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B2. Progression and Regression Search

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B2.1 Introduction

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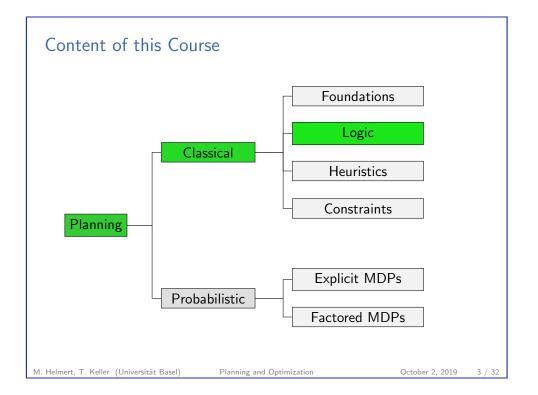
B2.4 Regression for STRIPS Tasks

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B2. Progression and Regression Search

Introduction

B2.1 Introduction

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B2. Progression and Regression Search

Search Direction

Search direction

- one dimension for classifying search algorithms
- forward search from initial state to goal based on progression
- backward search from goal to initial state based on regression
- bidirectional search

In this chapter we look into progression and regression planning.

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B2. Progression and Regression Search

Progression

B2.2 Progression

B2. Progression and Regression Search

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Reminder: Interface for Heuristic Search Algorithms

Abstract Interface Needed for Heuristic Search Algorithms

► init()

▶ is_goal(s)

 \rightsquigarrow tests if s is a goal state

 \triangleright succ(s)

 \rightsquigarrow returns all pairs $\langle a, s' \rangle$ with $s \stackrel{a}{\rightarrow} s'$

► cost(a)

 \rightarrow returns cost of action a

ightharpoonup h(s)

 \rightsquigarrow returns heuristic value for state s

B2. Progression and Regression Search

Planning by Forward Search: Progression

Progression: Computing the successor state s[o] of a state swith respect to an operator o.

Progression planners find solutions by forward search:

- start from initial state
- iteratively pick a previously generated state and progress it through an operator, generating a new state
- solution found when a goal state generated

