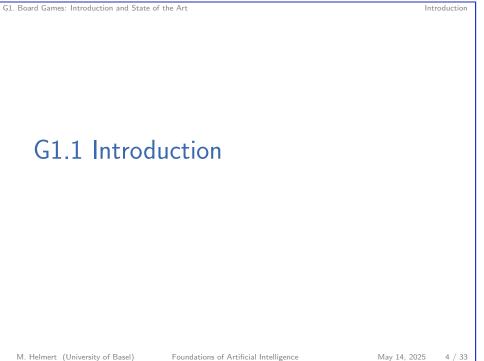
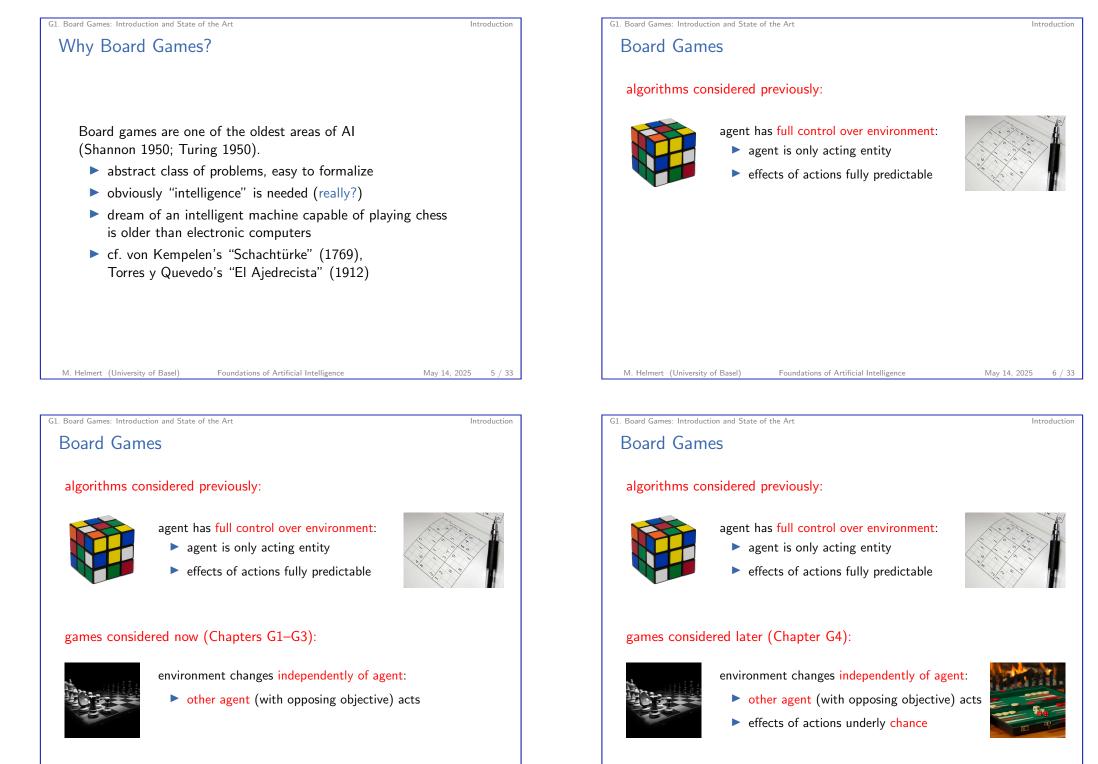




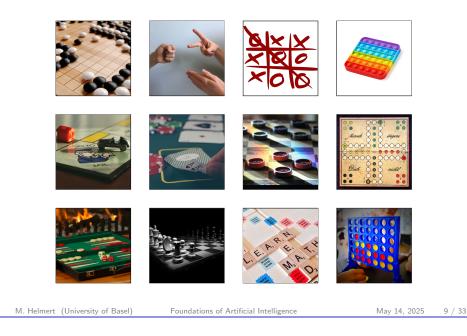
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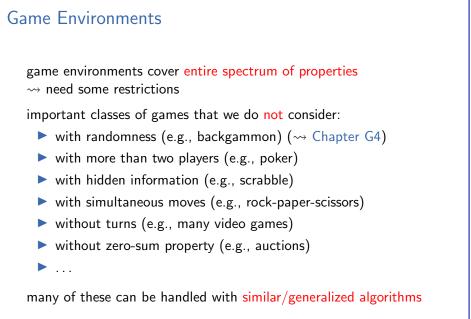


