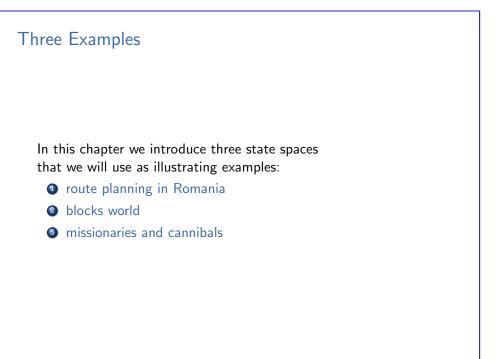


Foundations of Artir February 26, 2025 — B3. Star	ficial Intelligence te-Space Search: Examples of State	Spaces	
B3.1 Route Planning in Romania			
B3.2 Blocks World			
B3.3 Missionaries and Cannibals			
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B3.1 Route Planning in Romania

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B3. State-Space Search: Examples of State Spaces

Route Planning in Romania

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Romania Formally

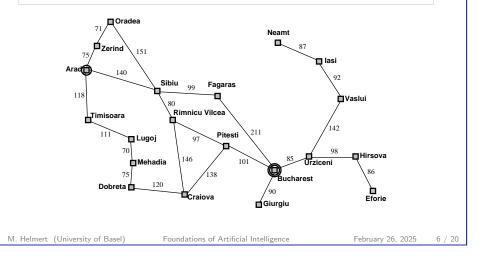
State Space Route Planning in Romania

- states S: {arad, bucharest, craiova, ..., zerind}
- actions A: $move_{c,c'}$ for any two cities c and c' connected by a single road segment
- ▶ action costs *cost*: see figure, e.g., *cost*(*move*_{iasi,vaslui}) = 92
- transitions $T: s \xrightarrow{a} s'$ iff $a = move_{s s'}$
- \blacktriangleright initial state: $s_{I} = arad$
- goal states: $S_G = \{ bucharest \}$

Route Planning in Romania

Setting: Route Planning in Romania

We are on holiday in Romania and are currently located in Arad. Our flight home leaves from Bucharest. How to get there?





Blocks World

Blocks world is a traditional example problem in AI.

Setting: Blocks World

- Colored blocks lie on a table.
- They can be stacked into towers, moving one block at a time.

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Our task is to create a given goal configuration.

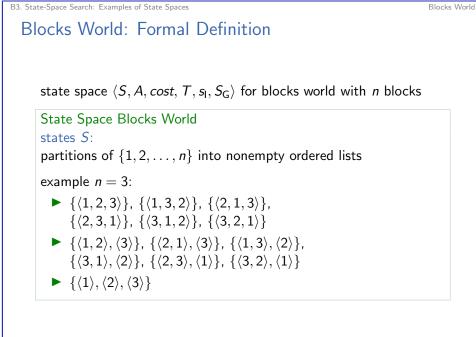
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Blocks World

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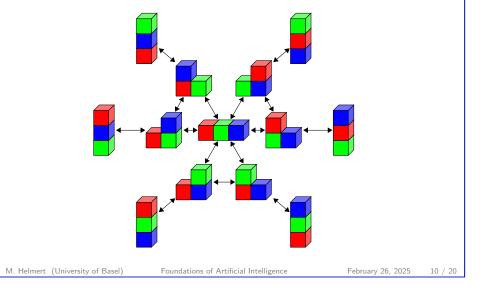
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Blocks World



Example: Blocks World with Three Blocks

Action names omitted for readability. All actions cost 1. Initial state and goal can be arbitrary.



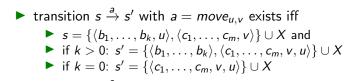
B3. State-Space Search: Examples of State Spaces Blocks World Blocks World: Formal Definition state space $(S, A, cost, T, s_1, S_G)$ for blocks world with *n* blocks State Space Blocks World actions A: • {*move*_{*u*,*v*} | $u, v \in \{1, ..., n\}$ with $u \neq v$ } \blacktriangleright move block *u* onto block *v*. both must be uppermost blocks in their towers ▶ {*to-table*_{*u*} | $u \in \{1, ..., n\}$ } • move block u onto the table (\rightsquigarrow forming a new tower) must be uppermost block in its tower action costs cost: cost(a) = 1 for all actions $a \in A$



