gamma \rangle$ can easily be transformed into an analogous task in i-g form.

- ▶ If i or g are in V already, rename them everywhere.
- ▶ Add i and g to V .
- ▶ Add an operator $\langle \{i\}, \{v \in V \mid I(v) = \mathbf{T}\}, \{\}, 0 \rangle$.
- ▶ Add an operator $\langle \gamma, \{g\}, \{\}, 0 \rangle$.
- ▶ Replace all operator preconditions \mathbf{T} with i .
- ▶ Replace initial state and goal.

For the remainder of this chapter, we assume tasks in i-g form.

Example: Delete-Free Planning Task in i-g Form

Example

Consider a delete-free STRIPS planning task $\langle V, I, O, \gamma \rangle$ with $V = \{i, a, b, c, d, g\}$, $I = \{i \mapsto \mathbf{T}\} \cup \{v \mapsto \mathbf{F} \mid v \in V \setminus \{i\}\}$, $\gamma = \{g\}$ and operators

- ▶ $O_{\text{blue}} = \langle \{i\}, \{a, b\}, \{\}, 4 \rangle$,
- ▶ $O_{\text{green}} = \langle \{i\}, \{a, c\}, \{\}, 5 \rangle$,
- ▶ $O_{\text{black}} = \langle \{i\}, \{b, c\}, \{\}, 3 \rangle$,
- ▶ $O_{\text{red}} = \langle \{b, c\}, \{d\}, \{\}, 2 \rangle$, and
- ▶ $O_{\text{orange}} = \langle \{a, d\}, \{g\}, \{\}, 0 \rangle$.

optimal solution to reach g from i :

- ▶ plan: $\langle O_{\text{blue}}, O_{\text{black}}, O_{\text{red}}, O_{\text{orange}} \rangle$
- ▶ cost: $4 + 3 + 2 + 0 = 9$ ($= h^+(I)$ because plan is **optimal**)

E3.2 Cut Landmarks

Justification Graphs

Definition (Precondition Choice Function)

A **precondition choice function (pcf)** $P : O \rightarrow V$ for a delete-free STRIPS task $\Pi = \langle V, I, O, \gamma \rangle$ in i-g form maps each operator to one of its preconditions (i.e. $P(o) \in \text{pre}(o)$ for all $o \in O$).

Definition (Justification Graphs)

Let P be a pcf for $\langle V, I, O, \gamma \rangle$ in i-g form. The **justification graph** for P is the directed, edge-labeled graph $J = \langle V, E \rangle$, where

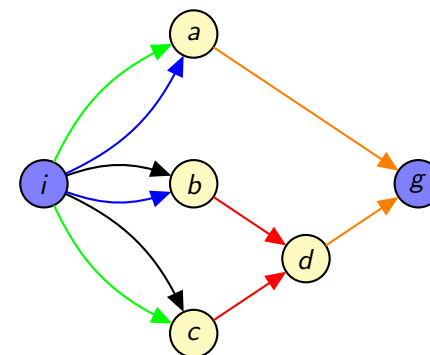
- ▶ the vertices are the variables from V , and
- ▶ E contains an edge $P(o) \xrightarrow{o} a$ for each $o \in O$, $a \in \text{add}(o)$.

Example: Justification Graph

Example (Precondition Choice Function)

$$P(O_{\text{blue}}) = P(O_{\text{green}}) = P(O_{\text{black}}) = i, P(O_{\text{red}}) = b, P(O_{\text{orange}}) = a$$

$$P'(O_{\text{blue}}) = P'(O_{\text{green}}) = P'(O_{\text{black}}) = i, P'(O_{\text{red}}) = c, P'(O_{\text{orange}}) = d$$