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Applications



G1. Board Games: Introduction and State of the Art



Game Applications Beyond Specific Board Games



Properties of Games Considered (for Now)

- current situation representable by finite set of positions
- there is a finite set of moves players can play
- effects of actions are deterministic
- the game ends when a terminal position is reached
- ▶ a terminal position is reached after a finite number of steps (*)
- terminal positions yield a utility
- no randomness, no hidden information
- (*) Our definitions do not enforce this, and there are some subtleties associated with this requirement which we ignore.

Introduction

Properties of Games Considered (for Now)

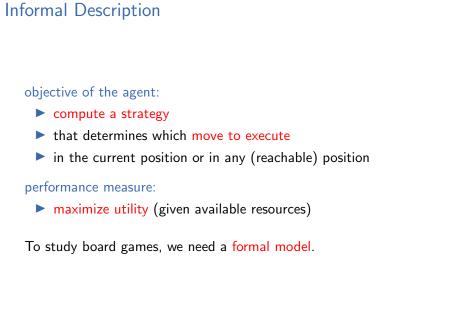


- there are exactly two players called MAX and MIN
- both players observe the entire position (perfect information)
- it is the turn of exactly one player in each non-terminal position
- utility for MAX is opposite of utility for MIN (zero-sum game)
- MAX aims to maximize utility, MIN aims to minimize utility

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G1. Board Games: Introduction and State of the Art

Classification

classification:

Board Games

environment:

- **static vs.** dynamic
- deterministic vs. nondeterministic vs. stochastic
- **fully observable vs.** partially observable
- discrete vs. continuous
- single-agent vs. multi-agent (adversarial)

problem solving method:

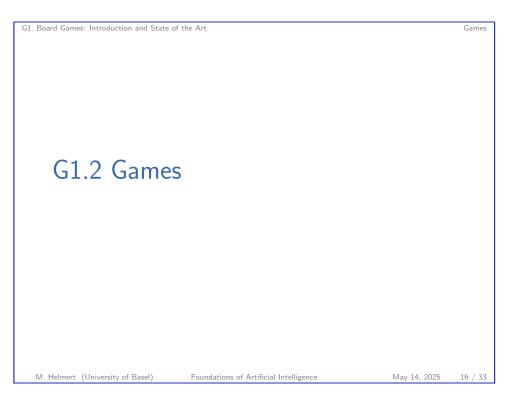
problem-specific vs. general **vs.** learning

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Introduction



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Example: Chess

Example (Chess)

- positions described by:
 - configuration of pieces
 - whose turn it is
 - en-passant and castling rights
- turns alternate
- terminal positions: checkmate and stalemate positions
- utility of terminal position for first player (white):
 - \blacktriangleright +1 if black is checkmated
 - 0 if stalemate position
 - \blacktriangleright -1 if white is checkmated

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Definition

Definition (game)

A game is a 7-tuple $\mathcal{S} = \langle S, A, T, s_{\mathsf{I}}, S_{\mathsf{G}}, \textit{utility}, \textit{player} \rangle$ with

- ► finite set of positions *S*
- ► finite set of moves *A*
- deterministic transition relation $T \subseteq S \times A \times S$
- ▶ initial position $s_{l} \in S$
- ▶ set of terminal positions $S_G \subseteq S$
- ▶ utility function $utility : S_G \to \mathbb{R}$
- ▶ player function player : $S \setminus S_G \rightarrow \{MAX, MIN\}$

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Terminology Compared to State-Space Search

Many concepts for board games are similar to state-space search. Terminology differs, but is often in close correspondence:

- ► state ~→ position
- ▶ goal state ~→ terminal position
- ► action ~→ move
- ► search tree ~→ game tree

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Games: Introduction and State of the Art
Reminder: Bounded Inc-and-Square Search Problem
informal description:

find a sequence of
increment-mod10 (*inc*) and
square-mod10 (*sqr*) actions

on the natural numbers from 0 to 9
that reaches the number 6 or 7
starting from the number 1
assuming each action costs 1.

