

# Foundations of Artificial Intelligence

## G6. Board Games: Monte-Carlo Tree Search Framework

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May 18, 2026 — G6. Board Games: Monte-Carlo Tree Search Framework

G6.1 Introduction

G6.2 Monte-Carlo Tree Search

G6.3 Summary

## Board Games: Overview

chapter overview:

- ▶ G1. Introduction and State of the Art
- ▶ G2. Formal Definition and Minimax Search
- ▶ G3. Evaluation Functions
- ▶ G4. Alpha-Beta Search
- ▶ G5. Stochastic Games
- ▶ G6. Monte-Carlo Tree Search Framework
- ▶ G7. Monte-Carlo Tree Search Variants

## G6.1 Introduction

## Monte-Carlo Tree Search

algorithms considered previously:

13	2	3	12
9	11	1	10
	6	4	14
15	8	7	5

systematic search:

- ▶ systematic exploration of search space
- ▶ computation of (state) quality follows performance metric

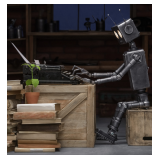


algorithms considered today:



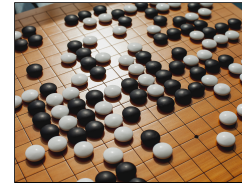
search based on Monte-Carlo methods:

- ▶ sampling of game simulations
- ▶ estimation of (state) quality by averaging over simulation results



## Game Applications

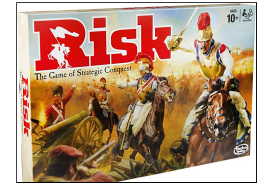
board games



hidden information games



stochastic games



general game playing



real-time strategy games



dynamic difficulty adjustment

Świechowski et al., Monte Carlo Tree Search: a review of recent modifications and applications (2023)

## Applications Beyond Games

story generation



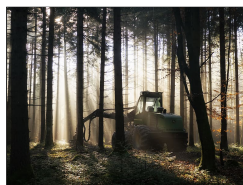
chemical synthesis



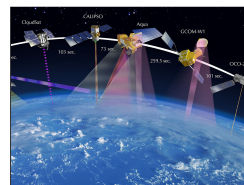
UAV routing



coast security



forest harvesting



Earth observation

Świechowski et al., Monte Carlo Tree Search: a review of recent modifications and applications (2023)

## MCTS Environments

MCTS environments cover **entire spectrum of properties**.

We study MCTS under the **same restrictions** as before, i.e.,

- ▶ environment classification,
- ▶ problem solving method,
- ▶ objective of the agent and
- ▶ performance measure

are identical to Chapters G1–G4.

MCTS extensions exist that allow us to **drop most restrictions**.

## G6.2 Monte-Carlo Tree Search

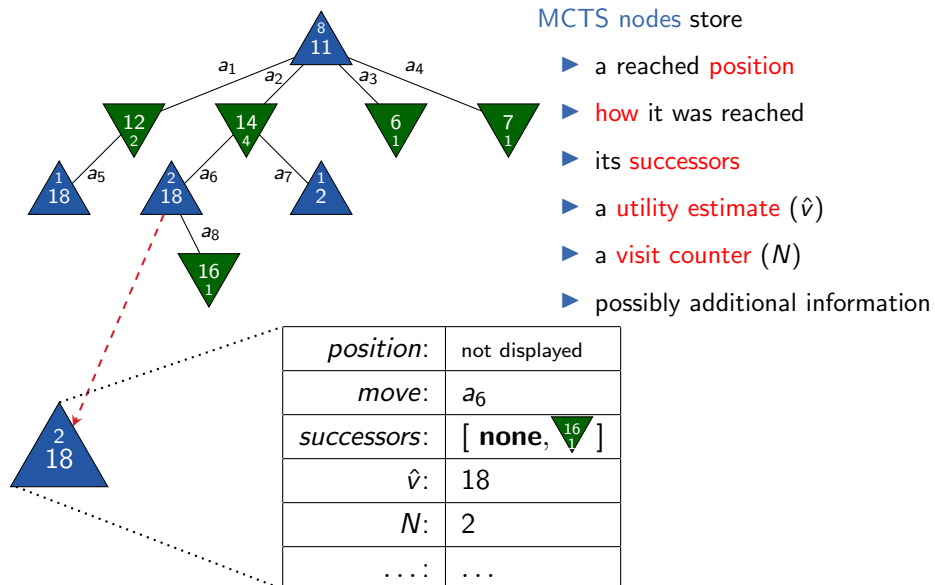
## Data Structures

Monte-Carlo tree search

- ▶ is a **tree search** variant
  - ↪ **no closed list**
- ▶ iteratively performs **game simulations** from the initial position (called **trial** or **rollout**)
  - ↪ **no (explicit) open list**

