

Algorithms and Data Structures

B2. Abstract Data Types: Stacks & Queues

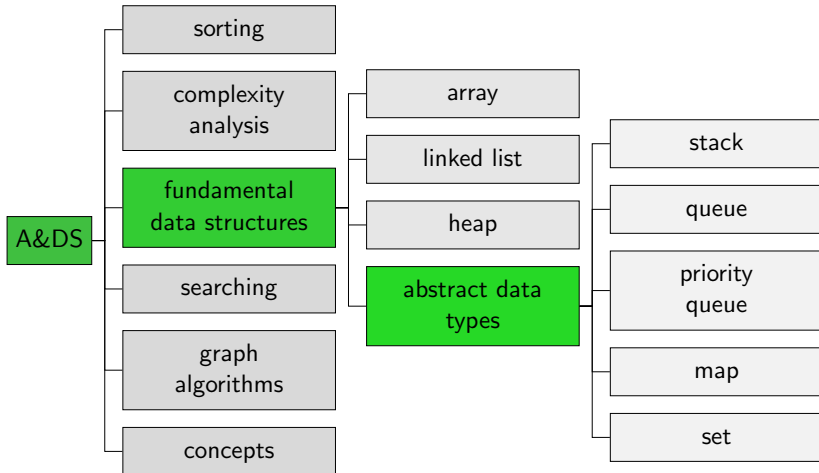
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Abstract Data Type

Content of the Course



Abstract Data Type

Abstract Data Type

Description of a data type, summarizing the possible data and the possible operations on this data.

- **User perspective:** How can I use the data type?
- In contrast to data structures, not specifying the concrete representation of the data.

Advantages of Abstract Data Types

- User codes against an interface.
- The underlying data structure (representation) is hidden/encapsulated.
 - Representation can be replaced at any time.
- Separating two aspects:
 - ① What is the data type doing (interface)?
 - ② How is this achieved (internal structure)?

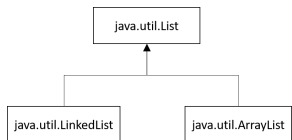
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We can abstract away the dirty details and stay more flexible.

Abstract Data Types and Classes

- In object-oriented languages, abstract data types are often implemented as interfaces.
- For example, lists in Java:



```
interface List<E>:  
    E get(int index);  
    void add(E element);  
    void add(int pos, E element);  
    ...
```

Today: Stacks and Queues



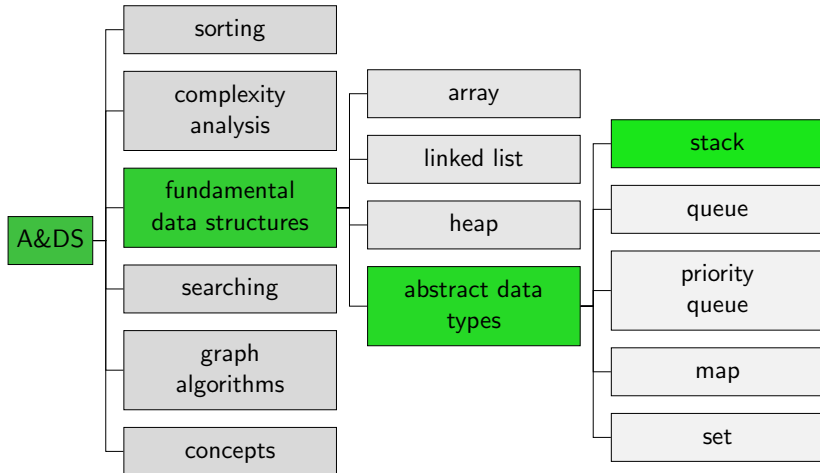
Stack (of plates)



Queue (of persons)

Stack

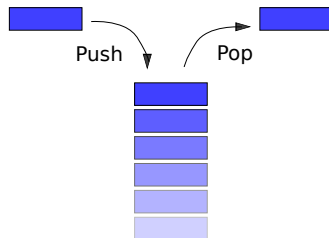
Content of the Course



Stack

A **stack** is a data structure following the **last-in-first-out (LIFO)** principle supporting the following operations:

- **push**: puts an item on top of the stack
- **pop**: removes the item at the top of the stack

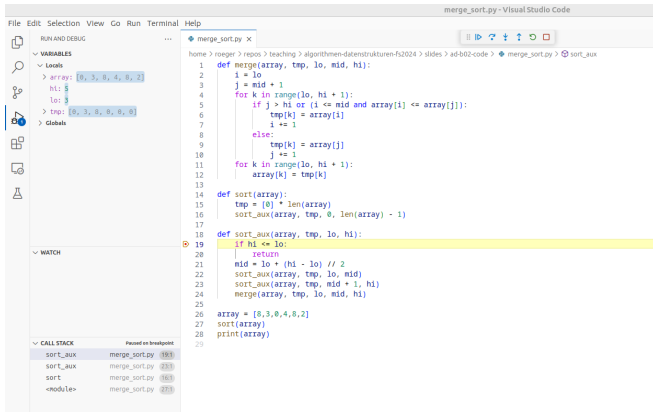


Both operations should take constant time.

Application: Call Stack

The **call stack** stores information when running subroutines of a computer program.

