

Combinato	orial Opt	timization: Overv	view		
Chapter o	verview: c	ombinatorial optimiza	tion		
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C2. Combinatorial Optimization: Advanced Techniques

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Dealing with Local Optima

## C2.1 Dealing with Local Optima





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Weaknesses of Local Soarch Algorithms

Dealing with Local Optima

Dealing with Local Optima

## Allowing Stagnation

#### allowing stagnation:

- do not terminate when no neighbor is an improvement
- limit number of steps to guarantee termination
- ▶ at end, return best visited candidate
  - pure search problems: terminate as soon as solution found

#### Example 8 queens problem:

- ▶ with a bound of 100 steps solution found in 96% of the cases
- on average 22 steps until solution found
- $\rightsquigarrow$  works very well for this problem; for more difficult problems often not good enough

### Random Aspects in the Search Neighborhood

a possible variation of hill climbing for 8 queens: Randomly select a file; move queen in this file to square with minimal number of conflicts (null move possible).





 → Good local search approaches often combine randomness (exploration) with heuristic guidance (exploitation).

German: Exploration, Exploitation

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Outlook: Simulated Annealing

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### Simulated Annealing

Simulated annealing is a local search algorithm that systematically injects noise, beginning with high noise, then lowering it over time.

- walk with fixed number of steps N (variations possible)
- initially it is "hot", and the walk is mostly random
- over time temperature drops (controlled by a schedule)
- ► as it gets colder, moves to worse neighbors become less likely very successful in some applications, e.g., VLSI layout

German: simulierte Abkühlung, Rauschen

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## C2.2 Outlook: Simulated Annealing

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Simulated Annealing: Pseudo-Code

Outlook: Simulated Annealing

```
Simulated Annealing (for Maximization Problems)

curr := a random candidate

best := none

for each t \in \{1, ..., N\}:

if is_solution(curr) and (best is none or v(curr) > v(best)):

best := curr

T := schedule(t)

next := a random neighbor of curr

\Delta E := h(next) - h(curr)

if \Delta E \ge 0 or with probability e^{\frac{\Delta E}{T}}:

curr := next

return best
```

# C2.3 Outlook: Genetic Algorithms

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Outlook: Genetic Algorithms

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Genetic Algorithm: Example

#### example 8 queens problem:

- genome: encode candidate as string of 8 numbers
- fitness: number of non-attacking queen pairs
- use population of 100 candidates

```
Evolution often finds good solutions.
idea: simulate evolution by selection, crossover and mutation of individuals
ingredients:

encode each candidate as a string of symbols (genome)
fitness function: evaluates strength of candidates (= heuristic)
population of k (e.g. 10–1000) individuals (candidates)

German: Evolution, Selektion, Kreuzung, Mutation, Genom, Fitnessfunktion, Population, Individual
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### Genetic Algorithms

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