Games

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Games

Running Example: Bounded Inc-and-Square Game

informal description:

formal model:

- Players alternatingly apply a
 - ▶ increment-mod10 (inc) or
 - ▶ square-mod10 (*sqr*) move
- on the natural numbers from 0 to 9
- starting from the number 1;
- ▶ if the game reaches the number 6 or 7
- or after a fixed number of 4 moves
- ▶ MAX obtains utility u (MIN: -u) where u is the current number.

 \blacktriangleright $A = \{inc, sqr\}$

- for $0 \le i \le 9$ and $0 \le k \le 4$:
 - $\langle s_i^k, inc, s_{(i+1) \mod 10}^{k+1} \rangle \in T$ $\langle s_i^k, sqr, s_{i^{2} \mod 10}^{k+1} \rangle \in T$

▶ $S = \{s_i^k \mid 0 \le i \le 9, 0 \le k \le 4\}$

- $> s_1 = s_1^0$
- ► $S_G = \{s_i^k \mid i \in \{6, 7\} \lor k = 4\}$
- ▶ $utility(s_i^k) = i$ for all $s_i^k \in S_G$
- ▶ player(s_i^k) = MAX if k even and $player(s_i^k) = MIN$ otherwise

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Game

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Strategies

Definition (strategy, partial strategy) Let $S = \langle S, A, T, s_{I}, S_{G}, utility, player \rangle$ be a game and let $S_{MAX} = \{s \in S \mid player(s) = MAX\}.$ A partial strategy for player MAX is a function $\pi: S'_{\mathsf{M} \Delta \mathsf{X}} \mapsto A$ with $S'_{MAX} \subseteq S_{MAX}$ and $\pi(s) = a$ implies that a is applicable in s. If $S'_{MAX} = S_{MAX}$, then π is also called total strategy (or strategy).

We always take the viewpoint of MAX, but S_{MIN} and a (partial/total) strategy for MIN are defined accordingly.

As in classical search problems, the number of positions of (interesting) board games is huge:

- \blacktriangleright Chess: roughly 10⁴⁰ reachable positions; game with 50 moves/player and branching factor 35: tree size roughly $35^{100} \approx 10^{154}$
- \blacktriangleright Go: more than 10¹⁰⁰ positions; game with roughly 300 moves and branching factor 200: tree size roughly $200^{300} \approx 10^{690}$

In addition, it is not sufficient to find a solution path:

- ▶ We need a strategy reacting to all possible opponent moves.
- Usually, such a strategy is implemented as an algorithm that provides the next move on the fly (i.e., not precomputed).

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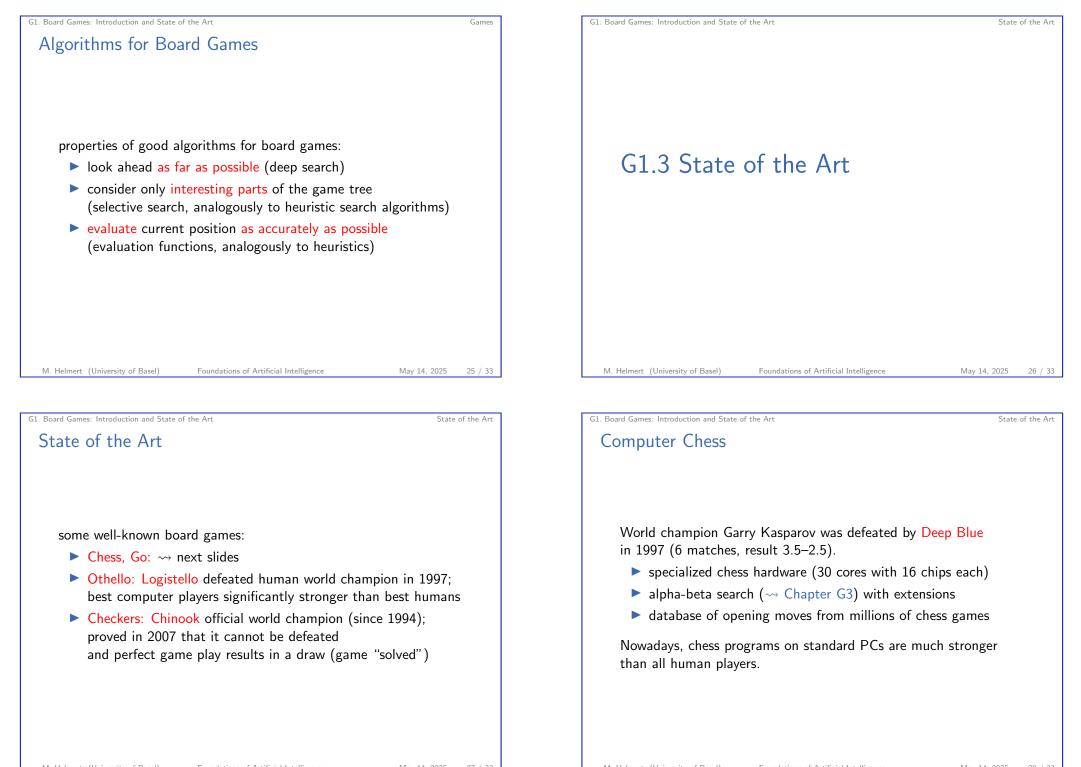
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Games