→ where to resume once the subroutine has terminated



The screenshot shows the Visual Studio Code editor with a Python file named `merge_sort.py`. The code implements a merge sort algorithm. The `sort_aux` function is currently active, and the call stack on the left shows the sequence of function calls: `sort_aux` (line 19), `sort_aux` (line 23), `sort` (line 16), and `<module>` (line 27). The `sort` function calls `sort_aux`, which in turn calls `merge`. The `merge` function is also visible in the code editor.

```
merge_sort.py - Visual Studio Code

home > roeger > repos > teaching > algorithmen-datenstrukturen-fs2024 > slides > ad-b02-code > merge_sort.py > sort_aux

1 def merge(array, tmp, lo, mid, hi):
2     i = lo
3     j = mid + 1
4     for k in range(lo, hi + 1):
5         if j > hi or (i <= mid and array[i] <= array[j]):
6             tmp[k] = array[i]
7             i += 1
8         else:
9             tmp[k] = array[j]
10            j += 1
11    for k in range(lo, hi + 1):
12        array[k] = tmp[k]
13
14 def sort(array):
15     tmp = [0] * len(array)
16     sort_aux(array, tmp, 0, len(array) - 1)
17
18 def sort_aux(array, tmp, lo, hi):
19     if hi <= lo:
20         return
21     mid = lo + (hi - lo) // 2
22     sort_aux(array, tmp, lo, mid)
23     sort_aux(array, tmp, mid + 1, hi)
24     merge(array, tmp, lo, mid, hi)
25
26 array = [0, 3, 0, 4, 8, 2]
27 sort(array)
28 print(array)
29
```

VARIABLES

- Locals
 - `array`: [0, 3, 0, 4, 8, 2]
 - `hi`: 5
 - `lo`: 0
 - `tmp`: [0, 3, 0, 4, 8, 8]
- Globals

WATCH

CALL STACK (Paused on breakpoint)

Function	File	Line
sort_aux	merge_sort.py	19:1
sort_aux	merge_sort.py	23:1
sort	merge_sort.py	16:1
<module>	merge_sort.py	27:1

Jupyter Notebook



Jupyter notebook: `fundamental-adts.ipynb`

Stack: Possible Implementation with Doubly Linked Lists

```
class Stack:
    def __init__(self):
        self.list = DoublyLinkedList()

    def push(self, item):
        self.list.prepend(item)

    def pop(self):
        if self.list.is_empty():
            raise Exception("popping from empty stack")
        else:
            return self.list.remove_first()
```

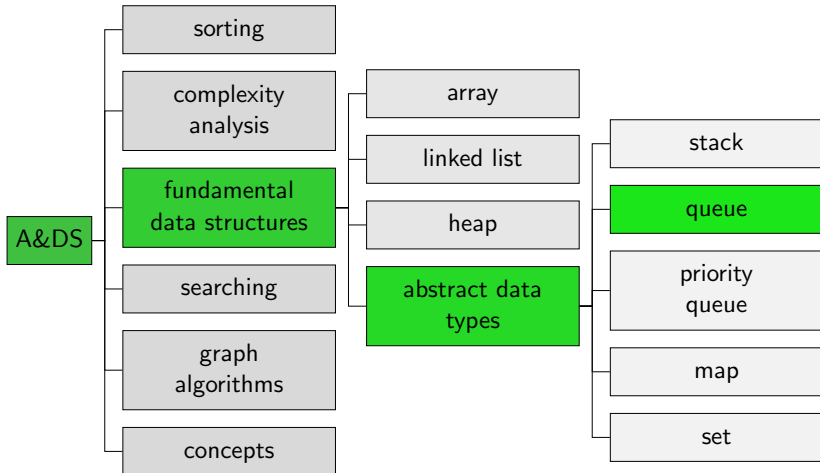
Questions



Questions?

Queue

Content of the Course



Queue

A **queue** is a data structure following the **first-in-first-out (FIFO)** principle supporting the following operations:

- **enqueue**: adds an item to the tail of the queue
- **dequeue**: removes the item at the head of the queue



Both operations should take constant time.

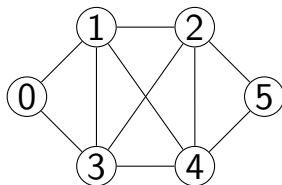
Application: Breadth-first Exploration

Queues are always helpful if we need to store elements and process them in the same order.

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With a breadth-first exploration, we want to visit all reachable nodes in a graph in the order of their distance from a given start node.



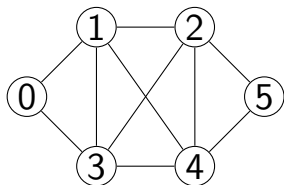
Starting from node 5, any of the following visitation orders would be fine:

- 5 2 4 1 3 0
- 5 4 2 1 3 0
- 5 2 4 3 1 0
- 5 4 2 3 1 0

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Implementation with queue in Jupyter notebook

Jupyter Notebook



Jupyter notebook: `fundamental-adts.ipynb`

Queue: Possible Implementation with Doubly Linked Lists

```
class Queue:
    def __init__(self):
        self.list = DoublyLinkedList()

    def enqueue(self, item):
        self.list.append(item)

    def dequeue(self):
        if self.list.is_empty():
            raise Exception("dequeuing from empty queue")
        else:
            return self.list.remove_first()
```

Questions



Questions?

Deque

Dequeues

A **double-ended queue** (deque) generalizes both, queues and stacks:

- **append**: adds an item to the right side of the deque.
- **appendleft**: adds an item to the left side of the deque.
- **pop**: removes the item at the right end of the deque.
- **popleft**: removes the item at the left end of the deque.

Operation names can differ between programming languages.

All operations should take constant time.

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How would you implement a deque?

Summary

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- **Deque**: generalizes stack and queue.
- All: in principle just lists with limited functionality.
- Limitations help clarifying intended usage and avoiding mistakes.

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- **Abstract data types** (ADTs) specify the **behavior** of a data type, not the internal representation.
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- **Deque**: generalizes stack and queue.
- All: in principle just lists with limited functionality.
- Limitations help clarifying intended usage and avoiding mistakes.

→ Preferably code against an ADT/interface.