pro: very easy and efficient to implement

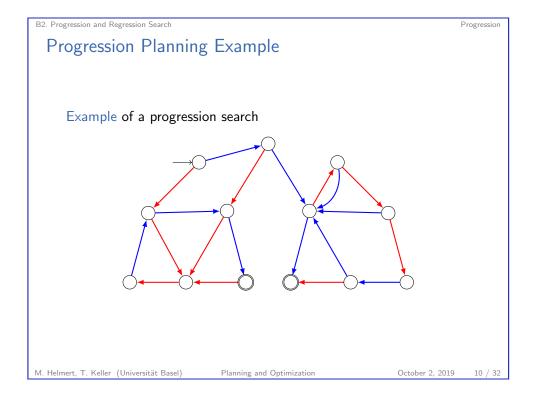
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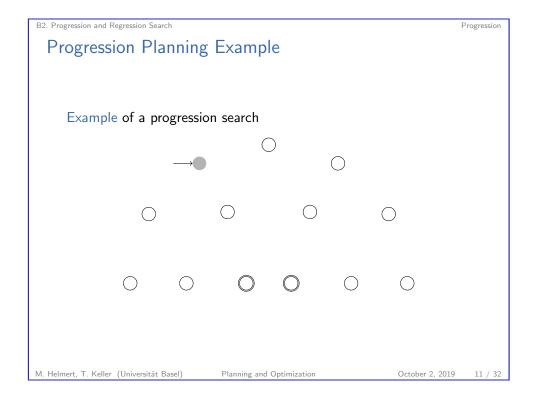
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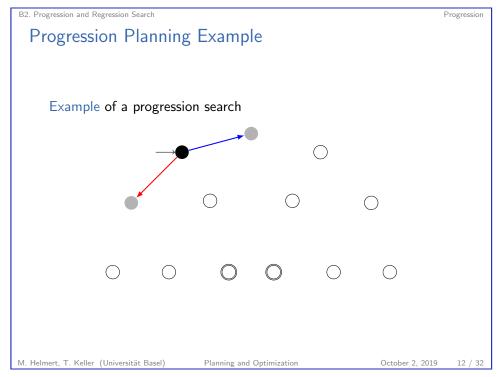
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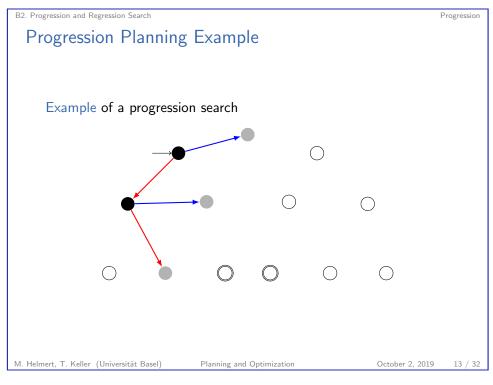
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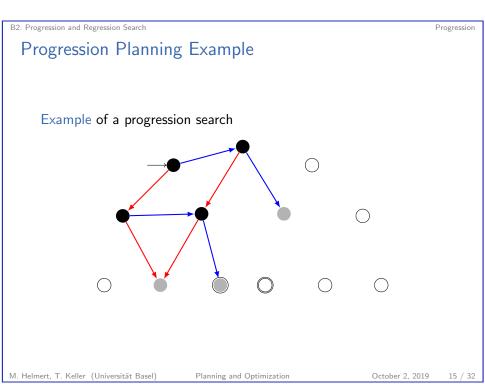
B2. Progression and Regression Search Search Space for Progression Search Space for Progression search space for progression in a planning task $\Pi = \langle V, I, O, \gamma \rangle$ (search states are world states s of Π ; actions of search space are operators $o \in O$) ▶ init() \rightsquigarrow returns I▶ is_goal(s) \rightsquigarrow tests if $s \models \gamma$ \triangleright succ(s) \rightsquigarrow returns all pairs $\langle o, s \llbracket o \rrbracket \rangle$ where $o \in O$ and o is applicable in s▶ cost(o) \rightsquigarrow returns cost(o) as defined in Π \rightsquigarrow estimates cost from s to γ (\rightsquigarrow Parts C-F) ► h(s) M. Helmert, T. Keller (Universität Basel) Planning and Optimization October 2, 2019

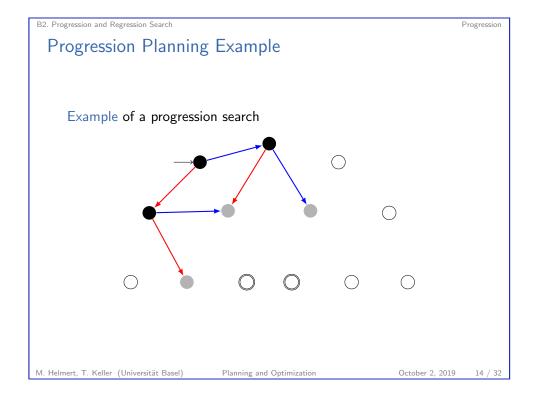


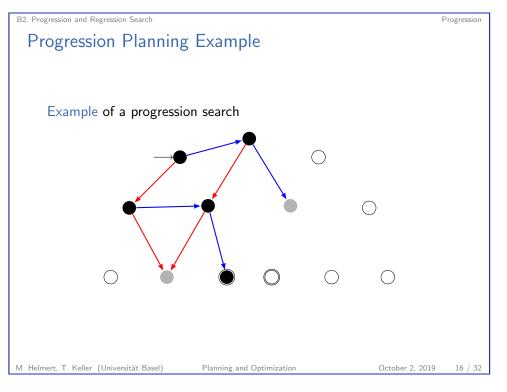












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B2.3 Regression

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B2. Progression and Regression Search

Regression

Forward Search vs. Backward Search

Searching planning tasks in forward vs. backward direction is not symmetric:

- forward search starts from a single initial state; backward search starts from a set of goal states
- ▶ when applying an operator o in a state s in forward direction, there is a unique successor state s'; if we just applied operator o and ended up in state s', there can be several possible predecessor states s
- → in most natural representation for backward search in planning, each search state corresponds to a set of world states

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B2. Progression and Regression Search

Regression

Planning by Backward Search: Regression

Regression: Computing the possible predecessor states regr(S', o) of a set of states S' ("subgoal") given the last operator o that was applied.

