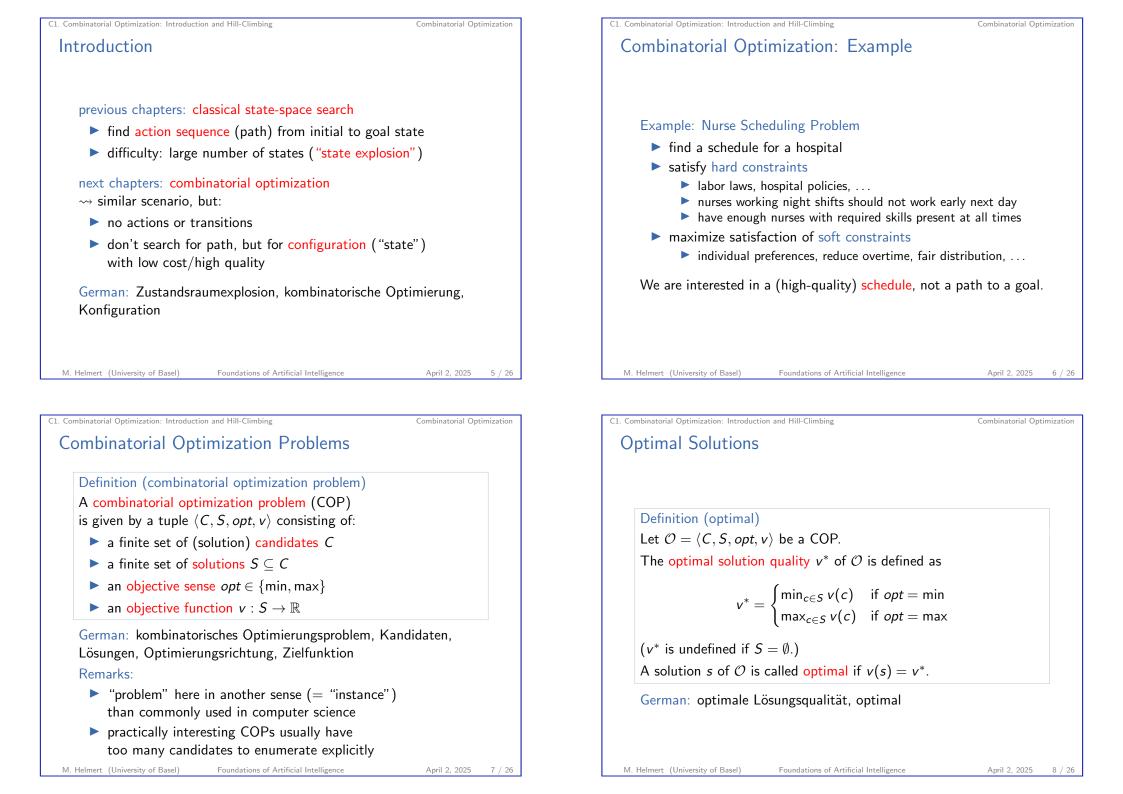


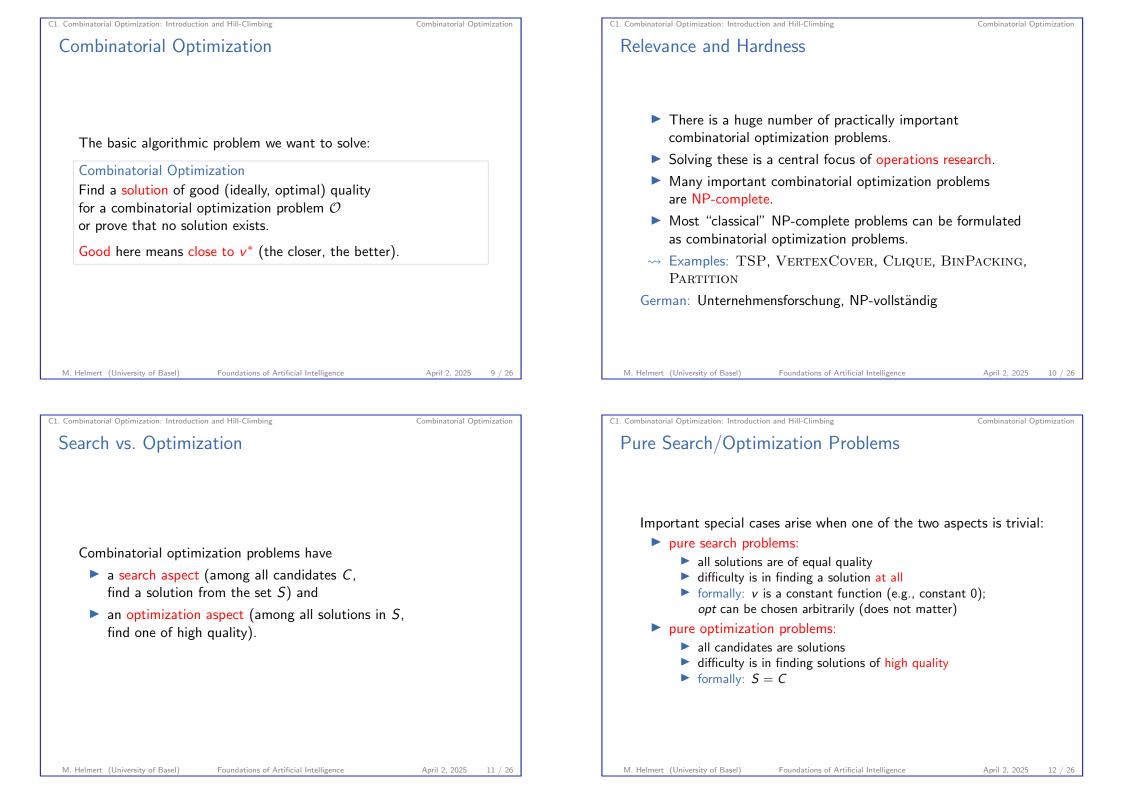
Foundations of Arti April 2, 2025 — C1. Combine	ficial Intelligence atorial Optimization: Introduction and	Hill-Climbing	
C1.1 Combinator	rial Optimization		
C1.2 Example			
C1.3 Local Search: Hill Climbing			
C1.4 Summary			
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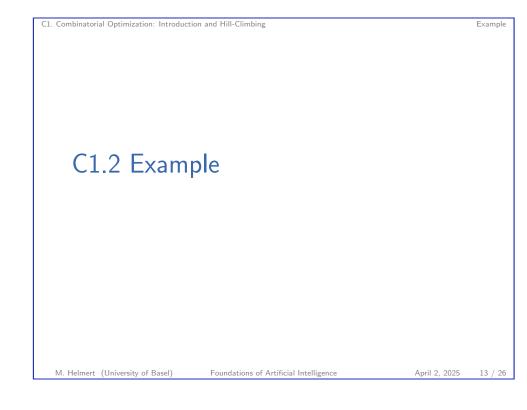
C1. Combinatorial Optimization: Introduction and Hill-Climbing

Combinatorial Optimization

C1.1 Combinatorial Optimization

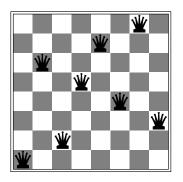