Blocks World: Formal Definition

state space $(S, A, cost, T, s_1, S_G)$ for blocks world with *n* blocks

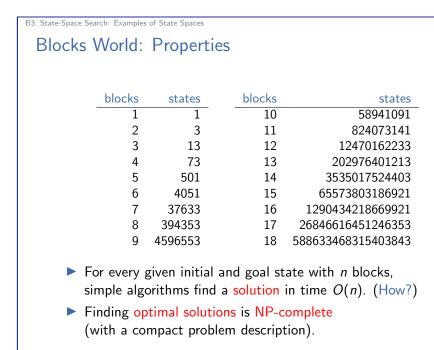
State Space Blocks World transitions:



- transition $s \xrightarrow{a} s'$ with a = to-table_u exists iff
 - $s = \{ \langle b_1, \ldots, b_k, u \rangle \} \cup X$ with k > 0 and
 - $\blacktriangleright s' = \{ \langle b_1, \ldots, b_k \rangle, \langle u \rangle \} \cup X$

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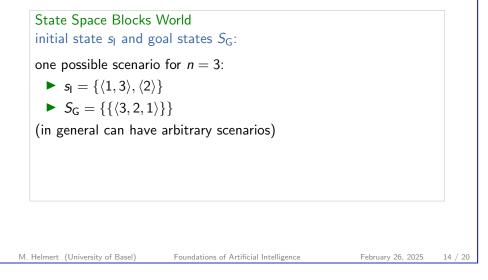
Blocks World

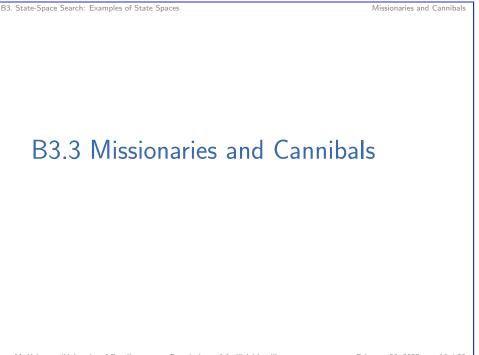
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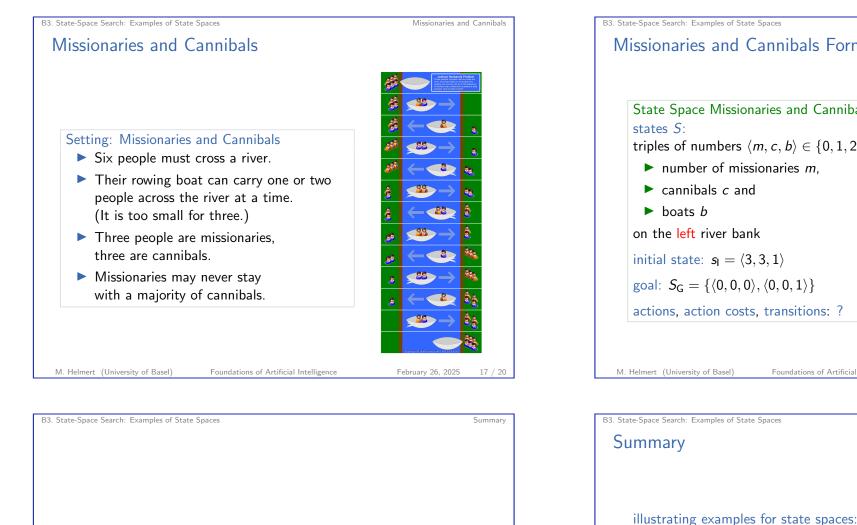
Blocks World

Blocks World: Formal Definition

state space $(S, A, cost, T, s_1, S_G)$ for blocks world with *n* blocks







B3.4 Summary

route planning in Romania:

missionaries and cannibals:

traditional example problem in AI

blocks world:

small example of explicitly representable state space

number of states explodes quickly as n grows

traditional brain teaser with small state space (32 states, of which many unreachable)

▶ family of tasks where *n* blocks on a table must be rearranged

Summary

Missionaries and Cannibals Formally