↪ **MCTS nodes** are the only used data structure

## Data Structure: MCTS Nodes



## Monte-Carlo Tree Search: Idea

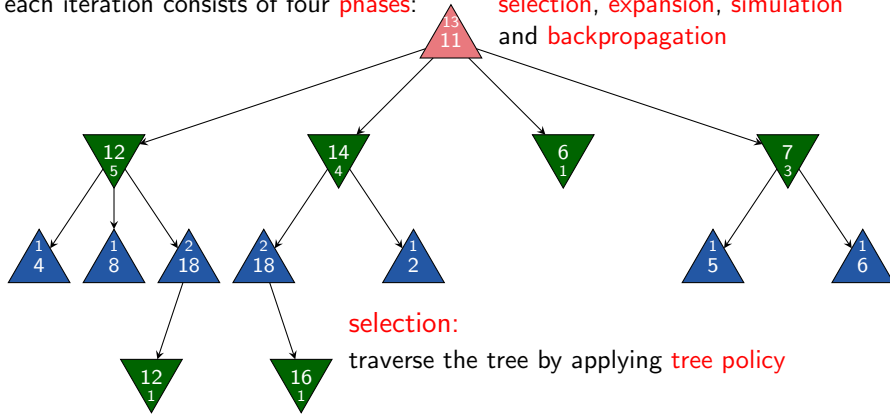
Monte-Carlo Tree Search (MCTS) ideas:

- ▶ **build a partial game tree**
- ▶ by performing **trials** as long as resources (deliberation time, memory) allow
- ▶ initially, the tree contains only the root node
- ▶ each trial adds (at most) **one node** to the tree

after termination, play the associated move of a successor of the root node with **highest utility estimate**

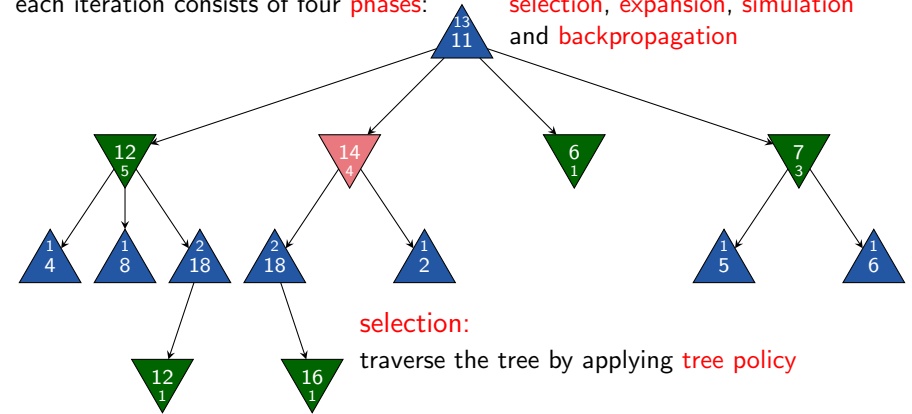
## Idea and Example

each iteration consists of four phases: **selection, expansion, simulation and backpropagation**