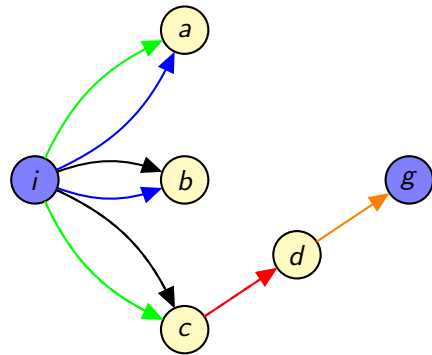


- $O_{\text{blue}} = \langle \{i\}, \{a, b\}, \{\}, 4 \rangle$
- $O_{\text{green}} = \langle \{i\}, \{a, c\}, \{\}, 5 \rangle$
- $O_{\text{black}} = \langle \{i\}, \{b, c\}, \{\}, 3 \rangle$
- $O_{\text{red}} = \langle \{b, c\}, \{d\}, \{\}, 2 \rangle$
- $O_{\text{orange}} = \langle \{a, d\}, \{g\}, \{\}, 0 \rangle$

Cuts

Definition (Cut)

A **cut** in a justification graph is a subset C of its edges such that all paths from i to g contain an edge from C .



$O_{\text{blue}} = \langle \{i\}, \{a, b\}, \{\}, 4 \rangle$
 $O_{\text{green}} = \langle \{i\}, \{a, c\}, \{\}, 5 \rangle$
 $O_{\text{black}} = \langle \{i\}, \{b, c\}, \{\}, 3 \rangle$
 $O_{\text{red}} = \langle \{b, c\}, \{d\}, \{\}, 2 \rangle$
 $O_{\text{orange}} = \langle \{a, d\}, \{g\}, \{\}, 0 \rangle$

Cuts are Disjunctive Action Landmarks

Theorem (Cuts are Disjunctive Action Landmarks)

Let P be a pcf for $\langle V, I, O, \gamma \rangle$ (in i - g form) and C be a **cut** in the justification graph for P .

The set of **edge labels** from C (formally $\{o \mid \langle v, o, v' \rangle \in C\}$) is a **disjunctive action landmark** for I .

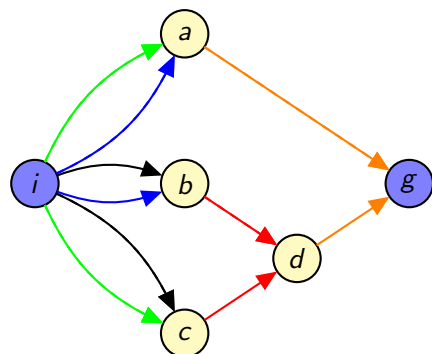
Proof idea:

- ▶ The justification graph corresponds to a simpler problem where some preconditions (those not picked by the pcf) are ignored.
- ▶ Cuts are landmarks for this simplified problem.
- ▶ Hence they are also landmarks for the original problem.

Example: Cuts in Justification Graphs

Example (Landmarks)

- ▶ $L_1 = \{O_{\text{orange}}\}$ (cost = 0)
- ▶ $L_2 = \{O_{\text{green}}, O_{\text{black}}\}$ (cost = 3)
- ▶ $L_3 = \{O_{\text{red}}\}$ (cost = 2)
- ▶ $L_4 = \{O_{\text{green}}, O_{\text{blue}}\}$ (cost = 4)



$O_{\text{blue}} = \langle \{i\}, \{a, b\}, \{\}, 4 \rangle$
 $O_{\text{green}} = \langle \{i\}, \{a, c\}, \{\}, 5 \rangle$
 $O_{\text{black}} = \langle \{i\}, \{b, c\}, \{\}, 3 \rangle$
 $O_{\text{red}} = \langle \{b, c\}, \{d\}, \{\}, 2 \rangle$
 $O_{\text{orange}} = \langle \{a, d\}, \{g\}, \{\}, 0 \rangle$

Power of Cuts in Justification Graphs

- ▶ Which landmarks can be computed with the cut method?
- ▶ **all interesting ones!**

Proposition (perfect hitting set heuristics)

Let \mathcal{L} be the set of **all** "cut landmarks" of a given planning task with initial state I . Then $h^{\text{MHS}}(\mathcal{L}) = h^+(I)$.

⇔ Hitting set heuristic for \mathcal{L} is **perfect**.

