## Planning and Optimization A6. Positive Normal Form, STRIPS and SAS+

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A6.1 Motivation

A6.2 Positive Normal Form

A6.3 STRIPS

A6.4 SAS<sup>+</sup>

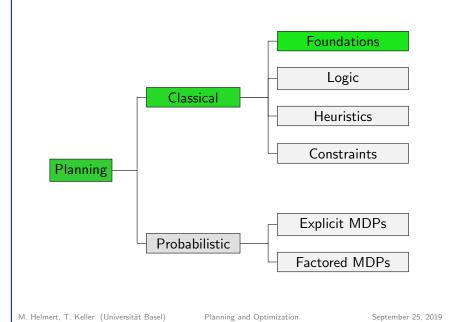
A6.5 Summary

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A6. Positive Normal Form, STRIPS and SAS

Motivation

A6.1 Motivation

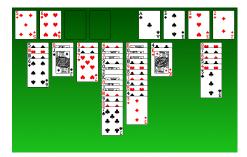
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## Example: Freecell



Example (Good and Bad Effects)

If we move  $K\diamondsuit$  to a free tableau position, the good effect is that  $4\clubsuit$  is now accessible.

The bad effect is that we lose one free tableau position.

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Question: Which operator effects are good, and which are bad?

We now consider a reformulation of propositional planning tasks that makes the distinction between good and bad effects obvious.

Difficult to answer in general, because it depends on context:

Locking our door is good if we want to keep burglars out.

Locking our door is bad if we want to enter.

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Positive Normal Form

# A6.2 Positive Normal Form

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A6. Positive Normal Form, STRIPS and SAS

What is a Good or Bad Effect?

Positive Normal Form

#### Positive Formulas, Operators and Tasks

#### Definition (Positive Formula)

A logical formula  $\varphi$  is positive if no negation symbols appear in  $\varphi$ .

Note: This includes the negation symbols implied by  $\rightarrow$  and  $\leftrightarrow$ .

#### Definition (Positive Operator)

An operator o is positive if pre(o) and all effect conditions in eff(o) are positive.

#### Definition (Positive Propositional Planning Task)

A propositional planning task  $\langle V, I, O, \gamma \rangle$  is positive if all operators in O and the goal  $\gamma$  are positive.

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Positive Normal Form

#### Positive Normal Form

#### Definition (Positive Normal Form)

A propositional planning task is in positive normal form if it is positive and all operator effects are flat.

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#### Positive Normal Form

#### Positive Normal Form: Existence

#### Theorem (Positive Normal Form)

For every propositional planning task  $\Pi$ , there is an equivalent propositional planning task  $\Pi'$  in positive normal form. Moreover,  $\Pi'$  can be computed from  $\Pi$  in polynomial time.

Note: Equivalence here means that the transition systems induced by  $\Pi$  and  $\Pi'$ , restricted to the reachable states, are isomorphic.

We prove the theorem by describing a suitable algorithm. (However, we do not prove its correctness or complexity.)

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Positive Normal Form

#### Positive Normal Form: Algorithm

#### Transformation of $\langle V, I, O, \gamma \rangle$ to Positive Normal Form

Replace all operators with equivalent conflict-free operators. Convert all conditions to negation normal form (NNF). **while** any condition contains a negative literal  $\neg v$ :

Let  $\nu$  be a variable which occurs negatively in a condition.

 $V:=V\cup\{\hat{v}\}$  for some new propositional state variable  $\hat{v}$ 

$$I(\hat{v}) := \begin{cases} \mathbf{F} & \text{if } I(v) = \mathbf{T} \\ \mathbf{T} & \text{if } I(v) = \mathbf{F} \end{cases}$$

Replace the effect v by  $(v \land \neg \hat{v})$  in all operators  $o \in O$ .

Replace the effect  $\neg v$  by  $(\neg v \land \hat{v})$  in all operators  $o \in O$ .

Replace  $\neg v$  by  $\hat{v}$  in all conditions.

Convert all operators  $o \in O$  to flat operators.

Here, all conditions refers to all operator preconditions, operator effect conditions and the goal.

