Planning and Optimization G4. Heuristics for Probabilistic Planning

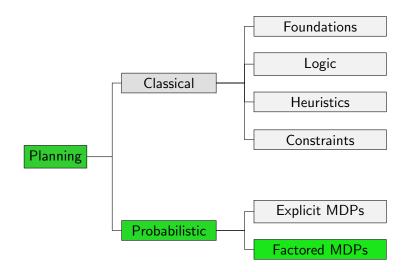
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December 9, 2019

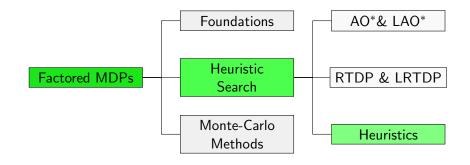
Motivation Determi			Summary
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Content of this Course





Content of this Course: Factored MDPs



Motivation	
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Determinization 0000000 Properties

Summary 00

Motivation

Heuristics

Heuristics for probabilistic planning

- most heuristics are based on domain-specific knowledge
- for a long time, determinization-based heuristics were the only notable domain-independent solution
- Recent progress: occupation measures (only covered in exercises)

Determinization ••••••

Properties

Summary 00

Determinization

What is a Determinization?

- Replace SSP operators with deterministic operators
- Results in classical planning task
- For SSPs, this is a classical planning task
- SSP and its determinization are related but not equivalent

How to Come up with a Determinization?

Typically, two types of determinization are distinguished:

- All-outcomes determinization
 - Create one deterministic transition to each outcome
- Single-outcome determinization
 - Pick one outcome of each probabilistic transition ...
 - ... and turn it into a deterministic transition
 - often, the most likely outcome is preserved
 - or one outcome is sampled according to its probability

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All-outcomes Determinizion

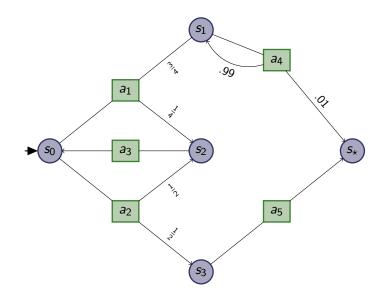
Definition (All-outcomes Determinization)

Let $\mathcal{T} = \langle S, L, c, T, s_0, S_* \rangle$ be an SSP. The all-outcomes determinization of T is the (deterministic) transition system $\mathcal{T}^d = \langle S, L^d, c, T^d, s_0, S_* \rangle$ with

$$L^{d} = \{ \langle s, \ell, s' \rangle \mid s, s' \in S, \ell \in L \text{ and } T(s, \ell, s') > 0 \}$$
$$T^{d} = \{ \langle s, \ell^{d}, s' \rangle \mid \ell^{d} = \langle s, \ell, s' \rangle \in L^{d} \}.$$



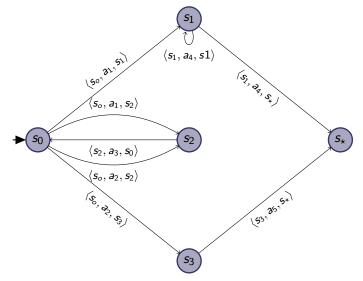
All-outcomes Determinization: (Unit-cost) Example





All-outcomes Determinization: (Unit-cost) Example

Generate one action for each outcome



Single-outcome Determinization

Definition (Single-outcome Determinization)

Let $\mathcal{T} = \langle \textit{S},\textit{L},\textit{c},\textit{T},\textit{s}_{0},\textit{S}_{\star} \rangle$ be an SSP and let

$$L^{aod} = \{ \langle s, \ell, s' \rangle \mid s, s' \in S, \ell \in L \text{ and } T(s, \ell, s') > 0 \}.$$

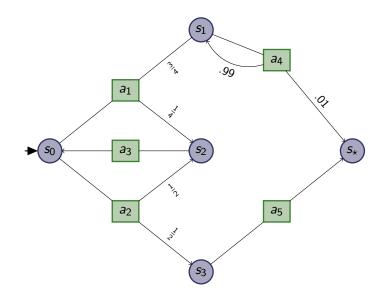
A (deterministic) transition system $T^d = \langle S, L^d, c, T^d, s_0, S_\star \rangle$ is a single-outcome determinization of T if

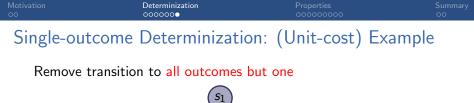
• $L^d \subseteq L^{aod}$ s.t. for all $s \in S$ and $\ell \in L(s)$ there is exactly one $\langle s, \ell, s' \rangle \in L^d$ and

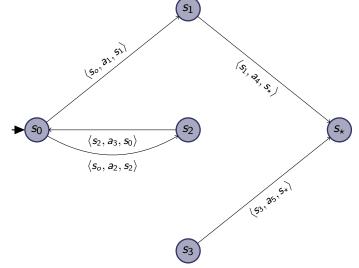
$$T^{d} = \{ \langle s, \ell^{d}, s' \rangle \mid \ell^{d} = \langle s, \ell, s' \rangle \in L^{d} \}$$