→ formal definition in next chapter

Regression planners find solutions by backward search:

- start from set of goal states
- ► iteratively pick a previously generated subgoal (state set) and regress it through an operator, generating a new subgoal
- > solution found when a generated subgoal includes initial state

pro: can handle many states simultaneously

con: basic operations complicated and expensive

B2. Progression and Regression Search

Regression

Search Space Representation in Regression Planners

identify state sets with logical formulas (again):

- each search state corresponds to a set of world states ("subgoal")
- ▶ each search state is represented by a logical formula: φ represents $\{s \in S \mid s \models \varphi\}$
- many basic search operations like detecting duplicates are NP-complete or coNP-complete

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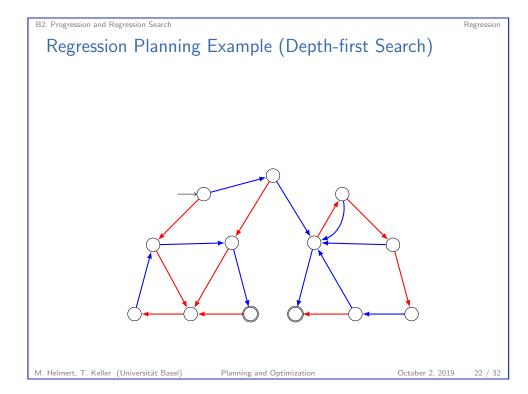
B2. Progression and Regression Search Search Space for Regression Search Space for Regression search space for regression in a planning task $\Pi = \langle V, I, O, \gamma \rangle$ (search states are formulas φ describing sets of world states; actions of search space are operators $o \in O$) ▶ init() \rightsquigarrow returns γ ▶ is_goal(φ) \rightsquigarrow tests if $I \models \varphi$ ightharpoonup succ(φ) \rightsquigarrow returns all pairs $\langle o, regr(\varphi, o) \rangle$ where $o \in O$ and $regr(\varphi, o)$ is defined ▶ cost(o) \rightsquigarrow returns cost(o) as defined in Π

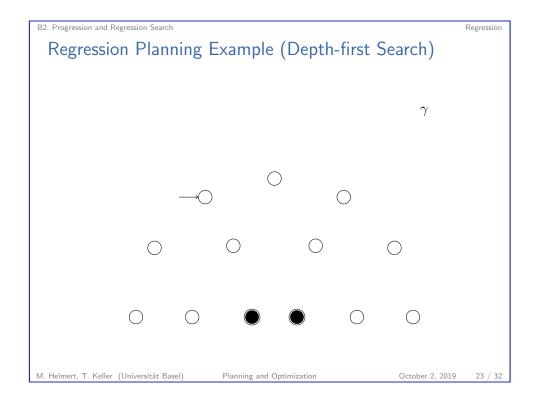
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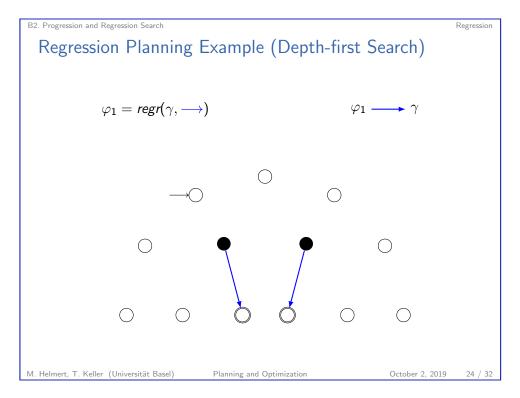
 $ightharpoonup h(\varphi)$

