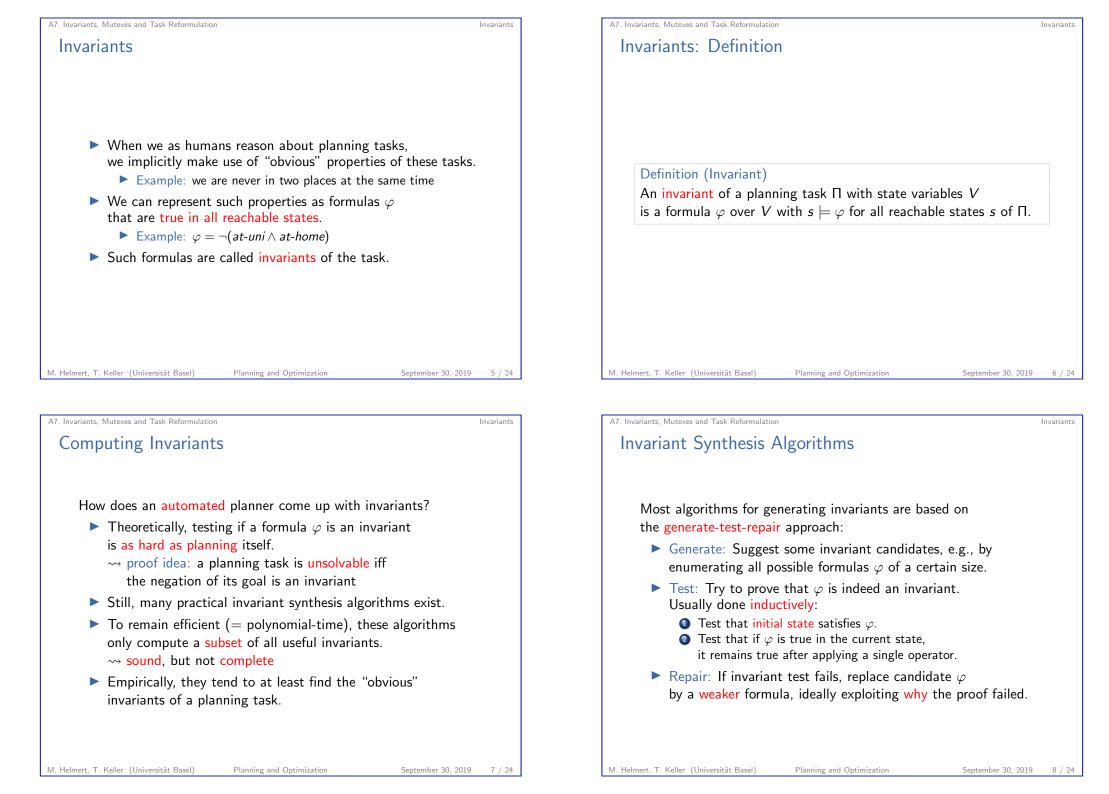


| Planning and Optimiz<br>September 30, 2019 — A7. Inva |                           | formulation        |        |
|-------------------------------------------------------|---------------------------|--------------------|--------|
| A7.1 Invariants                                       |                           |                    |        |
| A7.2 Mutexes                                          |                           |                    |        |
| A7.3 Reformulation                                    | n                         |                    |        |
| A7.4 Summary                                          |                           |                    |        |
|                                                       |                           |                    |        |
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## Invariant Synthesis: References

We will not cover invariant synthesis algorithms in this course.

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#### Literature on invariant synthesis:

- DISCOPLAN (Gerevini & Schubert, 1998)
- TIM (Fox & Long, 1998)
- Edelkamp & Helmert's algorithm (1999)
- Bonet & Geffner's algorithm (2001)
- Rintanen's algorithm (2008)

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Mutexes

Invariant

A7.2 Mutexes

# A7. Invariants. Mutexes and Task Reformulation

# **Exploiting Invariants**

Invariants have many uses in planning:

- ► Regression search: Prune subgoals that violate (are inconsistent with) invariants.
- ▶ Planning as satisfiability: Add invariants to a SAT encoding of a planning task to get tighter constraints.
- Proving unsolvability: If  $\varphi$  is an invariant such that  $\varphi \wedge \gamma$  is unsatisfiable,

the planning task with goal  $\gamma$  is unsolvable.