Single-outcome Determinization: (Unit-cost) Example







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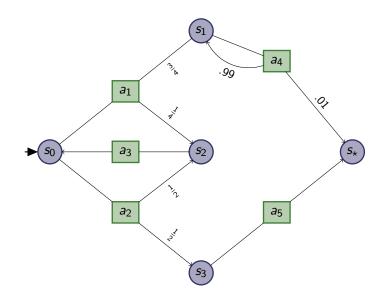
Properties

Single-outcome Determinization: Properties

- single-outcome determinizations are not well-suited to be used as a heuristic:
 - can be inadmissible
 - and even unsafe



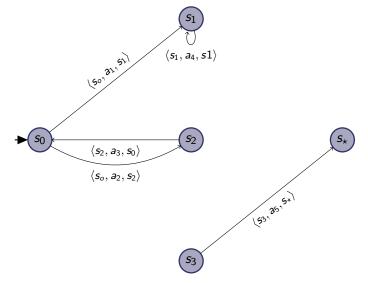
Single-outcome Determinization: Inadmissibility





Single-outcome Determinization: Inadmissibility

Remove transition to all outcomes but one



Single-outcome Determinization: Properties

- single-outcome determinizations are not well-suited to be used as a heuristic:
 - can be inadmissible
 - and even unsafe
- often part of domain-specific solutions

(e.g., by ignoring that some action may "fail")

 and as part of algorithms that average over several samples (Chapter G5)

Determinization	Properties	
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Min-min Heuristic

Definition (Min-min Heuristic)

Let \mathcal{T} be an SSP and let \mathcal{T}^d be the all-outcomes determinization of \mathcal{T} . The min-min heuristic h_{\min} maps each state $s \in S$ to the cost of the cheapest path from s to a goal state in \mathcal{T}^d .

Motivation	Determinization	Properties	Summary
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Min-min He	euristic: Admissibility		

Theorem (Admissibility)

The min-min heuristic is admissible.

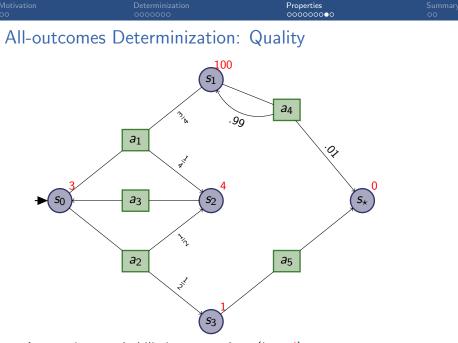
Proof Sketch.

$$V^{\star}(s) \stackrel{(1)}{=} \min_{\ell \in L(s)} c(\ell) + \sum_{s' \in S} T(s, \ell, s') \cdot V^{\star}(s')$$
$$\stackrel{(2)}{=} \min_{\ell \in L(s)} c(\ell) + \sum_{s' \in \operatorname{succ}(s, \ell)} T(s, \ell, s') \cdot V^{\star}(s')$$
$$\stackrel{(3)}{\geq} \min_{\ell \in L(s)} c(\ell) + \min_{s' \in \operatorname{succ}(s, \ell)} V^{\star}(s') = h_{\min}(s)$$

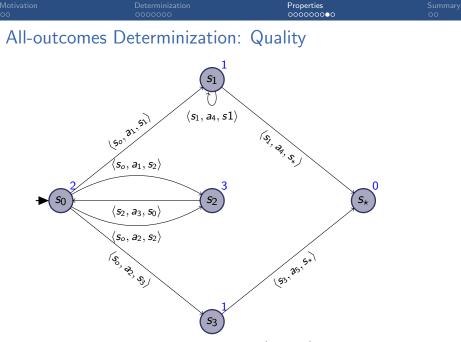
(1) is the Bellman equation, (2) holds because $T(s, \ell, s') = 0$ for all $s' \notin \operatorname{succ}(s, \ell)$ and (3) because the weight from more expensive outcomes is shifted to the cheapest one.

Min-min Heuristic: Properties

- The min-min heuristic is also called the optimistic heuristic ...
- ... because the planner may choose its preferred outcome
- Min-min heuristic can be well informed
- ... but can also be utterly optimistic



Annotation: probabilistic state-values (in red)



Annotation: deterministic state-values (in blue)

Min-min Heuristic: Properties

- The min-min heuristic is also called the optimistic heuristic ...
- ... because the planner may choose its preferred outcome
- Min-min heuristic can be well informed ...
- ... but can also be utterly optimistic
- Min-min heuristic often solvable in practice even if SSP is not
- If still unsolvable: compute classical heuristic of all-outcomes determinization

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Summary

Determinization	Summary
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Summary

- Almost all heuristics in probabilistic planning are either domain-specific or based on a determinization
- A single-outcome determinization removes all outcomes from a transition except for one
- The all-outcomes determinization creates a deterministic transition for each outcome
- The min-min heuristic computes the shortest path in the all-outcomes determinization
- The min-min heuristic is admissible