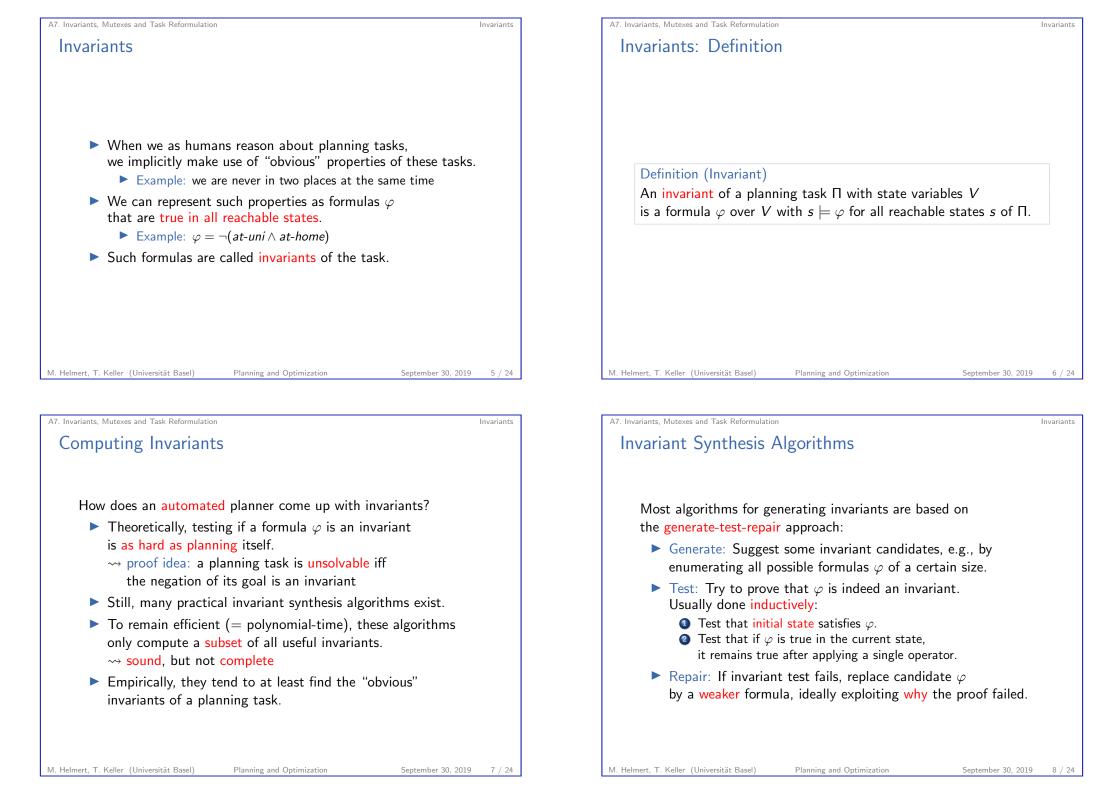


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A7.1 Invariants			
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Invariant Synthesis: References

We will not cover invariant synthesis algorithms in this course.

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Literature on invariant synthesis:

- DISCOPLAN (Gerevini & Schubert, 1998)
- TIM (Fox & Long, 1998)
- Edelkamp & Helmert's algorithm (1999)
- Bonet & Geffner's algorithm (2001)
- Rintanen's algorithm (2008)

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Mutexes

Invariant

A7.2 Mutexes

A7. Invariants. Mutexes and Task Reformulation

Exploiting Invariants

Invariants have many uses in planning:

- ► Regression search: Prune subgoals that violate (are inconsistent with) invariants.
- ▶ Planning as satisfiability: Add invariants to a SAT encoding of a planning task to get tighter constraints.
- Proving unsolvability: If φ is an invariant such that $\varphi \wedge \gamma$ is unsatisfiable,

the planning task with goal γ is unsolvable.

► Finite-Domain Reformulation:

Derive a more compact FDR representation (equivalent, but with fewer states) from a given propositional planning task.