Specific vs. General Algorithms ▶ We consider approaches that must be tailored to a specific board game for good performance, e.g., by using a suitable evaluation function. → see chapters on informed search methods

- Analogously to the generalization of search methods to declaratively described problems (automated planning), board games can be considered in a more general setting, where game rules (state spaces) are part of the input.
- \rightarrow general game playing: regular competitions since 2005



State of the Art

Computer Chess: Quotes

Computer Chess: Another Quote

John McCarthy (1997)

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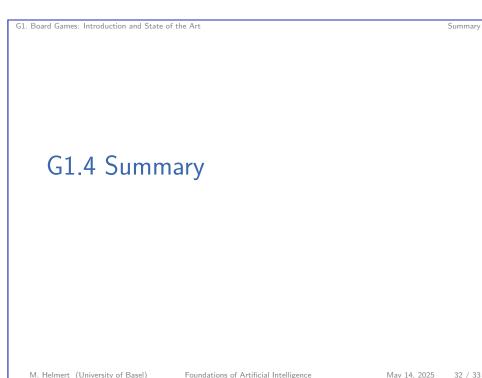
In 1965, the Russian mathematician Alexander Kronrod said, "Chess is the drosophila of artificial intelligence."

However, computer chess has developed much as genetics might have if the geneticists had concentrated their efforts starting in 1910 on breeding racing drosophilae. We would have some science, but mainly we would have very fast fruit flies.

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Claude Shannon (1950)

The chess machine is an ideal one to start with, since

- the problem is sharply defined both in allowed operations (the moves) and in the ultimate goal (checkmate),
- 2 it is neither so simple as to be trivial nor too difficult for satisfactory solution,
- **3** chess is generally considered to require "thinking" for skillful play, [...]
- the discrete structure of chess fits well into the digital nature of modern computers.

Alexander Kronrod (1965)

Chess is the drosophila of Artificial Intelligence.

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State of the Art

G1. Board Games: Introduction and State of the Art

Computer Go

Computer Go

▶ The best Go programs use Monte-Carlo techniques (UCT).

Foundations of Artificial Intelligence

- Until autumn 2015, leading programs Zen, Mogo, Crazystone played on the level of strong amateurs (1 kyu/1 dan).
- Until then, Go was considered as one of the "last" games that are too complex for computers.
- ▶ In October 2015, Deep Mind's AlphaGo defeated the European Champion Fan Hui (2p dan) with 5:0.
- ▶ In March 2016, AlphaGo defeated world-class player Lee Sedol (9p dan) with 4:1. The prize for the winner was 1 million US dollars.

G1. Board Games: Introduction and State of the Art

Summary

Summary

- Board games can be considered as classical search problems extended by an opponent.
- Both players try to reach a terminal position with (for the respective player) maximal utility.
- very successful for a large number of popular games
- Deep Blue defeated the world chess champion in 1997.
 Today, chess programs play vastly more strongly than humans.
- AlphaGo defeated one of the world's best players in the game of Go in 2016.

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