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 \rightsquigarrow estimates cost from I to φ (\rightsquigarrow Parts C–F)



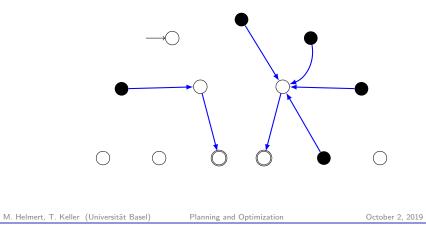




Regression

Regression Planning Example (Depth-first Search)

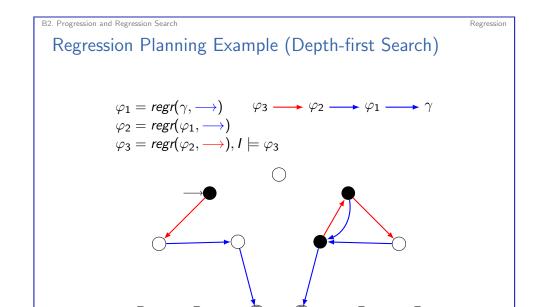
$$\varphi_1 = regr(\gamma, \longrightarrow) \qquad \qquad \varphi_2 \longrightarrow \varphi_1 \longrightarrow \varphi_2 = regr(\varphi_1, \longrightarrow)$$



B2. Progression and Regression Search

Regression for STRIPS Tasks

B2.4 Regression for STRIPS Tasks



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Regression for STRIPS Tasks

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Regression for STRIPS Planning Tasks

Regression for STRIPS planning tasks is much simpler than the general case:

- Consider subgoal φ that is conjunction of atoms $a_1 \wedge \cdots \wedge a_n$ (e.g., the original goal γ of the planning task).
- First step: Choose an operator o that deletes no a_i.
- **Second step**: Remove any atoms added by o from φ .
- ▶ Third step: Conjoin pre(o) to φ .
- Outcome of this is regression of φ w.r.t. o. It is again a conjunction of atoms.

optimization: only consider operators adding at least one ai

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Regression for STRIPS Tasks

STRIPS Regression

Definition (STRIPS Regression)

Let $\varphi = \varphi_1 \wedge \cdots \wedge \varphi_n$ be a conjunction of atoms, and let o be a STRIPS operator which adds the atoms a_1, \ldots, a_k and deletes the atoms d_1, \ldots, d_l .

The STRIPS regression of φ with respect to o is

$$\mathit{sregr}(\varphi, o) := egin{cases} \bot & \mathsf{if} \ arphi_i = d_j \ \mathsf{for} \ \mathsf{some} \ i, j \ pre(o) \land \bigwedge (\{\varphi_1, \ldots, \varphi_n\} \setminus \{a_1, \ldots, a_k\}) \ \ \ \mathsf{else} \end{cases}$$

Note: $sregr(\varphi, o)$ is again a conjunction of atoms, or \bot .

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B2. Progression and Regression Search

B2.5 Summary

B2. Progression and Regression Search

Regression for STRIPS Tasks

Does this Capture the Idea of Regression?

For our definition to capture the concept of regression, it must have the following property:

Regression Property

For all sets of states described by a conjunction of atoms φ , all states s and all STRIPS operators o,

$$s \models sregr(\varphi, o)$$
 iff $s[o] \models \varphi$.

This is indeed true. We do not prove it now because we prove this property for general regression (not just STRIPS) later.

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Summar

Summary

- ▶ Progression search proceeds forward from the initial state.
- ▶ In progression search, the search space is identical to the state space of the planning task.
- ▶ Regression search proceeds backwards from the goal.
- ► Each search state corresponds to a set of world states, for example represented by a formula.
- ► Regression is simple for **STRIPS** operators.
- ► The theory for general regression is more complex. This is the topic of the following chapters.

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