Foundations of Artificial Intelligence B4. State-Space Search: Data Structures for Search Algorithms

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Foundations of Artificial Intelligence March 3, 2025 — B4. State-Space Search: Data Structures for Search Algorithms

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B4.2 Search Nodes

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State-Space Search: Overview

Chapter overview: state-space search

- ▶ B1–B3. Foundations
- ▶ B4–B8. Basic Algorithms
 - B4. Data Structures for Search Algorithms
 - ▶ B5. Tree Search and Graph Search
 - B6. Breadth-first Search
 - B7. Uniform Cost Search
 - B8. Depth-first Search and Iterative Deepening
- ▶ B9–B15. Heuristic Algorithms

B4.1 Introduction

Finding Solutions in State Spaces



How can we systematically find a solution?

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Search Algorithms

► We now move to search algorithms.

As everywhere in computer science, suitable data structures are a key to good performance.

 \rightsquigarrow common operations must be fast

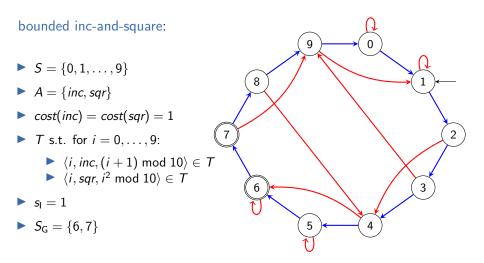
 Well-implemented search algorithms process up to ~30,000,000 states/second on a single CPU core.
 → bonus materials (Burns et al. paper)

this chapter: some fundamental data structures for search

Preview: Search Algorithms

- next chapter: we introduce search algorithms
- now: short preview to motivate data structures for search

Running Example: Reminder



iteratively create a search tree:

starting with the initial state,



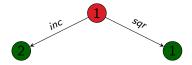
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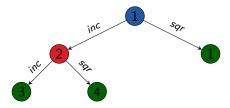
iteratively create a search tree:

- starting with the initial state,
- repeatedly expand a state by generating its successors (which state depends on the used search algorithm)



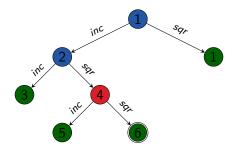
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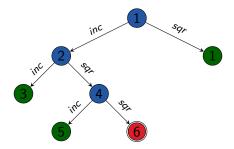
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iteratively create a search tree:

- starting with the initial state,
- repeatedly expand a state by generating its successors (which state depends on the used search algorithm)
- stop when a goal state is expanded (sometimes: generated)
- or all reachable states have been considered



Fundamental Data Structures for Search

We consider three abstract data structures for search:

search node: stores a state that has been reached, how it was reached, and at which cost

- \rightsquigarrow nodes of the example search tree
- open list: efficiently organizes leaves of search tree

 \rightsquigarrow set of leaves of example search tree

 closed list: remembers expanded states to avoid duplicated expansions of the same state
 inner nodes of a search tree

German: Suchknoten, Open-Liste, Closed-Liste

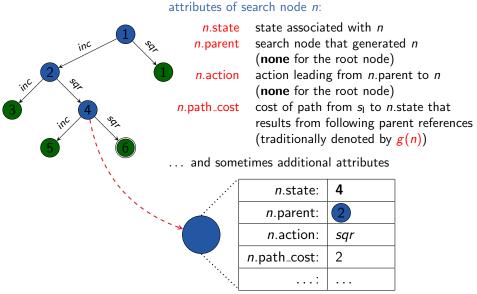
Not all algorithms use all three data structures, and they are sometimes implicit (e.g., on the CPU stack)

B4.2 Search Nodes

Search Nodes

Search Node A search node (node for short) stores a state that has been reached, how it was reached, and at which cost. Collectively they form the so-called search tree (Suchbaum).

Data Structure: Search Nodes



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Search Nodes: Java

```
Search Nodes (Java Syntax)
public interface State {
}
public interface Action {
}
public class SearchNode {
    State state:
    SearchNode parent;
    Action action;
    int pathCost;
}
```

Implementing Search Nodes

- reasonable implementation of search nodes is easy
- advanced aspects:
 - Do we need explicit nodes at all?
 - Can we use lazy evaluation?
 - Should we manually manage memory?
 - Can we compress information?

Operations on Search Nodes: make_root_node

Generate root node of a search tree:

```
function make_root_node()
node := new SearchNode
node.state := init()
node.parent := none
node.action := none
node.path_cost := 0
return node
```

Operations on Search Nodes: make_node

Generate child node of a search node:

```
function make_node(parent, action, state)
node := new SearchNode
node.state := state
node.parent := parent
node.action := action
node.path_cost := parent.path_cost + cost(action)
return node
```

Operations on Search Nodes: extract_path

Extract the path to a search node:

```
function extract_path(node)
path := ⟨⟩
while node.parent ≠ none:
    path.append(node.action)
    node := node.parent
path.reverse()
return path
```

B4.3 Open Lists

Open Lists

Open List

The open list (also: frontier) organizes the leaves of a search tree.

It must support two operations efficiently:

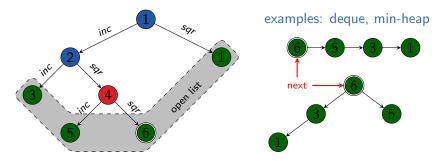
- determine and remove the next node to expand
- insert a new node that is a candidate node for expansion

Remark: despite the name, it is usually a very bad idea to implement open lists as simple lists.

Open Lists: Modify Entries

- Some implementations support modifying an open list entry when a shorter path to the corresponding state is found.
- This complicates the implementation.
- → We do not consider such modifications
 and instead use delayed duplicate elimination (→ later).

Interface of Open Lists



open list open organizes leaves of search tree with the methods: open.is_empty() test if the open list is empty open.pop() remove and return the next node to expand open.insert(n) insert node n into the open list

 open determines strategy which node to expand next (depends on algorithm)

underlying data structure choice depends on this strategy

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B4.4 Closed Lists

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Closed Lists

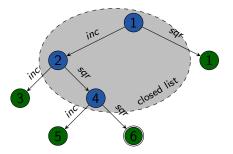
Closed List The closed list remembers expanded states to avoid duplicated expansions of the same state.

It must support two operations efficiently:

- insert a node whose state is not yet in the closed list
- test if a node with a given state is in the closed list; if yes, return it

Remark: despite the name, it is usually a very bad idea to implement closed lists as simple lists. (Why?)

Interface and Implementation of Closed Lists



closed list closed keeps track of expanded states with the methods:

closed.insert(n) insert node n into closed; if a node with this state already exists in closed, replace it closed.lookup(s) test if a node with state s exists in the closed list; if yes, return it; otherwise, return none

efficient implementation often as hash table with states as keys

B4.5 Summary

Summary

search node:

represents states reached during search and associated information

node expansion:

generate successor nodes of a node by applying all actions applicable in the state belonging to the node

open list or frontier:

set of nodes that are currently candidates for expansion

closed list:

set of already expanded nodes (and their states)