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Positive Normal Form

## Positive Normal Form: Example

#### Example (Transformation to Positive Normal Form)

```
V = \{\textit{home}, \textit{uni}, \textit{lecture}, \textit{bike}, \textit{bike-locked}\}
```

$$I = \{ \textit{home} \mapsto \mathbf{T}, \textit{bike} \mapsto \mathbf{T}, \textit{bike-locked} \mapsto \mathbf{T},$$

$$\textit{uni} \mapsto \textbf{F}, \textit{lecture} \mapsto \textbf{F}\}$$

$$O = \{ \langle \textit{home} \land \textit{bike} \land \neg \textit{bike-locked}, \neg \textit{home} \land \textit{uni} \rangle,$$

$$\langle bike \wedge bike-locked, \neg bike-locked \rangle$$
,

$$\langle bike \wedge \neg bike\text{-locked}, bike\text{-locked} \rangle$$
,

$$\langle uni, lecture \land ((bike \land \neg bike-locked) \rhd \neg bike) \rangle \}$$

 $\gamma = lecture \wedge bike$ 

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#### Positive Normal Form: Example

```
Example (Transformation to Positive Normal Form)
   V = \{home, uni, lecture, bike, bike-locked\}
     I = \{ home \mapsto \mathbf{T}, bike \mapsto \mathbf{T}, bike-locked \mapsto \mathbf{T}, \}
             uni \mapsto \mathbf{F}, lecture \mapsto \mathbf{F}
   O = \{ \langle home \wedge bike \wedge \neg bike-locked, \neg home \wedge uni \rangle, \}
              \langle bike \wedge bike\text{-locked}, \neg bike\text{-locked} \rangle,
              \langle bike \wedge \neg bike-locked \rangle, bike-locked\rangle,
              \langle uni, lecture \land ((bike \land \neg bike-locked) \rhd \neg bike) \rangle \}
    \gamma = lecture \wedge bike
```

Identify state variable v occurring negatively in conditions.

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## Positive Normal Form: Example

```
Example (Transformation to Positive Normal Form)
   V = \{home, uni, lecture, bike, bike-locked, bike-unlocked\}
    I = \{ home \mapsto \mathbf{T}, bike \mapsto \mathbf{T}, bike-locked \mapsto \mathbf{T}, \}
            uni \mapsto \mathbf{F}, lecture \mapsto \mathbf{F}, bike-unlocked \mapsto \mathbf{F}
   O = \{ \langle home \wedge bike \wedge \neg bike\text{-locked}, \neg home \wedge uni \rangle, \}
             \langle bike \wedge bike-locked \rangle,
            \langle bike \wedge \neg bike\text{-locked} \rangle,
            \langle uni, lecture \land ((bike \land \neg bike-locked) \rhd \neg bike) \rangle \}
    \gamma = lecture \wedge bike
```

Introduce new variable  $\hat{v}$  with complementary initial value.

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Positive Normal Form

#### Positive Normal Form: Example

#### Example (Transformation to Positive Normal Form)

```
V = \{home, uni, lecture, bike, bike-locked, bike-unlocked\}
 I = \{ home \mapsto \mathbf{T}, bike \mapsto \mathbf{T}, bike-locked \mapsto \mathbf{T}, \}
          uni \mapsto \mathbf{F}, lecture \mapsto \mathbf{F}, bike-unlocked \mapsto \mathbf{F}}
O = \{ \langle home \wedge bike \wedge \neg bike\text{-locked}, \neg home \wedge uni \rangle, \}
          \langle bike \wedge bike-locked, \neg bike-locked \rangle,
          \langle bike \wedge \neg bike\text{-locked} \rangle,
          \langle uni, lecture \land ((bike \land \neg bike-locked) \rhd \neg bike) \rangle \}
\gamma = lecture \wedge bike
```

Identify effects on variable v.

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Positive Normal Form

## Positive Normal Form: Example

#### Example (Transformation to Positive Normal Form)

```
V = \{home, uni, lecture, bike, bike-locked, bike-unlocked\}
 I = \{ home \mapsto \mathbf{T}, bike \mapsto \mathbf{T}, bike-locked \mapsto \mathbf{T}, \}
          uni \mapsto \mathbf{F}, lecture \mapsto \mathbf{F}, bike-unlocked \mapsto \mathbf{F}}
O = \{ \langle home \wedge bike \wedge \neg bike\text{-locked}, \neg home \wedge uni \rangle, \}
          \langle bike \wedge bike\text{-locked}, \neg bike\text{-locked} \wedge bike\text{-unlocked} \rangle
          \langle bike \land \neg bike\text{-locked}, bike\text{-locked} \land \neg bike\text{-unlocked} \rangle
          \langle uni, lecture \land ((bike \land \neg bike-locked) \rhd \neg bike) \rangle \}
\gamma = lecture \wedge bike
```

Introduce complementary effects for  $\hat{v}$ .