► Finite-Domain Reformulation:

Derive a more compact FDR representation (equivalent, but with fewer states) from a given propositional planning task.

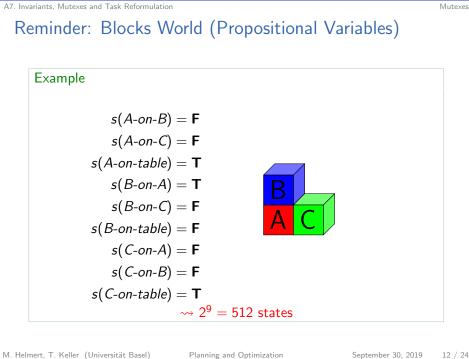
We now discuss the last point because it connects to our discussion of propositional vs. FDR planning tasks.

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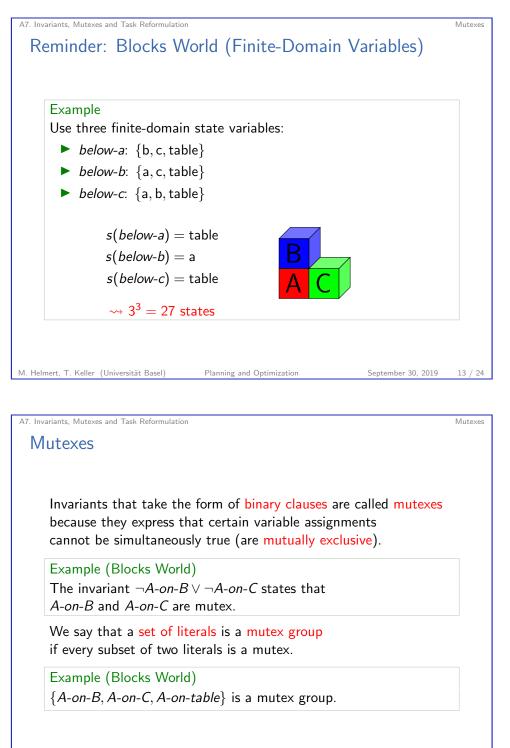
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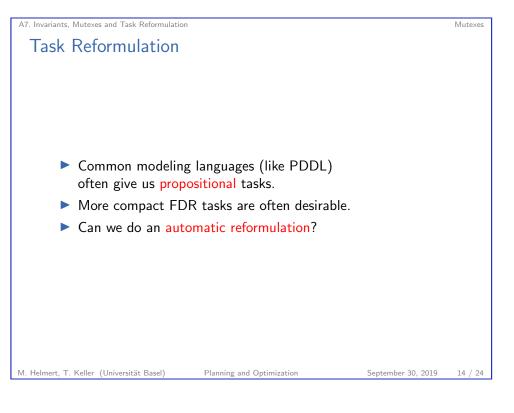
Invariants

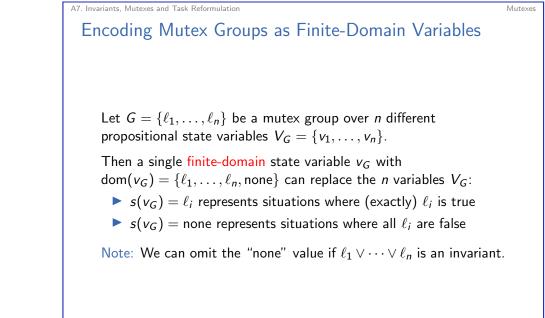


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|------------------------------------------------|---|
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#### **Mutex Covers**

Mutexes

#### Definition (Mutex Cover)

A mutex cover for a propositional planning task  $\Pi$  is a set of mutex groups  $\{G_1, \ldots, G_n\}$  where each variable of  $\Pi$  occurs in exactly one group  $G_i$ .

A mutex cover is positive if all literals in all groups are positive.

Note: always exists (use trivial group  $\{v\}$  if v otherwise uncovered)

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Reformulation

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# A7.3 Reformulation

A7. Invariants, Mutexes and Task Reformulation

## Positive Mutex Covers

In the following, we stick to positive mutex covers for simplicity.