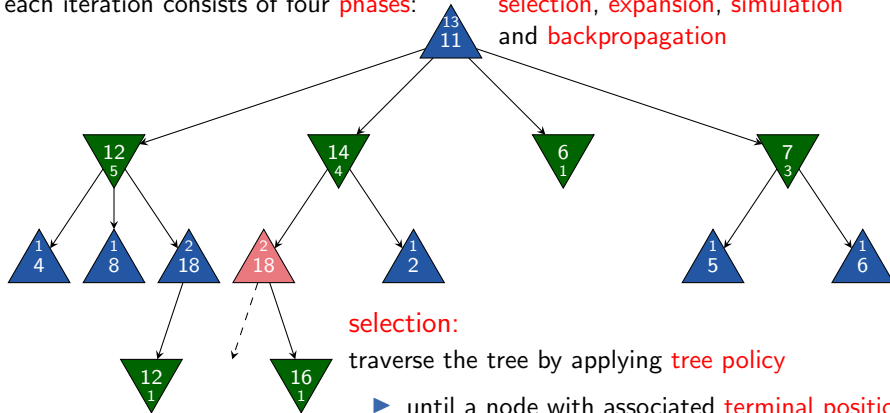
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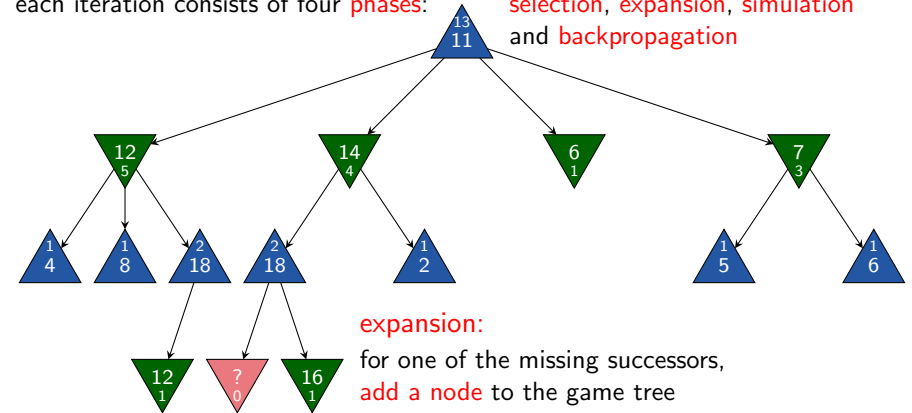
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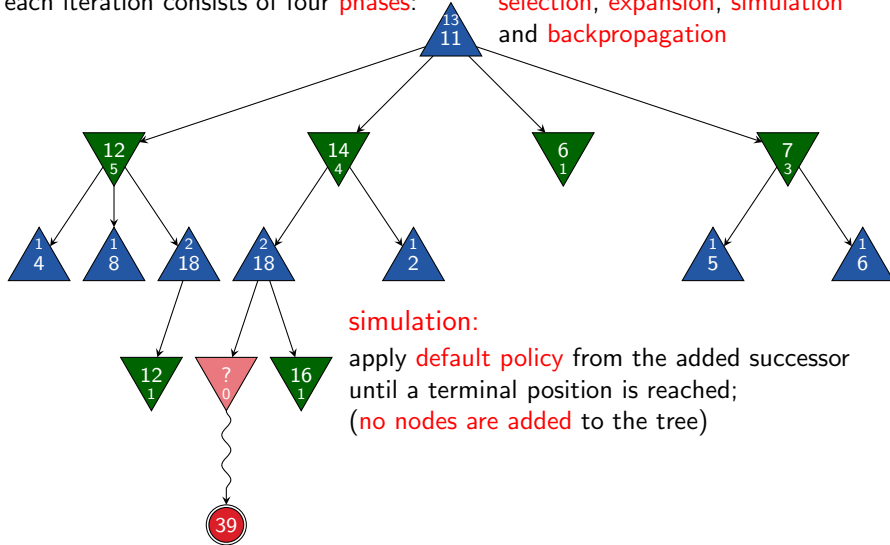
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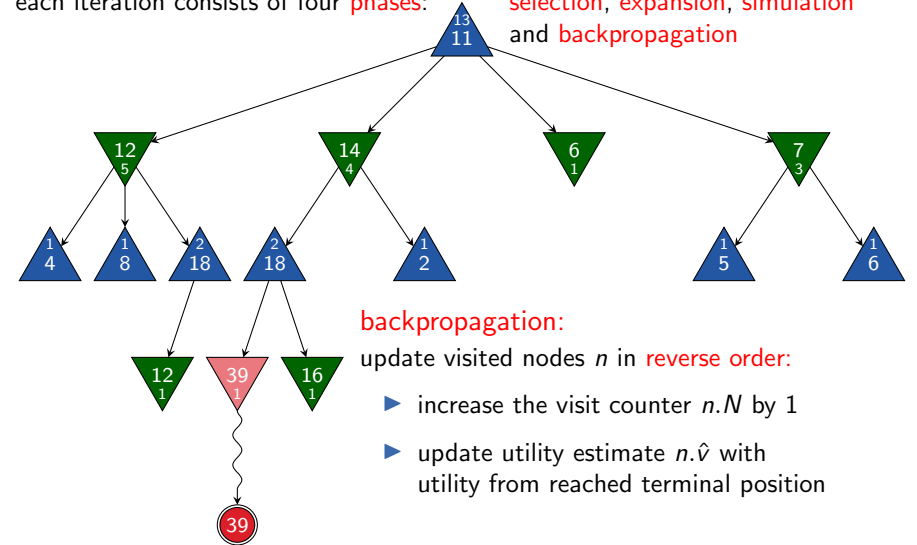