#### Positive Normal Form: Example

## Example (Transformation to Positive Normal Form)

```
V = \{home, uni, lecture, bike, bike-locked, bike-unlocked\}
 I = \{ home \mapsto \mathbf{T}, bike \mapsto \mathbf{T}, bike-locked \mapsto \mathbf{T}, \}
          uni \mapsto \mathbf{F}, lecture \mapsto \mathbf{F}, bike-unlocked \mapsto \mathbf{F}}
O = \{ \langle home \wedge bike \wedge \neg bike-locked, \neg home \wedge uni \rangle, \}
           \langle bike \wedge bike\text{-locked}, \neg bike\text{-locked} \wedge bike\text{-unlocked} \rangle,
           \langle bike \wedge \neg bike\text{-locked}, bike\text{-locked} \wedge \neg bike\text{-unlocked} \rangle
          \langle uni, lecture \land ((bike \land \neg bike-locked) \rhd \neg bike) \rangle \}
```

Identify negative conditions for v.

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 $\gamma = lecture \wedge bike$ 

Positive Normal Form

#### Positive Normal Form: Example

#### Example (Transformation to Positive Normal Form)

```
V = \{home, uni, lecture, bike, bike-locked, bike-unlocked\}
 I = \{ home \mapsto \mathbf{T}, bike \mapsto \mathbf{T}, bike-locked \mapsto \mathbf{T}, \}
          uni \mapsto \mathbf{F}, lecture \mapsto \mathbf{F}, bike-unlocked \mapsto \mathbf{F}}
O = \{ \langle home \wedge bike \wedge bike-unlocked, \neg home \wedge uni \rangle, \}
          \langle bike \wedge bike\text{-locked}, \neg bike\text{-locked} \wedge bike\text{-unlocked} \rangle,
          \langle bike \wedge bike-unlocked, bike-locked \wedge \neg bike-unlocked \rangle.
          \langle uni, lecture \land ((bike \land bike-unlocked) \rhd \neg bike) \rangle \}
\gamma = lecture \wedge bike
```

```
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```

## Positive Normal Form: Example

