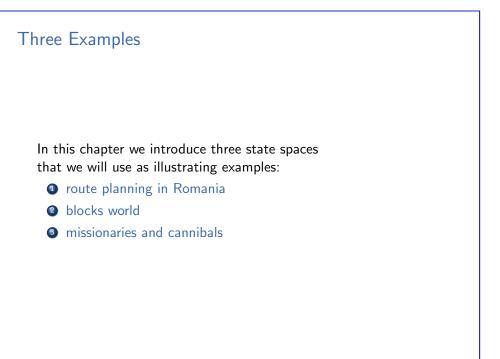


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# B3.1 Route Planning in Romania

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B3. State-Space Search: Examples of State Spaces

Route Planning in Romania

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**Romania Formally** 

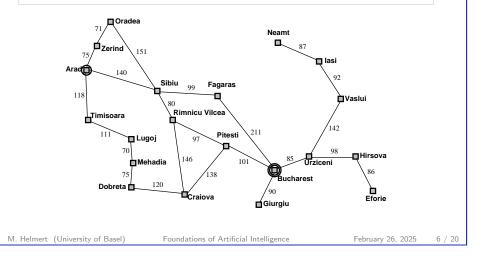
State Space Route Planning in Romania

- states S: {arad, bucharest, craiova, ..., zerind}
- actions A:  $move_{c,c'}$  for any two cities c and c' connected by a single road segment
- ▶ action costs *cost*: see figure, e.g., *cost*(*move*<sub>iasi,vaslui</sub>) = 92
- transitions  $T: s \xrightarrow{a} s'$  iff  $a = move_{s s'}$
- $\blacktriangleright$  initial state:  $s_{I} = arad$
- goal states:  $S_G = \{ bucharest \}$

### Route Planning in Romania

#### Setting: Route Planning in Romania

We are on holiday in Romania and are currently located in Arad. Our flight home leaves from Bucharest. How to get there?





#### **Blocks World**

Blocks world is a traditional example problem in AI.

#### Setting: Blocks World

- Colored blocks lie on a table.
- They can be stacked into towers, moving one block at a time.

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Our task is to create a given goal configuration.

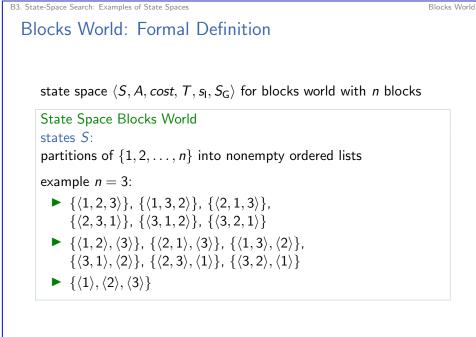
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Blocks World

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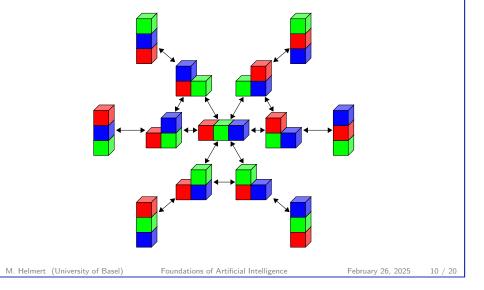
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Blocks World



### Example: Blocks World with Three Blocks

Action names omitted for readability. All actions cost 1. Initial state and goal can be arbitrary.



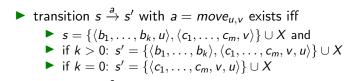
## B3. State-Space Search: Examples of State Spaces Blocks World Blocks World: Formal Definition state space $(S, A, cost, T, s_1, S_G)$ for blocks world with *n* blocks State Space Blocks World actions A: • {*move*<sub>*u*,*v*</sub> | $u, v \in \{1, ..., n\}$ with $u \neq v$ } $\blacktriangleright$ move block *u* onto block *v*. both must be uppermost blocks in their towers ▶ {*to-table*<sub>*u*</sub> | $u \in \{1, ..., n\}$ } • move block u onto the table ( $\rightsquigarrow$ forming a new tower) must be uppermost block in its tower action costs cost: cost(a) = 1 for all actions $a \in A$