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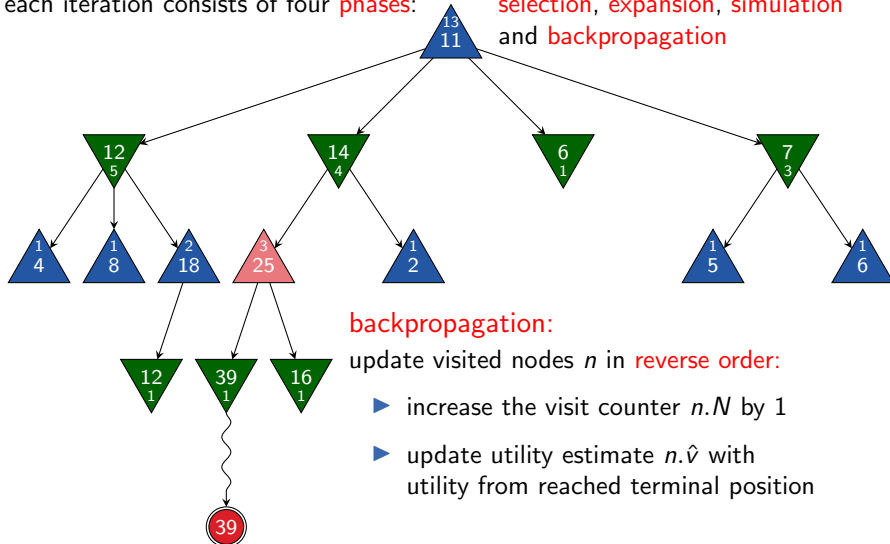
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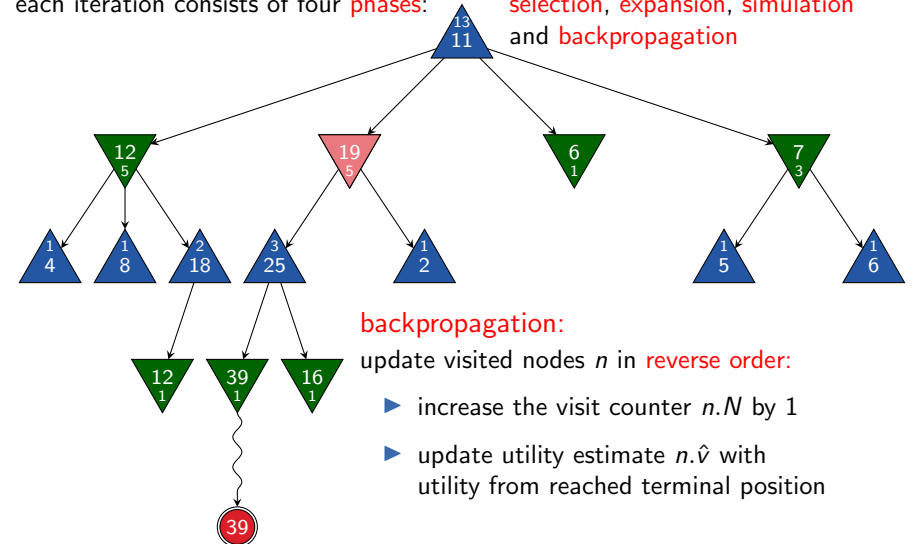
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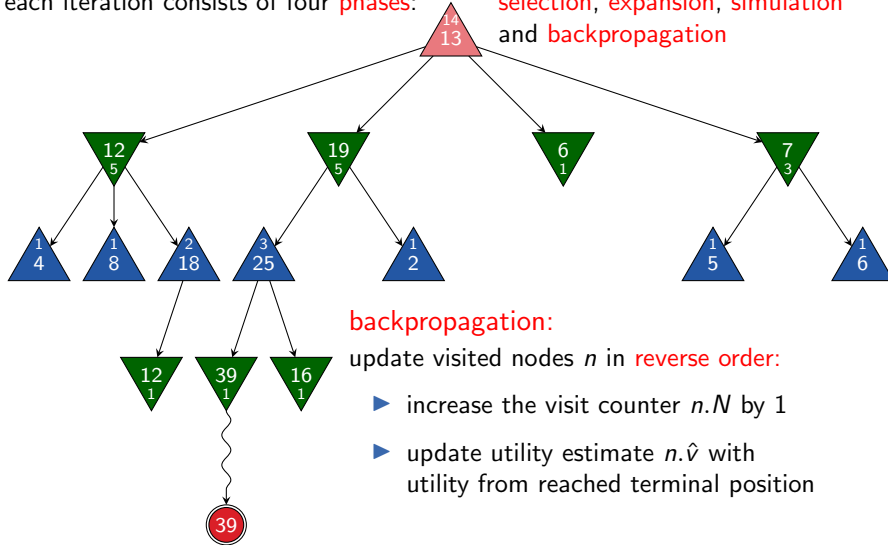
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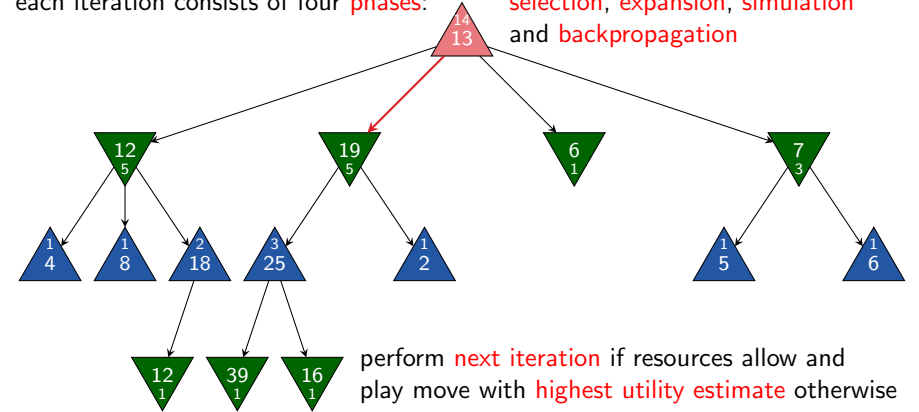
**backpropagation:**

