

# Planning and Optimization

## B1. Overview of Classical Planning Algorithms

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October 5, 2020

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B1.1 The Big Three

B1.2 Explicit Search

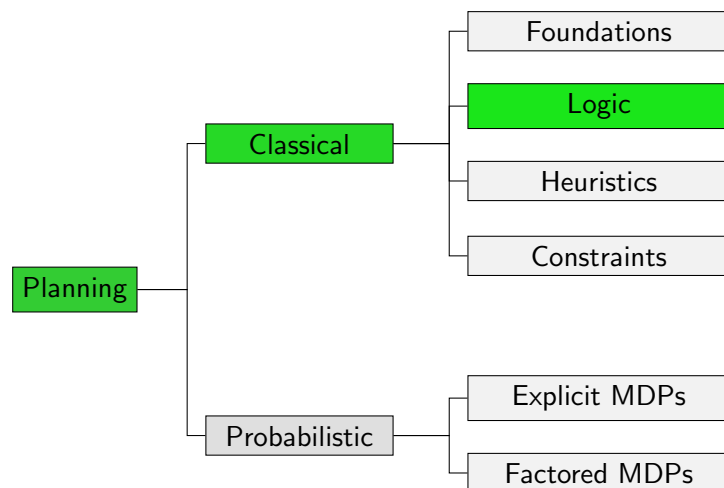
B1.3 SAT Planning

B1.4 Symbolic Search

B1.5 Planning System Examples

B1.6 Summary

## Content of this Course



# B1.1 The Big Three

# Classical Planning Algorithms

Let's start solving planning tasks!

This Chapter

very high-level overview of classical planning algorithms

- ▶ **bird's eye view:** no details, just some very brief ideas

# The Big Three

Of the many planning approaches, three techniques stand out:

- ▶ **explicit search** ~↔ Chapters B2–B4, Parts C–F
- ▶ **SAT planning** ~↔ Chapters B5–B6
- ▶ **symbolic search** ~↔ Chapters B7–B8

also: many algorithm portfolios

# Satisficing or Optimal Planning?

must carefully distinguish:

- ▶ **satisficing planning:** any plan is OK (cheaper ones preferred)
- ▶ **optimal planning:** plans must have minimum cost

solved by similar techniques, but:

- ▶ details **very different**
- ▶ almost **no overlap** between best techniques for satisficing planning and best techniques for optimal planning
- ▶ many tasks that are trivial for satisficing planners are impossibly hard for optimal planners

# B1.2 Explicit Search

# Explicit Search

You know this one already! (Hopefully.)

# Reminder: State-Space Search

## Need to Catch Up?

- ▶ We **assume prior knowledge** of basic search algorithms:

- ▶ uninformed vs. informed (heuristic)
- ▶ satisficing vs. optimal
- ▶ heuristics and their properties
- ▶ specific algorithms: e.g., breadth-first search, greedy best-first search, A\*

- ▶ If you are not familiar with them, we recommend Ch. 5–19 of the [Foundations of Artificial Intelligence](https://dmi.unibas.ch/en/academics/computer-science/courses-in-spring-semester-2020/lecture-foundations-of-artificial-intelligence/) course:

<https://dmi.unibas.ch/en/academics/computer-science/courses-in-spring-semester-2020/lecture-foundations-of-artificial-intelligence/>

# Reminder: Interface for Heuristic Search Algorithms

## Abstract Interface Needed for Heuristic Search Algorithms

- ▶ `init()`       ↔ returns initial state
- ▶ `is_goal(s)`   ↔ tests if `s` is a goal state
- ▶ `succ(s)`       ↔ returns all pairs  $\langle a, s' \rangle$  with  $s \xrightarrow{a} s'$
- ▶ `cost(a)`       ↔ returns cost of action `a`
- ▶ `h(s)`         ↔ returns heuristic value for state `s`

↔ Foundations of Artificial Intelligence course, Chapters 6 and 13

# State Space vs. Search Space

- ▶ Planning tasks induce transition systems (a.k.a. state spaces) with an initial state, labeled transitions and goal states.
- ▶ State-space search searches state spaces with an initial state, a successor function and goal states.
- ↔ looks like an obvious correspondence
- ▶ However, in planning as search, the state space being searched **can be different** from the state space of the planning task.
- ▶ When we need to make a distinction, we speak of
  - ▶ the **state space** of the planning task whose states are called **world states** vs.
  - ▶ the **search space** of the search algorithm whose states are called **search states**.

## Design Choice: Search Direction

How to apply explicit search to planning?  $\rightsquigarrow$  many design choices!

### Design Choice: Search Direction

- ▶ **progression**: forward from initial state to goal
- ▶ **regression**: backward from goal states to initial state
- ▶ **bidirectional search**

$\rightsquigarrow$  Chapters B2–B4

## Design Choice: Search Algorithm

How to apply explicit search to planning?  $\rightsquigarrow$  many design choices!

### Design Choice: Search Algorithm

- ▶ **uninformed search**:  
depth-first, breadth-first, iterative depth-first, . . .
- ▶ **heuristic search (systematic)**:  
greedy best-first,  $A^*$ , weighted  $A^*$ ,  $IDA^*$ , . . .
- ▶ **heuristic search (local)**:  
hill-climbing, simulated annealing, beam search, . . .

## Design Choice: Search Control

How to apply explicit search to planning?  $\rightsquigarrow$  many design choices!

### Design Choice: Search Control

- ▶ **heuristics** for informed search algorithms
- ▶ **pruning techniques**: invariants, symmetry elimination, partial-order reduction, helpful actions pruning, . . .

How do we find good heuristics in a domain-independent way?