```
Example (Transformation to Positive Normal Form)
```

```
V = \{home, uni, lecture, bike, bike-locked, bike-unlocked\}
 I = \{ home \mapsto \mathbf{T}, bike \mapsto \mathbf{T}, bike-locked \mapsto \mathbf{T}, \}
         uni \mapsto \mathbf{F}, lecture \mapsto \mathbf{F}, bike-unlocked \mapsto \mathbf{F}
O = \{ \langle home \wedge bike \wedge bike-unlocked, \neg home \wedge uni \rangle, \}
          \langle bike \wedge bike\text{-locked}, \neg bike\text{-locked} \wedge bike\text{-unlocked} \rangle
          \langle bike \wedge bike-unlocked \rangle, bike-locked \wedge \neg bike-unlocked \rangle,
         \langle uni, lecture \land ((bike \land bike-unlocked) \rhd \neg bike) \rangle \}
\gamma = lecture \wedge bike
```

Replace by positive condition  $\hat{v}$ .

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Positive Normal Form

Positive Normal Form

#### Why Positive Normal Form is Interesting

In positive normal form, good and bad effects are easy to distinguish:

- Effects that make state variables true (add effects) are good.
- Effects that make state variables false (delete effects) are bad.

This is particularly useful for planning algorithms based on delete relaxation, which we will study later in this course.

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## A6.3 STRIPS

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## STRIPS Operators and Planning Tasks

#### Definition (STRIPS Operator)

An operator o of a prop. planning task is a STRIPS operator if

- pre(o) is a conjunction of state variables, and
- eff(o) is a conflict-free conjunction of atomic effects.

#### Definition (STRIPS Planning Task)

A propositional planning task  $\langle V, O, I, \gamma \rangle$  is a STRIPS planning task if all operators  $o \in O$  are STRIPS operators and  $\gamma$  is a conjunction of state variables.

Note: STRIPS operators are conflict-free and flat.

STRIPS is a special case of positive normal form.

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STRIPS

## STRIPS Operators: Remarks

► Every STRIPS operator is of the form

$$\langle v_1 \wedge \cdots \wedge v_n, \ell_1 \wedge \cdots \wedge \ell_m \rangle$$

where  $v_i$  are state variables and  $\ell_i$  are atomic effects.

- ▶ Often, STRIPS operators *o* are described via three sets of state variables:
  - the preconditions (state variables occurring in pre(o))
  - ▶ the add effects (state variables occurring positively in eff(o))
  - ightharpoonup the delete effects (state variables occurring negatively in eff(o))
- ▶ Definitions of STRIPS in the literature often do **not** require conflict-freeness. But it is easy to achieve and makes many things simpler.
- ► There exists a variant called STRIPS with negation where negative literals are also allowed in conditions.

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STRIPS

## Why STRIPS is Interesting

- ► STRIPS is particularly simple, yet expressive enough to capture general planning tasks.
- ► In particular, STRIPS planning is no easier than planning in general (as we will see next week).
- Many algorithms in the planning literature are only presented for STRIPS planning tasks (generalization is often, but not always, obvious).

#### **STRIPS**

STanford Research Institute Problem Solver (Fikes & Nilsson, 1971)

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Transformation to STRIPS

- ▶ Not every operator is equivalent to a STRIPS operator.
- ► However, each operator can be transformed into a set of STRIPS operators whose "combination" is equivalent to the original operator. (How?)
- ► However, this transformation may exponentially increase the number of operators. There are planning tasks for which such a blow-up is unavoidable.
- ► There are polynomial transformations of propositional planning tasks to STRIPS, but these do not lead to isomorphic transition systems (auxiliary states are needed). (They are, however, equivalent in a weaker sense.)

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## SAS<sup>+</sup> Operators and Planning Tasks

Definition (SAS<sup>+</sup> Operator)

An operator o of an FDR planning task is a SAS<sup>+</sup> operator if

- pre(o) is a satisfiable conjunction of atoms, and
- eff(o) is a conflict-free conjunction of atomic effects.

Definition (SAS<sup>+</sup> Planning Task)

An FDR planning task  $\langle V, O, I, \gamma \rangle$  is a SAS<sup>+</sup> planning task if all operators  $o \in O$  are SAS<sup>+</sup> operators and  $\gamma$  is a satisfiable conjunction of atoms.

Note: SAS<sup>+</sup> operators are conflict-free and flat.

A6.4 SAS<sup>+</sup>

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SAS<sup>+</sup> Operators: Remarks

► Every SAS<sup>+</sup> operator is of the form

$$\langle v_1 = d_1 \wedge \cdots \wedge v_n = d_n, \quad v'_1 := d'_1 \wedge \cdots \wedge v'_m := d'_m \rangle$$

where all  $v_i$  are distinct and all  $v'_i$  are distinct.

- ▶ Often, SAS<sup>+</sup> operators o are described via two sets of partial assignments:
  - ▶ the preconditions  $\{v_1 \mapsto d_1, \dots, v_n \mapsto d_n\}$
  - ▶ the effects  $\{v_1' \mapsto d_1', \dots, v_m' \mapsto d_m'\}$

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SAS<sup>+</sup> vs. STRIPS

- ► SAS<sup>+</sup> is an analogue of STRIPS planning tasks for FDR, but there is no special role of "positive" conditions.
- ▶ Apart from this difference, all comments for STRIPS apply analogously.
- ▶ If all variable domains are binary, SAS<sup>+</sup> is essentially STRIPS with negation.

SAS<sup>+</sup>

Derives from SAS = Simplified Action Structures (Bäckström & Klein, 1991)

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## Summary

- A positive task allows distinguishing good and bad effects. The notion of positive tasks only exists for propositional tasks.
- A positive task with flat operators is in positive normal form.
- **STRIPS** is even more restrictive than positive normal form, forbidding complex preconditions and conditional effects.
- ▶ Both forms are expressive enough to capture general propositional planning tasks.
- ► Transformation to positive normal form is possible with polynomial size increase.
- Isomorphic transformations of propositional planning tasks to STRIPS can increase the number of operators exponentially; non-isomorphic polynomial transformations exist.
- ► SAS<sup>+</sup> is the analogue of STRIPS for FDR planning tasks.

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A6.5 Summary

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