Foundations of Artificial Intelligence F5. Automated Planning: Abstraction

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May 8, 2024

Automated Planning: Overview

Chapter overview: automated planning

- F1. Introduction
- F2. Planning Formalisms
- F3. Delete Relaxation
- F4. Delete Relaxation Heuristics
- F5. Abstraction
- F6. Abstraction Heuristics

Planning Heuristics

We consider two basic ideas for general heuristics:

- Delete Relaxation
- ◆ Abstraction → this chapter

Planning Heuristics

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- Abstraction → this chapter

Abstraction: Idea

Estimate solution costs by considering a smaller planning task.



 SAS^+

SAS⁺ Encoding

- in this chapter: SAS⁺ encoding instead of STRIPS (see Chapter F2)
- difference: state variables v not binary, but with finite domain dom(v)
- accordingly, preconditions, effects, goals specified as partial assignments
- everything else equal to STRIPS

(In practice, planning systems convert automatically between STRIPS and SAS⁺.)

SAS⁺ Planning Task

Definition (SAS⁺ planning task)

A SAS⁺ planning task is a 5-tuple $\Pi = \langle V, \text{dom}, I, G, A \rangle$ with the following components:

- V: finite set of state variables
- dom: domain; dom(v) finite and non-empty for all $v \in V$
 - states: total assignments for V according to dom
- *I*: the initial state (state = total assignment)
- G: goals (partial assignment)
- A: finite set of actions a with
 - pre(a): its preconditions (partial assignment)
 - eff(a): its effects (partial assignment)
 - $cost(a) \in \mathbb{N}_0$: its cost

German: SAS⁺-Planungsaufgabe

State Space of SAS⁺ Planning Task

Definition (state space induced by SAS⁺ planning task)

Let $\Pi = \langle V, dom, I, G, A \rangle$ be a SAS⁺ planning task.

Then Π induces the state space $S(\Pi) = \langle S, A, cost, T, s_1, S_G \rangle$:

- set of states: total assignments of V according to dom
- actions: actions A defined as in Π
- action costs: cost as defined in Π
- transitions: $s \xrightarrow{a} s'$ for states s, s' and action a iff
 - pre(a) agrees with s (precondition satisfied)
 - s' agrees with eff(a) for all variables mentioned in eff; agrees with s for all other variables (effects are applied)
- initial state: $s_l = I$
- goal states: $s \in S_G$ for state s iff G agrees with s

German: durch SAS+-Planungsaufgabe induzierter Zustandsraum

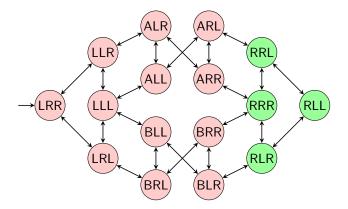
Example: Logistics Task with One Package, Two Trucks

Example (one package, two trucks)

Consider the SAS⁺ planning task $\langle V, dom, I, G, A \rangle$ with:

- $V = \{p, t_A, t_B\}$
- $dom(p) = \{L, R, A, B\}$ and $dom(t_A) = dom(t_B) = \{L, R\}$
- $I = \{p \mapsto L, t_A \mapsto R, t_B \mapsto R\}$
- $G = \{p \mapsto R\}$
- $A = \{load_{i,j} \mid i \in \{A, B\}, j \in \{L, R\}\}$ $\cup \{unload_{i,j} \mid i \in \{A, B\}, j \in \{L, R\}\}$ $\cup \{move_{i,j,j'} \mid i \in \{A, B\}, j, j' \in \{L, R\}, j \neq j'\}$ with:
 - load_{i,j} has preconditions $\{t_i \mapsto j, p \mapsto j\}$, effects $\{p \mapsto i\}$
 - $unload_{i,j}$ has preconditions $\{t_i \mapsto j, p \mapsto i\}$, effects $\{p \mapsto j\}$
 - $move_{i,j,j'}$ has preconditions $\{t_i \mapsto j\}$, effects $\{t_i \mapsto j'\}$
 - All actions have cost 1.

State Space for Example Task



- state $\{p \mapsto i, t_A \mapsto j, t_B \mapsto k\}$ denoted as *ijk*
- annotations of edges not shown for simplicity
- for example, edge from LLL to ALL has annotation loadA,L

Abstractions

State Space Abstraction

State space abstractions drop distinctions between certain states, but preserve the state space behavior as well as possible.

- An abstraction of a state space S is defined by an abstraction function α that determines which states can be distinguished in the abstraction.
- Based on S and α , we compute the abstract state space S^{α} which is "similar" to S but smaller.
- ullet main idea: use optimal solution cost in \mathcal{S}^{lpha} as heuristic

German: Abstraktionsfunktion, abstrakter Zustandsraum

Induced Abstraction

Definition (induced abstraction)

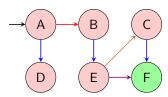
Let $S = \langle S, A, cost, T, s_l, S_G \rangle$ be a state space, and let $\alpha : S \to S'$ be a surjective function.

The abstraction of S induced by α , denoted as S^{α} , is the state space $S^{\alpha} = \langle S', A, cost, T', s'_1, S'_G \rangle$ with:

- $T' = \{ \langle \alpha(s), a, \alpha(t) \rangle \mid \langle s, a, t \rangle \in T \}$
- $s'_{l} = \alpha(s_{l})$
- $S'_{G} = \{ \alpha(s) \mid s \in S_{G} \}$

German: induzierte Abstraktion

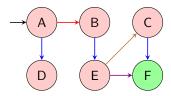
concrete state space with states $S = \{A, B, C, D, E, F\}$



abstraction function $\alpha: \mathcal{S} \to \mathcal{S}^{\alpha}$

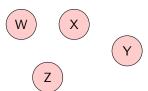
$$\alpha(A) = W$$
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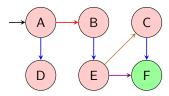


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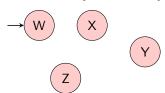


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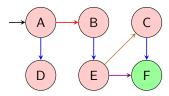


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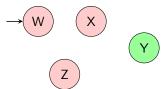


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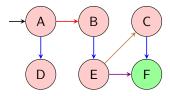


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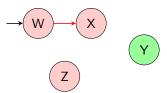


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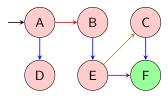


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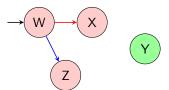


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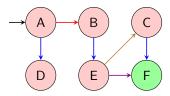


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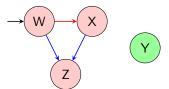


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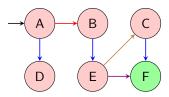


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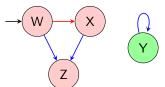


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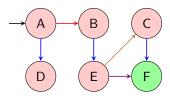


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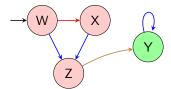


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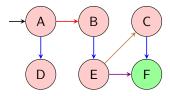


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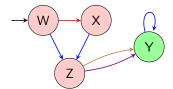


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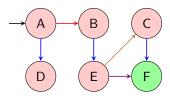


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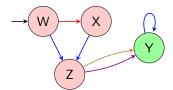
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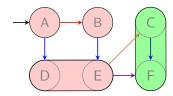
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abstract state space with states $S^{\alpha} = \{W, X, Y, Z\}$



intuition: grouping states



Summary

Summary

- basic idea of abstractions: simplify state space by considering a smaller version
- formally: abstraction function α maps states to abstract states and thus defines which states can be distinguished by the resulting abstraction
- induces abstract state space