If we have  $\neg v$  in *G* for some group *G* in the cover, we can reformulate the task to use an "opposite" variable  $\hat{v}$  instead, as in the conversion to positive normal form (Chapter A6).

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# A7. Invariants, Mutexes and Task Reformulation Reformulation

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# Mutex-Based Reformulation of Propositional Tasks

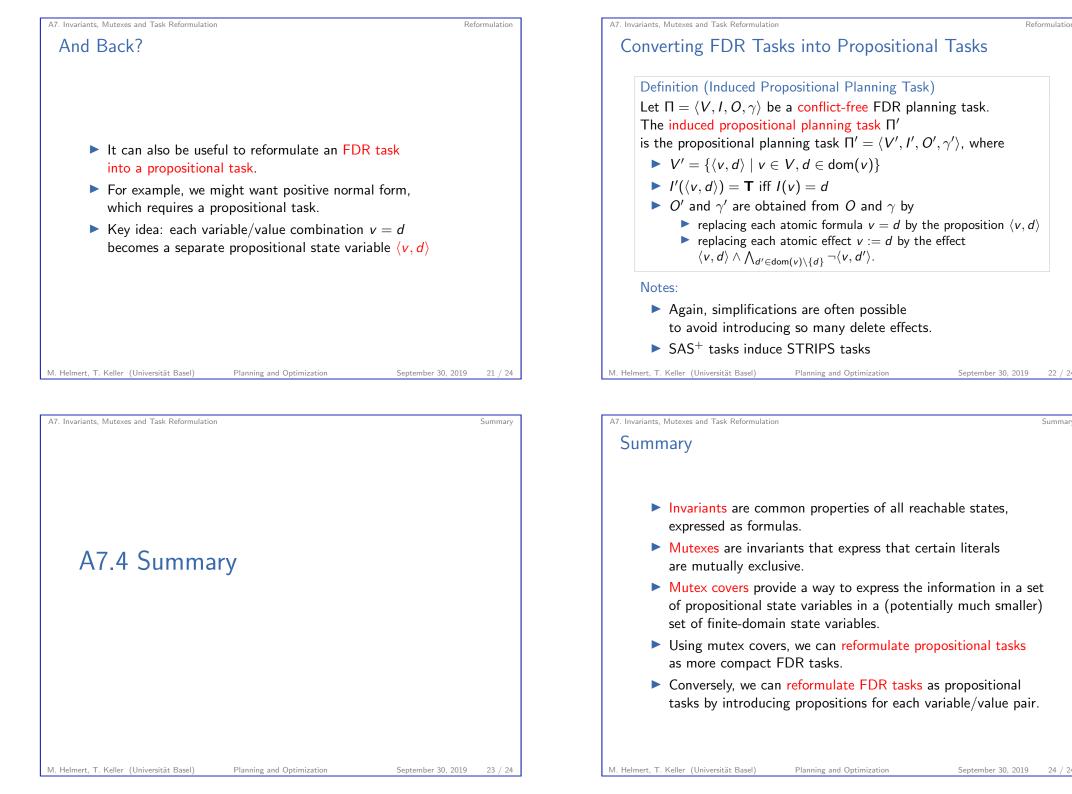
Given a conflict-free propositional planning task  $\Pi$  with positive mutex cover  $\{G_1, \ldots, G_n\}$ :

- ▶ In all conditions where variable  $v \in G_i$  occurs, replace v with  $v_{G_i} = v$ .
- ▶ In all effects *e* where variable  $v \in G_i$  occurs,
  - Replace all atomic add effects v with  $v_{G_i} := v$
  - Replace all atomic delete effects  $\neg v$  with

 $(v_{G_i} = v \land \neg \bigvee_{v' \in G_i \setminus \{v\}} \mathit{effcond}(v', e)) \rhd v_{G_i} := \mathsf{none}$ 

This results in an FDR planning task  $\Pi'$  that is equivalent to  $\Pi$  (without proof).

Note: the conditional effects can often be simplified away to an unconditional or empty effect.



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Summar

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