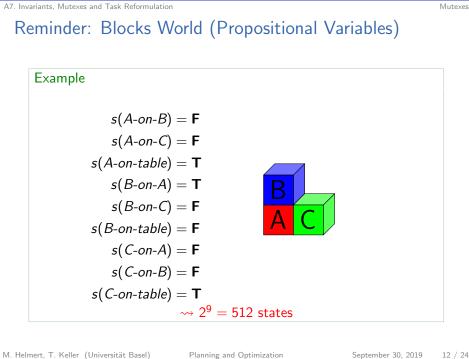
We now discuss the last point because it connects to our discussion of propositional vs. FDR planning tasks.

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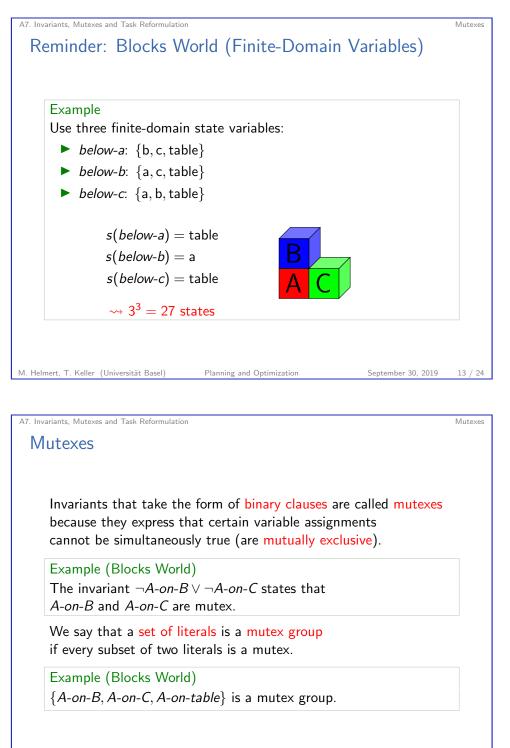
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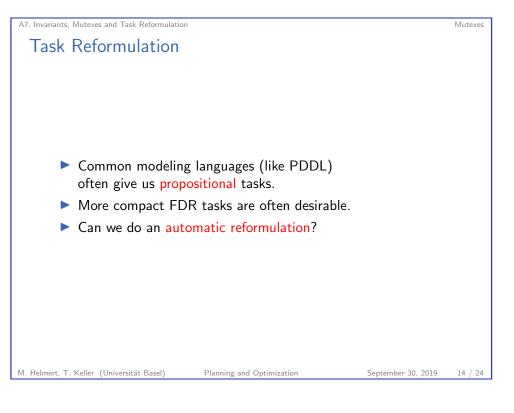
Invariants

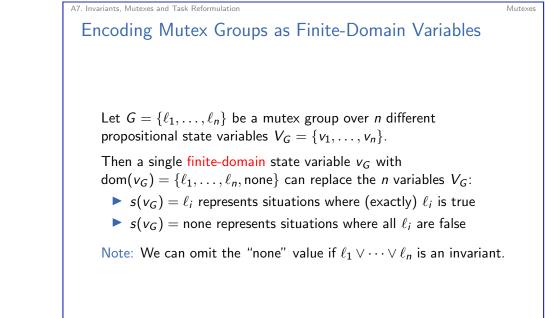


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Mutex Covers

Mutexes

Definition (Mutex Cover)

A mutex cover for a propositional planning task Π is a set of mutex groups $\{G_1, \ldots, G_n\}$ where each variable of Π occurs in exactly one group G_i .

A mutex cover is positive if all literals in all groups are positive.

Note: always exists (use trivial group $\{v\}$ if v otherwise uncovered)

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Reformulation

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A7.3 Reformulation

A7. Invariants, Mutexes and Task Reformulation

Positive Mutex Covers

In the following, we stick to positive mutex covers for simplicity.