C1. Combinatorial Optimization: Introduction and Hill-Climbing

Example: 8 Queens Problem Problem: Place 8 queens on a chess board such that no two queens threaten each other.



Is this candidate a solution?

Example

Example: 8 Queens Problem

8 Queens Problem

How can we

- ▶ place 8 queens on a chess board
- such that no two queens threaten each other?

German: 8-Damen-Problem

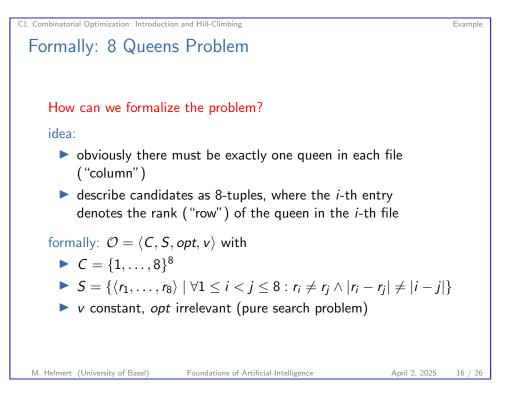
- originally proposed in 1848
- ▶ variants: board size; other pieces; higher dimension

There are 92 solutions, or 12 solutions if we do not count symmetric solutions (under rotation or reflection) as distinct.