Proof idea:

- ▶ Show 1:1 correspondence of hitting sets H for \mathcal{L} and plans, i.e., each hitting set for \mathcal{L} corresponds to a plan, and vice versa.

E3.3 The LM-Cut Heuristic

LM-Cut Heuristic: Motivation

- ▶ In general, there are exponentially many pcfs, hence computing all relevant landmarks is not tractable.
 - ▶ The **LM-cut heuristic** is a method that chooses pcfs and computes cuts in a **goal-oriented** way.
 - ▶ As a side effect, it computes
 - ▶ a cost partitioning over multiple instances of h^{\max} that is also
 - ▶ a **saturated cost partitioning** over disjunctive action landmarks.
- ↪ currently one of the best admissible planning heuristic

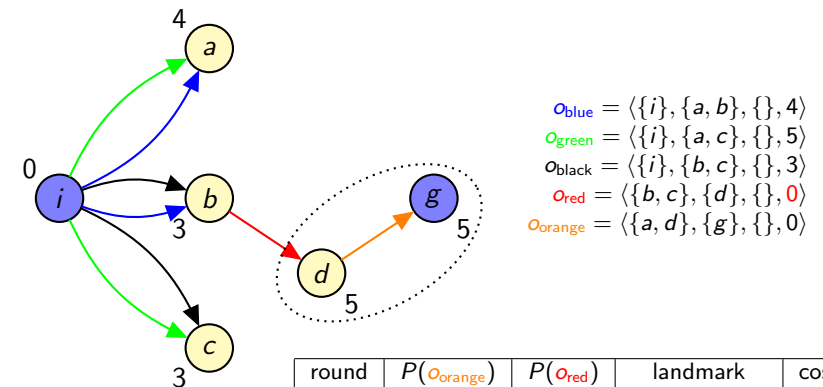
LM-Cut Heuristic

$h^{\text{LM-cut}}$: Helmert & Domshlak (2009)

Initialize $h^{\text{LM-cut}}(I) := 0$. Then iterate:

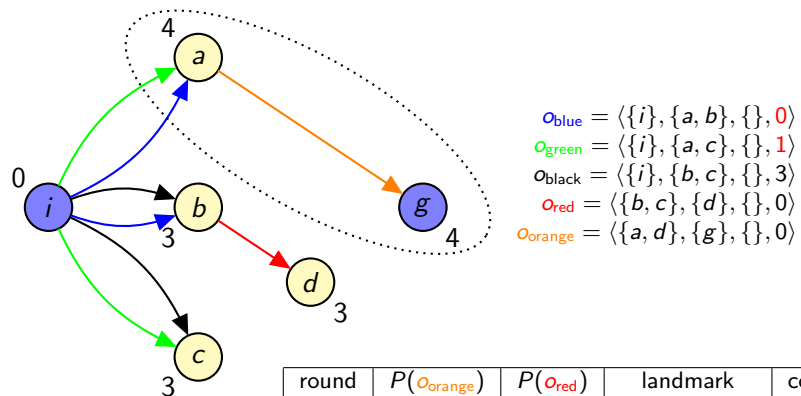
- 1 Compute h^{\max} values of the variables. Stop if $h^{\max}(g) = 0$.
- 2 Compute justification graph G for the P that chooses preconditions with **maximal h^{\max} value**
- 3 Determine the **goal zone** V_g of G that consists of all nodes that have a zero-cost path to g .
- 4 Compute the cut L that contains the labels of all edges $\langle v, o, v' \rangle$ such that $v \notin V_g$, $v' \in V_g$ and v can be reached from i without traversing a node in V_g .
It is guaranteed that $\text{cost}(L) > 0$.
- 5 Increase $h^{\text{LM-cut}}(I)$ by $\text{cost}(L)$.
- 6 Decrease $\text{cost}(o)$ by $\text{cost}(L)$ for all $o \in L$.