update visited nodes  $n$  in **reverse order**:

- ▶ increase the visit counter  $n.N$  by 1
- ▶ update utility estimate  $n.\hat{v}$  with utility from reached terminal position

## Idea and Example

each iteration consists of four phases: **selection, expansion, simulation and backpropagation**



perform **next iteration** if resources allow and play move with **highest utility estimate** otherwise

## Monte-Carlo Tree Search: Pseudo-Code

## Monte-Carlo Tree Search

```

 $n_0 := \text{create\_root\_node}()$ 
while time_allows():
    visit_node( $n_0$ )
 $n_{\text{best}} := \arg \max_{n \in \text{succ}(n_0)} n.\hat{v}$ 
return  $n_{\text{best}}.\text{move}$ 

```

## Monte-Carlo Tree Search: Pseudo-Code

```

function visit_node( $n$ )
if is_terminal( $n.\text{position}$ ):
     $utility := utility(n.\text{position})$ 
else:
     $s := n.\text{get\_unvisited\_successor}()$ 
    if  $s$  is none:
         $n' := \text{apply\_tree\_policy}(n)$ 
         $utility := \text{visit\_node}(n')$ 
    else:
         $utility := \text{simulate\_game}(s)$ 
         $n.\text{add\_and\_initialize\_child\_node}(s, utility)$ 
     $n.N := n.N + 1$ 
     $n.\hat{v} := n.\hat{v} + \frac{utility - n.\hat{v}}{n.N}$ 
return  $utility$ 

```

## G6.3 Summary

## Summary

- ▶ Monte-Carlo methods compute **averages** over a number of random **samples**.
- ▶ **Monte-Carlo Tree Search (MCTS)** algorithms **simulate** a playout of the game
- ▶ and iteratively build a search tree, adding (at most) one node in each iteration.
- ▶ MCTS is parameterized by a **tree policy** and a **default policy**.