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C1.3 Local Search: Hill Climbing

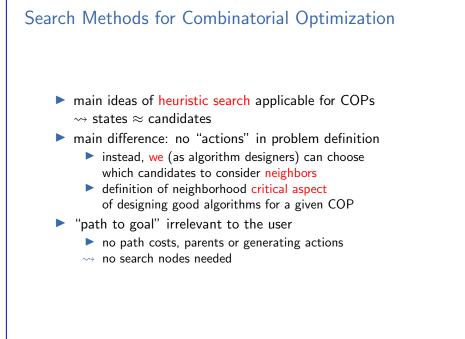
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C1. Combinatorial Optimization: Introduction and Hill-Climbing

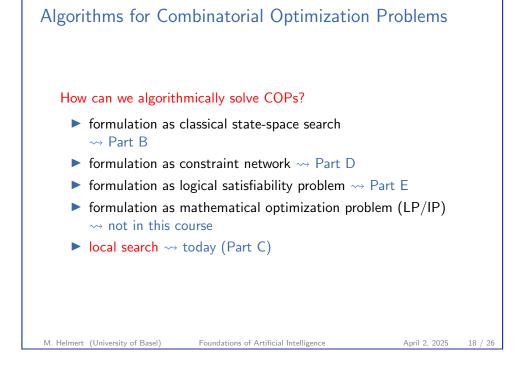
Local Search: Hill Climbing

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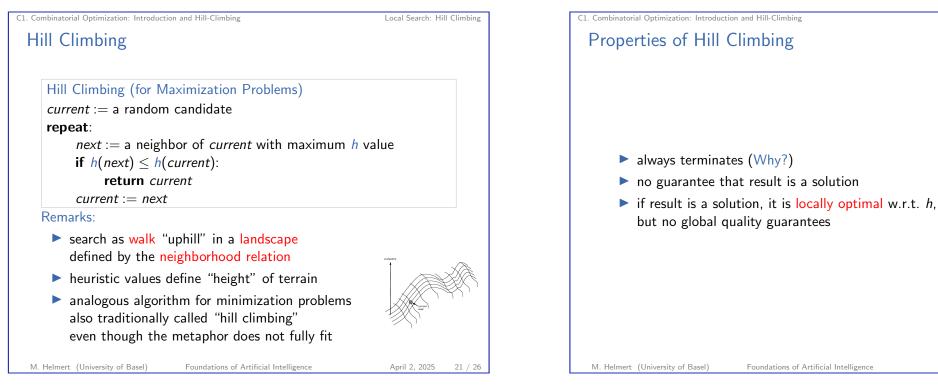
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C1. Combinatorial Optimization: Introduction and Hill-Climbing

C1. Combinatorial Optimization: Introduction and Hill-Climbing	Local Search: Hill Climbing
Local Search: Idea	
main ideas of local search algorithms for COPs	5:
heuristic h estimates quality of candidates	5
for pure optimization: often objective function	
for pure search: often distance estimate	to closest solution
(as in state-space search)	
do not remember paths, only candidates	
often only one current candidate ~> very i	memory-efficient
(however, not complete or optimal)	
often initialization with random candidate	
iterative improvement by hill climbing	

Local Search: Hill Climbing

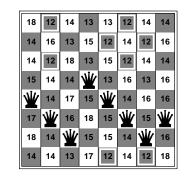


C1. Combinatorial Optimization: Introduction and Hill-Climbing

Local Search: Hill Climbing

Example: 8 Queens Problem

Problem: Place 8 queens on a chess board such that no two queens threaten each other. possible heuristic: no. of pairs of queens threatening each other (formalization as minimization problem) possible neighborhood: move one queen within its file



Local Search: Hill Climbing

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