### Blocks World: Formal Definition

state space  $(S, A, cost, T, s_1, S_G)$  for blocks world with *n* blocks

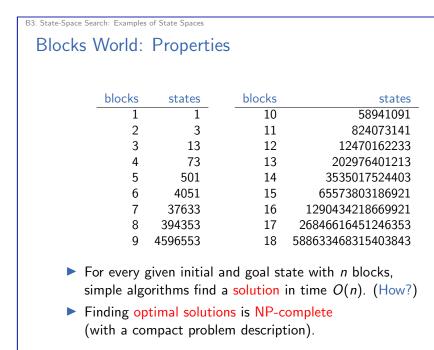
#### State Space Blocks World transitions:



- transition  $s \xrightarrow{a} s'$  with a = to-table<sub>u</sub> exists iff
  - $s = \{ \langle b_1, \ldots, b_k, u \rangle \} \cup X$  with k > 0 and
  - $\blacktriangleright s' = \{ \langle b_1, \ldots, b_k \rangle, \langle u \rangle \} \cup X$

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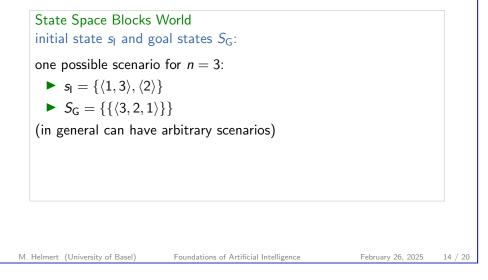
Blocks World

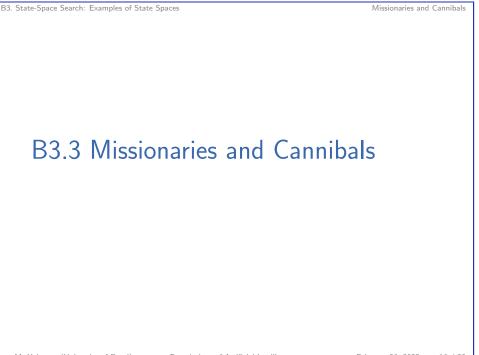
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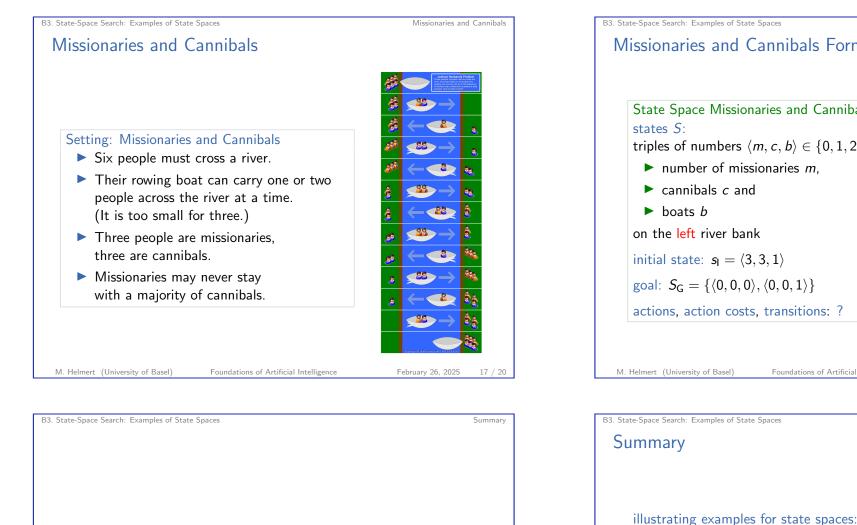
Blocks World

## Blocks World: Formal Definition

state space  $(S, A, cost, T, s_1, S_G)$  for blocks world with *n* blocks







# B3.4 Summary

route planning in Romania:

missionaries and cannibals:

traditional example problem in AI

blocks world:

small example of explicitly representable state space

number of states explodes quickly as n grows

traditional brain teaser with small state space (32 states, of which many unreachable)

▶ family of tasks where *n* blocks on a table must be rearranged

Summary

# Missionaries and Cannibals Formally

