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N. Helmert, T. Keller (Universität Basel) Pla	anning and Optimization	October 9, 2019	2 / 28









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SAT Formula: Operator Selection

Let $O = \{o_1, ..., o_n\}.$

SAT Formula: Operator Selection operator selection clauses:

•
$$o_1^i \lor \cdots \lor o_n^i$$
 for all $1 \le i \le T$

operator exclusion clauses:

• $\neg o_i^i \lor \neg o_k^i$ for all $1 \le i \le T$, $1 \le j < k \le n$

M. Helmert, T. Keller (Universität Basel)



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B5. SAT Planning: Core Idea and Sequential Encoding

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B5. SAT Planning: Core Idea and Sequential Encoding Simplifications and Abbreviations • Let us pick the last formula apart to understand it better (and also get a CNF representation along the way). • Let us call the formula τ ("transition"): $\tau = o^i \rightarrow (v^i \leftrightarrow regr(v, eff(o))^{i-1}).$ • First, some abbreviations: • Let e = eff(o). • Let e = eff(o). • Let $\rho = regr(v, e)$ ("regression"). We have $\rho = effcond(v, e) \lor (v \land \neg effcond(\neg v, e)).$ • Let $\delta = effcond(v, e)$ ("deleted"). • $\tau = o^i \rightarrow (v^i \leftrightarrow \rho^{i-1})$ with $\rho = \alpha \lor (v \land \neg \delta)$

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Transitions



Reminder: $\tau_1 = o^i \to (v^i \to \rho^{i-1})$ with $\rho = \alpha \lor (v \land \neg \delta)$ $\tau_1 = o^i \rightarrow (v^i \rightarrow o^{i-1})$ $\equiv o^i \rightarrow (\neg \rho^{i-1} \rightarrow \neg v^i)$ $\equiv (o^i \wedge \neg o^{i-1}) \rightarrow \neg v^i$ $\equiv (o^{i} \land \neg (\alpha^{i-1} \lor (v^{i-1} \land \neg \delta^{i-1}))) \to \neg v^{i}$ $\equiv (o^{i} \land (\neg \alpha^{i-1} \land (\neg \gamma^{i-1} \lor \delta^{i-1}))) \rightarrow \neg \gamma^{i}$ $\equiv \underbrace{((o^{i} \land \neg \alpha^{i-1} \land \neg v^{i-1}) \to \neg v^{i})}_{\tau_{11}} \land \underbrace{((o^{i} \land \neg \alpha^{i-1} \land \delta^{i-1}) \to \neg v^{i})}_{\tau_{12}}$ \rightarrow consider this two separate constraints τ_{11} and τ_{12} M. Helmert, T. Keller (Universität Basel) Planning and Optimization October 9, 2019 22 / 28 B5. SAT Planning: Core Idea and Sequential Encoding

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Picking it Apart (2)

Picking it Apart (3) Almost done! $\tau_{12} = (o^i \wedge \neg \alpha^{i-1} \wedge \delta^{i-1}) \rightarrow \neg v^i$ "When applying o, if o deletes v and does not add it, it is false afterwards." (Note the add-after-delete semantics.) called negative effect clause \blacktriangleright in clause form: $\neg o^i \lor \alpha^{i-1} \lor \neg \delta^{i-1} \lor \neg v^i$ For STRIPS tasks, these are indeed clauses. (And in general?) Planning and Optimization October 9, 2019 23 / 28 M. Helmert, T. Keller (Universität Basel)



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Summary

B5.5 Summary

SAT Formula: Transitions

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SAT Formula: Transitions			
precondition clauses:			
• $\neg o^i \lor pre(o)^{i-1}$	for all $1 \leq i \leq T$, $o \in O$		
positive and negative effect claus	ses:		
$\blacktriangleright \neg o^i \lor \neg \alpha^{i-1} \lor v^i$	for all $1 \leq i \leq T$, $o \in O$, $v \in V$		
$\blacktriangleright \neg o^i \lor \alpha^{i-1} \lor \neg \delta^{i-1} \lor \neg v^i$	for all $1 \leq i \leq T$, $o \in O$, $v \in V$		
positive and negative frame claus	ses:		
$\blacktriangleright \neg o^i \lor \neg v^{i-1} \lor \delta^{i-1} \lor v^i$	for all $1 \leq i \leq T$, $o \in O$, $v \in V$		
	for all $1 \leq i \leq T$, $o \in O$, $v \in V$		
where $\alpha = effcond(v, eff(o))$, $\delta = effcond(\neg v, eff(o))$.			
For STRIPS, all except the preco	ondition clauses are in clause form.		
The precondition clauses are easi	ily convertible to CNF		
(one clause $\neg o^i \lor v^{i-1}$ for each	precondition atom v of o).		
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Summar

B5. SAT Planning: Core Idea and Sequential Encoding

Summary

- **SAT** planning (planning as satisfiability) expresses a sequence of bounded-horizon planning tasks as SAT formulas.
- Plans can be extracted from satisfying assignments; unsolvable tasks are challenging for the algorithm.
- ▶ For each time step, there are propositions encoding which state variables are true and which operators are applied.
- ► We describe a basic sequential encoding where one operator is applied at every time step.
- The encoding produces a CNF formula for STRIPS tasks.
- ▶ The encoding follows naturally (with some work) from using regression to link state variables in adjacent time steps.

Transitions