$\rightsquigarrow$  one of the main focus areas of classical planning research

$\rightsquigarrow$  Parts C–F

# B1.3 SAT Planning

## SAT Planning: Basic Idea

- ▶ formalize problem of finding plan with a given horizon (length bound) as a propositional satisfiability problem and feed it to a generic SAT solver
- ▶ to obtain a (semi-) complete algorithm, try with increasing horizons until a plan is found (= the formula is satisfiable)
- ▶ important optimization: allow applying several non-conflicting operators “at the same time” so that a shorter horizon suffices

## SAT Encodings: Variables

- ▶ given propositional planning task  $\langle V, I, O, \gamma \rangle$
- ▶ given horizon  $T \in \mathbb{N}_0$

### Variables of SAT Encoding

- ▶ propositional variables  $v^i$  for all  $v \in V, 0 \leq i \leq T$   
encode state after  $i$  steps of the plan
- ▶ propositional variables  $o^i$  for all  $o \in O, 1 \leq i \leq T$   
encode operator(s) applied in  $i$ -th step of the plan

## Design Choice: SAT Encoding

Again, there are several important design choices.

### Design Choice: SAT Encoding

- ▶ sequential or parallel
- ▶ many ways of modeling planning semantics in logic

↔ main focus of research on SAT planning

## Design Choice: SAT Solver

Again, there are several important design choices.

### Design Choice: SAT Solver

- ▶ out-of-the-box like MiniSAT, Glucose, Lingeling
- ▶ planning-specific modifications

## Design Choice: Evaluation Strategy

Again, there are several important **design choices**.

### Design Choice: Evaluation Strategy

- ▶ always advance horizon by +1 or more aggressively
- ▶ possibly probe multiple horizons concurrently

## B1.4 Symbolic Search

## Symbolic Search Planning: Basic Ideas

- ▶ search processes **sets of states** at a time
- ▶ operators, goal states, state sets reachable with a given cost etc. represented by **binary decision diagrams (BDDs)** (or similar data structures)
- ▶ **hope**: exponentially large state sets can be represented as polynomially sized BDDs, which can be efficiently processed
- ▶ perform **symbolic breadth-first search** (or something more sophisticated) on these set representations

## Symbolic Breadth-First Progression Search

prototypical algorithm:

### Symbolic Breadth-First Progression Search

```

def bfs-progression( $V, I, O, \gamma$ ):
     $goal\_states := models(\gamma)$ 
     $reached_0 := \{I\}$ 
     $i := 0$ 
    loop:
        if  $reached_i \cap goal\_states \neq \emptyset$ :
            return solution found
         $reached_{i+1} := reached_i \cup apply(reached_i, O)$ 
        if  $reached_{i+1} = reached_i$ :
            return no solution exists
         $i := i + 1$ 

```

↔ If we can implement operations  **$models, \{I\}, \cap, \neq \emptyset, \cup,$**   
 **$apply$**  and  **$=$**  efficiently, this is a reasonable algorithm.

## Design Choice: Symbolic Data Structure

Again, there are several important **design choices**.

### Design Choice: Symbolic Data Structure

- ▶ BDDs
- ▶ ADDs
- ▶ EVMDDs
- ▶ SDDs

## Other Design Choices

- ▶ additionally, same design choices as for explicit search:
  - ▶ search direction
  - ▶ search algorithm
  - ▶ search control (incl. heuristics)
- ▶ in practice, hard to make heuristics and other advanced search control efficient for symbolic search  
 ~→ rarely used

## B1.5 Planning System Examples

## Planning Systems: FF

### FF (Hoffmann & Nebel, 2001)

- ▶ **problem class:** satisficing
- ▶ **algorithm class:** explicit search
- ▶ **search direction:** forward search
- ▶ **search algorithm:** enforced hill-climbing
- ▶ **heuristic:** FF heuristic (inadmissible)
- ▶ **other aspects:** helpful action pruning; goal agenda manager

~→ breakthrough for heuristic search planning;  
winner of IPC 2000

## Planning Systems: LAMA

### LAMA (Richter & Westphal, 2008)

- ▶ problem class: satisficing
- ▶ algorithm class: explicit search
- ▶ search direction: forward search
- ▶ search algorithm: restarting Weighted A\* (anytime)
- ▶ heuristic: FF heuristic and landmark heuristic (inadmissible)
- ▶ other aspects: preferred operators; deferred heuristic evaluation; multi-queue search

↪ still one of the leading satisficing planners;  
winner of IPC 2008 and IPC 2011 (satisficing tracks)

## Planning Systems: Fast Downward Stone Soup

### Fast Downward Stone Soup (Helmert et al., 2011)

- ▶ problem class: optimal
- ▶ algorithm class: (portfolio of) explicit search
- ▶ search direction: forward search
- ▶ search algorithm: A\*
- ▶ heuristic: LM-cut; merge-and-shrink; landmarks; blind (admissible)

↪ winner of IPC 2011 (optimal track)

## Planning Systems: SymBA\*

### SymBA\* (Torralba, 2015)

- ▶ problem class: optimal
- ▶ algorithm class: symbolic search
- ▶ symbolic data structure: BDDs
- ▶ search direction: bidirectional
- ▶ search algorithm: mixture of (symbolic) Dijkstra and A\*
- ▶ heuristic: perimeter abstractions/blind

↪ winner of IPC 2014 (optimal track)

## B1.6 Summary



# Summary

big three classes of algorithms for classical planning:

- ▶ **explicit search**
  - ▶ **design choices:** search direction, search algorithm, search control (incl. heuristics)
- ▶ **SAT planning**
  - ▶ **design choices:** SAT encoding, SAT solver, evaluation strategy
- ▶ **symbolic search**
  - ▶ **design choices:** symbolic data structure
    - + same ones as for explicit search