









B3. Finite Automata

### Finite Automaton: Example



When reading the input 01100 the automaton visits the states  $q_0$ ,  $q_1$ ,  $q_0$ ,  $q_0$ ,  $q_1$ ,  $q_2$ .







DFAs

9 / 32

DFAs







DFAs

### A Note on Terminology

 In the literature, "accept" and "recognize" are sometimes used synonymously or the other way around.
 DFA recognizes a word or accepts a language. DFAs

17 / 32

We try to stay consistent using the previous definitions (following the text book by Sipser).







NFAs

### In what Sense is a DFA Deterministic?

- A DFA has a single fixed state from which the computation starts.
- When a DFA is in a specific state and reads an input symbol, we know what the next state will be.
- ▶ For a given input, the entire computation is determined.
- ► This is a deterministic computation.

21 / 32





# Nondeterministic Finite Automata: Example



### differences to DFAs:

- ► transition function δ can lead to zero or more successor states for the same a ∈ Σ
- ε-transitions can be taken without "consuming" a symbol from the input
- the automaton accepts a word if there is at least one accepting sequence of states

22 / 32

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B3. Finite Automata

### $\varepsilon\text{-closure of a State}$

For a state  $q \in Q$ , we write E(q) to denote the set of states that are reachable from q via  $\varepsilon$ -transitions in  $\delta$ .

Definition ( $\varepsilon$ -closure)

For NFA  $M = \langle Q, \Sigma, \delta, q_0, F \rangle$  and state  $q \in Q$ , state p is in the  $\varepsilon$ -closure E(q) of q iff there is a sequence of states  $q'_0, \ldots, q'_n$  with

 $q'_0 = q,$   $q'_i \in \delta(q'_{i-1}, \varepsilon)$  for all  $i \in \{1, \ldots, n\}$  and
  $q'_n = p.$ 

 $q \in E(q)$  for every state q

NFA: Accepted Words Definition (Words Accepted by an NFA) NFA  $M = \langle Q, \Sigma, \delta, q_0, F \rangle$  accepts the word  $w = a_1 \dots a_n$ if there is a sequence of states  $q'_0, \dots, q'_n \in Q$  with

$$\begin{array}{l} @ \quad q'_i \in \bigcup_{q \in \delta(q'_{i-1}, a_i)} E(q) \text{ for all } i \in \{1, \dots, n\} \text{ and} \\ @ \quad q'_n \in F. \end{array}$$

B3. Finite Automata

NFAs

25 / 32

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# Exercise (slido)





NFAs



### Exercise (slido)





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29 / 32

Does this NFA accept input 01010?



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## NFA: Recognized Language

Definition (Language Recognized by an NFA) Let M be an NFA with input alphabet  $\Sigma$ .

The language recognized by M is defined as  $\mathcal{L}(M) = \{ w \in \Sigma^* \mid w \text{ is accepted by } M \}.$ 

Summarv

30 / 32

NFAs

# DFAs are automata where every state transition is uniquely determined. NFAs can have zero, one or more transitions for a given state and input symbol. NFAs can have ε-transitions that can be taken without reading a symbol from the input. NFAs accept a word if there is at least one accepting sequence of states.