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B8.1 Depth-first Search

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Depth-first Search



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Non-recursive Depth-first Search: Discussion

discussion:

- there isn't much wrong with this pseudo-code (as long as we ensure to release nodes that are no longer required when using programming languages without garbage collection)
- however, depth-first search as a recursive algorithm is simpler and more efficient
- $\rightsquigarrow~\mathsf{CPU}$ stack as implicit open list
- \rightsquigarrow no search node data structure needed

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Depth-first Searc

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Depth-first Search: Complexity

time complexity:

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- If the state space includes paths of length m, depth-first search can generate O(b^m) nodes, even if much shorter solutions (e.g., of length 1) exist.
- On the other hand: in the best case, solutions of length l can be found with O(bl) generated nodes. (Why?)

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• improvable to $O(\ell)$ with incremental successor generation

space complexity:

- only need to store nodes along currently explored path ("along": nodes on path and their children)
- \rightsquigarrow space complexity O(bm) if m maximal search depth reached
- Iow memory complexity main reason why depth-first search interesting despite its disadvantages

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Depth-first Search (Recursive Version)

function depth_first_search(s) if is_goal(s): return $\langle \rangle$ for each $\langle a, s' \rangle \in \text{succ}(s)$: $solution := depth_first_search(s')$ if solution \neq none: *solution*.push_front(*a*) return solution return none main function: Depth-first Search (Recursive Version) **return** depth_first_search(init()) M. Helmert (University of Basel) Foundations of Artificial Intelligence March 17, 2025 18 / 35















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Comparison of Blind Search Algorithms

completeness, optimality, time and space complexity

		search algorithm				
	criterion	breadth-	uniform	depth-	depth-	iterative
		first	cost	first	limited	deepening
	complete?	yes*	yes	no	no	semi
	optimal?	yes**	yes	no	no	yes**
	time	$O(b^d)$	$O(b^{\lfloor c^*/\varepsilon floor+1})$	$O(b^m)$	$O(b^\ell)$	$O(b^d)$
	space	$O(b^d)$	$O(b^{\lfloor c^*/\varepsilon floor+1})$	O(bm)	$O(b\ell)$	O(bd)
Ь ≥	 2 branching factor d minimal solution depth m maximal search depth ℓ depth limit 			remarks: * for BFS- ** only wit	Tree: sem h uniform:	i-complete action costs

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Summary

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