

# Foundations of Artificial Intelligence

## B2. State-Space Search: Representation of State Spaces

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February 26, 2025 — B2. State-Space Search: Representation of State Spaces

B2.1 Representation of State Spaces

B2.2 Explicit Graphs

B2.3 Declarative Representations

B2.4 Black Box

B2.5 Summary

## State-Space Search: Overview

Chapter overview: state-space search

- ▶ B1–B3. Foundations
  - ▶ B1. State Spaces
  - ▶ B2. Representation of State Spaces
  - ▶ B3. Examples of State Spaces
- ▶ B4–B8. Basic Algorithms
- ▶ B9–B15. Heuristic Algorithms

## B2.1 Representation of State Spaces

## Representation of State Spaces

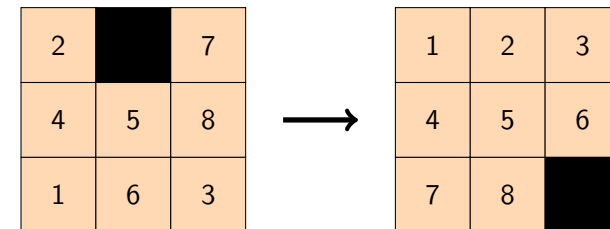
- ▶ practically interesting state spaces are often **huge** ( $10^{10}$ ,  $10^{20}$ ,  $10^{100}$  states)
- ▶ How do we **represent** them, so that we can efficiently deal with them algorithmically?

three main options:

- 1 as **explicit** (directed) graphs
- 2 with **declarative** representations
- 3 as a **black box**

German: explizit, deklarativ, Black Box

## Example: 8-Puzzle



## B2.2 Explicit Graphs

### State Spaces as Explicit Graphs

#### State Spaces as Explicit Graphs

represent state spaces as **explicit directed graphs**:

- ▶ vertices = states
- ▶ directed arcs = transitions

↔ represented as **adjacency list** or **adjacency matrix**

German: Adjazenzliste, Adjazenzmatrix

Example (explicit graph for bounded inc-and-square)

`ai-b02-bounded-inc-and-square.graph`

## State Spaces as Explicit Graphs

### State Spaces as Explicit Graphs

represent state spaces as **explicit directed graphs**:

- ▶ vertices = states
- ▶ directed arcs = transitions

↪ represented as **adjacency list** or **adjacency matrix**

German: Adjazenliste, Adjazenzmatrix

### Example (explicit graph for 8-puzzle)

`ai-b02-puzzle8.graph`

## State Spaces as Explicit Graphs: Discussion

discussion:

- ▶ **impossible** for **large** state spaces (too much space required)
- ▶ if spaces small enough for explicit representations, solutions easy to compute: **Dijkstra's algorithm**  
 $O(|S| \log |S| + |T|)$
- ▶ interesting for time-critical **all-pairs-shortest-path** queries  
(examples: route planning, path planning in video games)

## B2.3 Declarative Representations

## State Spaces with Declarative Representations

### State Spaces with Declarative Representations

represent state spaces **declaratively**:

- ▶ **compact** description of state space as input to algorithms  
↪ state spaces **exponentially larger** than the input
- ▶ algorithms directly operate on compact description
- ↪ allows automatic reasoning about problem:  
reformulation, simplification, abstraction, etc.

### Example (declarative representation for 8-puzzle)

`puzzle8-domain.pddl + puzzle8-problem.pddl`

## B2.4 Black Box

## State Spaces as Black Boxes

### State Spaces as Black Boxes

Define an **abstract interface** for state spaces.

For state space  $S = \langle S, A, cost, T, s_1, S_G \rangle$

we need these methods:

- ▶ **init()**: generate initial state  
result: state  $s_1$
- ▶ **is\_goal(s)**: test if  $s$  is a goal state  
result: **true** if  $s \in S_G$ ; **false** otherwise
- ▶ **succ(s)**: generate applicable actions and successors of  $s$   
result: sequence of pairs  $\langle a, s' \rangle$  with  $s \xrightarrow{a} s'$
- ▶ **cost(a)**: gives cost of action  $a$   
result:  $cost(a) (\in \mathbb{N}_0)$

**Remark:** we will extend the interface later  
in a small but important way

## State Spaces as Black Boxes: Example and Discussion

### Example (Black Box Representation for 8-Puzzle)

demo: `puzzle8.py`

- ▶ **in the following:** focus on black box model
- ▶ **explicit graphs** only as illustrating examples
- ▶ **near end of semester:** declarative state spaces  
(**classical planning**)

## B2.5 Summary

## Summary

- ▶ state spaces often **huge** ( $> 10^{10}$  states)  
~> **how to represent?**
- ▶ **explicit graphs**: adjacency lists or matrices;  
only suitable for small problems
- ▶ **declaratively**: compact description as input  
to search algorithms
- ▶ **black box**: implement an abstract interface