If we have $\neg v$ in *G* for some group *G* in the cover, we can reformulate the task to use an "opposite" variable \hat{v} instead, as in the conversion to positive normal form (Chapter A6).

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A7. Invariants, Mutexes and Task Reformulation Reformulation

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Mutex-Based Reformulation of Propositional Tasks

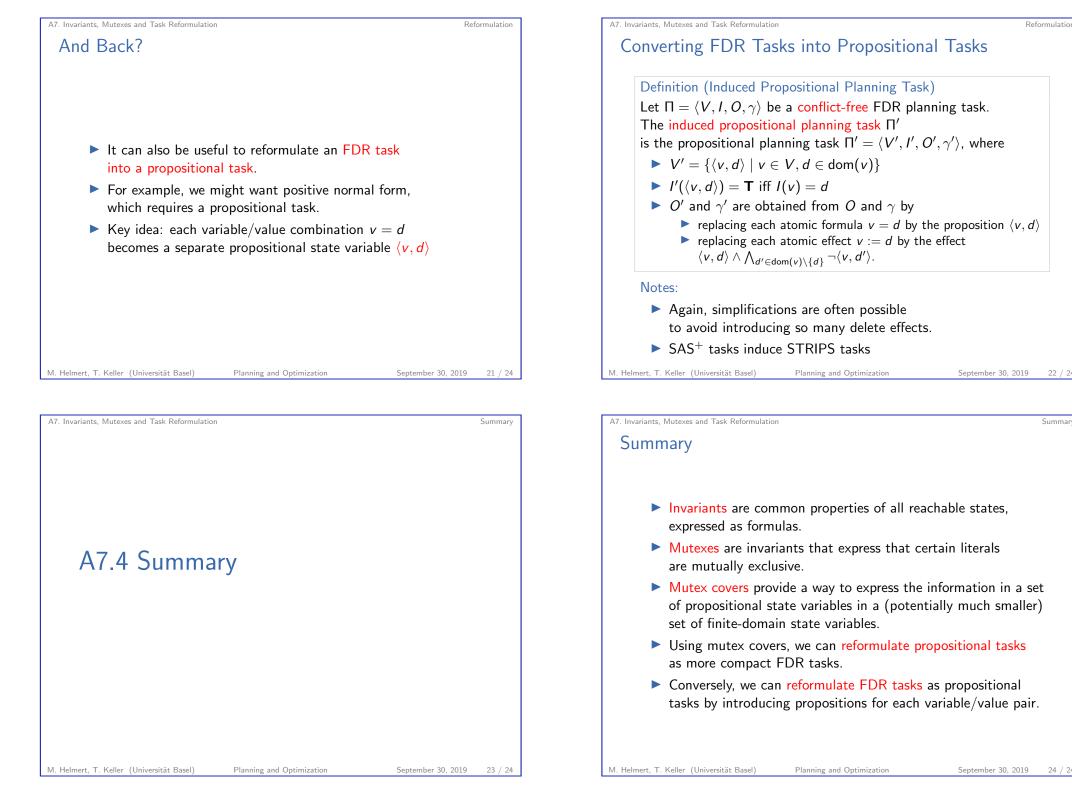
Given a conflict-free propositional planning task Π with positive mutex cover $\{G_1, \ldots, G_n\}$:

- ▶ In all conditions where variable $v \in G_i$ occurs, replace v with $v_{G_i} = v$.
- ▶ In all effects *e* where variable $v \in G_i$ occurs,
 - Replace all atomic add effects v with $v_{G_i} := v$
 - Replace all atomic delete effects $\neg v$ with

 $(v_{G_i} = v \land \neg \bigvee_{v' \in G_i \setminus \{v\}} \mathit{effcond}(v', e)) \rhd v_{G_i} := \mathsf{none}$

This results in an FDR planning task Π' that is equivalent to Π (without proof).

Note: the conditional effects can often be simplified away to an unconditional or empty effect.



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Summar

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