Example: Computation of LM-Cut



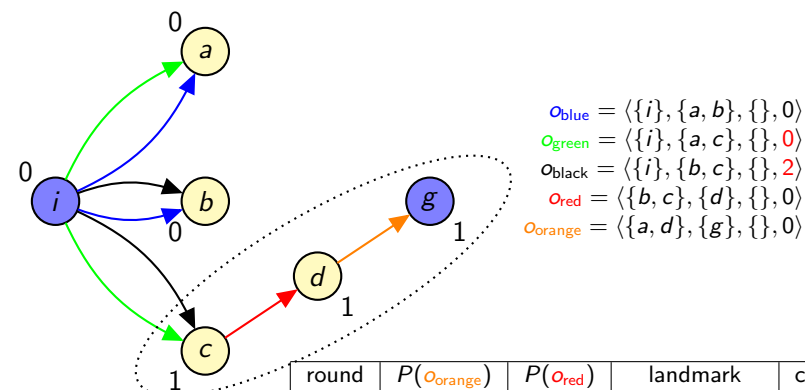
round	$P(O_{\text{orange}})$	$P(O_{\text{red}})$	landmark	cost
1	d	b	$\{O_{\text{red}}\}$	2
			$h^{\text{LM-cut}}(I)$	2

Example: Computation of LM-Cut



round	$P(O_{\text{orange}})$	$P(O_{\text{red}})$	landmark	cost
1	d	b	$\{O_{\text{red}}\}$	2
2	a	b	$\{O_{\text{green}}, O_{\text{blue}}\}$	4
			$h^{\text{LM-cut}}(I)$	6

Example: Computation of LM-Cut



round	$P(O_{\text{orange}})$	$P(O_{\text{red}})$	landmark	cost
1	d	b	$\{O_{\text{red}}\}$	2
2	a	b	$\{O_{\text{green}}, O_{\text{blue}}\}$	4
3	d	c	$\{O_{\text{green}}, O_{\text{black}}\}$	1
			$h^{\text{LM-cut}}(I)$	7

Properties of LM-Cut Heuristic

Theorem

Let $\langle V, I, O, \gamma \rangle$ be a delete-free STRIPS task in i - g normal form.

The **LM-cut heuristic is admissible**: $h^{\text{LM-cut}}(I) \leq h^*(I)$.

Proof omitted.

If Π is not delete-free, we can compute $h^{\text{LM-cut}}$ on Π^+ .

Then $h^{\text{LM-cut}}$ is bounded by h^+ .



E3.4 Summary & Outlook

Summary



- ▶ Cuts in justification graphs are a general method to find disjunctive action landmarks.
- ▶ The minimum hitting set over all cut landmarks is a perfect heuristic for delete-free planning tasks.
- ▶ The LM-cut heuristic is an admissible heuristic based on these ideas.

Literature (1)



References on landmark heuristics:

-  Julie Porteous, Laura Sebastia and Joerg Hoffmann.
On the Extraction, Ordering, and Usage of Landmarks in Planning.
Proc. ECP 2001, pp. 174–182, 2013.
Introduces landmarks.
-  Malte Helmert and Carmel Domshlak.
Landmarks, Critical Paths and Abstractions: What's the Difference Anyway?
Proc. ICAPS 2009, pp. 162–169, 2009.
Introduces cut landmarks and LM-cut heuristic.

Literature (2)

-  Lin Zhu and Robert Givan.
Landmark Extraction via Planning Graph Propagation.
Doctoral Consortium ICAPS 2003, 2003.
Core idea for complete landmark generation.
-  Emil Keyder, Silvia Richter and Malte Helmert.
Sound and Complete Landmarks for And/Or Graphs
Proc. ECAI 2010, pp. 335–340, 2010.
Introduces landmarks from AND/OR graphs and usage of Π^m compilation.

Literature (3)

-  Silvia Richter and Matthias Westphal.
The LAMA Planner: Guiding Cost-Based Anytime Planning with Landmarks.
JAIR 39 (2010), pp. 127–177, 2010.
Introduces landmark-count heuristic and contains another landmark generation method.
-  Erez Karpas and Carmel Domshlak.
Cost-Optimal Planning with Landmarks.
Proc. IJCAI 2009, pp. 1728–1733, 2009.
Introduces admissible variant of landmark heuristic.