Foundations of Artificial Intelligence

B4. State-Space Search: Data Structures for Search Algorithms

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State-Space Search: Overview

Chapter overview: state-space search

- B1–B3. Foundations
- B4-B8. Basic Algorithms
 - B4. Data Structures for Search Algorithms
 - B5. Tree Search and Graph Search
 - B6. Breadth-first Search
 - B7. Uniform Cost Search
 - B8. Depth-first Search and Iterative Deepening
- B9-B15. Heuristic Algorithms

Introduction

Finding Solutions in State Spaces



How can we systematically find a solution?

Search Algorithms

- We now move to search algorithms.
- As everywhere in computer science, suitable data structures are a key to good performance.
- Well-implemented search algorithms process up to ~30,000,000 states/second on a single CPU core.
 - → bonus materials (Burns et al. paper)

this chapter: some fundamental data structures for search

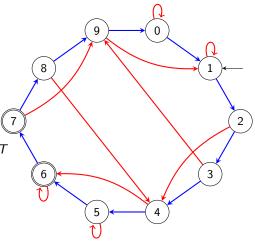
Preview: Search Algorithms

- next chapter: we introduce search algorithms
- now: short preview to motivate data structures for search

bounded inc-and-square:

•
$$S = \{0, 1, \dots, 9\}$$

- $A = \{inc, sqr\}$
- cost(inc) = cost(sqr) = 1
- T s.t. for i = 0, ..., 9:
 - $\langle i, inc, (i+1) \mod 10 \rangle \in T$
 - $\langle i, sqr, i^2 \mod 10 \rangle \in T$
- $s_l = 1$
- $S_G = \{6, 7\}$



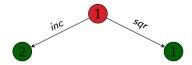
iteratively create a search tree:

• starting with the initial state,



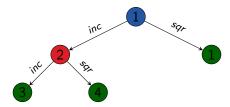
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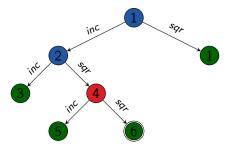
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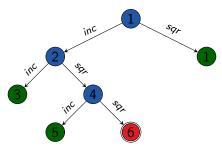
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iteratively create a search tree:

- starting with the initial state,
- repeatedly expand a state by generating its successors (which state depends on the used search algorithm)
- stop when a goal state is expanded (sometimes: generated)
- or all reachable states have been considered



Fundamental Data Structures for Search

We consider three abstract data structures for search:

- search node: stores a state that has been reached, how it was reached, and at which cost
 - → nodes of the example search tree
- open list: efficiently organizes leaves of search tree
 - → set of leaves of example search tree
- closed list: remembers expanded states to avoid duplicated expansions of the same state
 - → inner nodes of a search tree

German: Suchknoten, Open-Liste, Closed-Liste

Not all algorithms use all three data structures, and they are sometimes implicit (e.g., on the CPU stack)

Search Nodes

Search Nodes

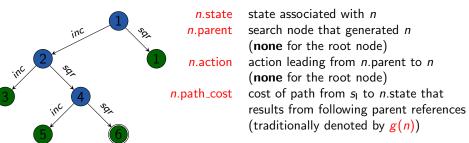
Search Node

A search node (node for short) stores a state that has been reached, how it was reached, and at which cost.

Collectively they form the so-called search tree (Suchbaum).

Data Structure: Search Nodes

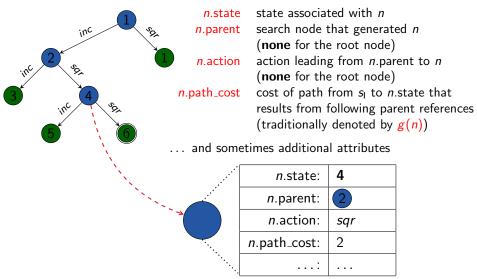
attributes of search node *n*:



... and sometimes additional attributes

Data Structure: Search Nodes

attributes of search node *n*:



Search Nodes (Java Syntax)

```
public interface State {
public interface Action {
public class SearchNode {
    State state;
    SearchNode parent;
    Action action;
    int pathCost;
```

Implementing Search Nodes

- reasonable implementation of search nodes is easy
- advanced aspects:
 - Do we need explicit nodes at all?
 - Can we use lazy evaluation?
 - Should we manually manage memory?
 - Can we compress information?

Operations on Search Nodes: make_root_node

Generate root node of a search tree:

function make_root_node()

 $\textit{node} := \textbf{new} \; \mathsf{SearchNode}$

node.state := init()
node.parent := none

node.action := none node.path_cost := 0

return node

Operations on Search Nodes: make_node

Generate child node of a search node:

function make_node(parent, action, state)

```
node := new SearchNode
```

node.state := state node.parent := parent

node.action := action

 $node.path_cost := parent.path_cost + cost(action)$

return node

Operations on Search Nodes: extract_path

Extract the path to a search node:

```
function extract_path(node)
path := ⟨⟩
while node.parent ≠ none:
    path.append(node.action)
    node := node.parent
path.reverse()
return path
```

Open Lists

Open Lists

Open List

The open list (also: frontier) organizes the leaves of a search tree.

It must support two operations efficiently:

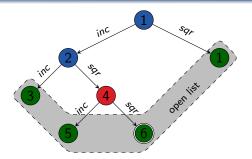
- determine and remove the next node to expand
- insert a new node that is a candidate node for expansion

Remark: despite the name, it is usually a very bad idea to implement open lists as simple lists.

Open Lists: Modify Entries

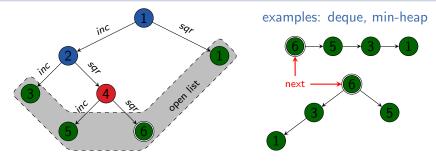
- Some implementations support modifying an open list entry when a shorter path to the corresponding state is found.
- This complicates the implementation.
- → We do not consider such modifications
 and instead use delayed duplicate elimination (→ later).

Interface of Open Lists



- open list open organizes leaves of search tree with the methods:
 - open.is_empty() test if the open list is empty
 open.pop() remove and return the next node to expand
 open.insert(n) insert node n into the open list
- open determines strategy which node to expand next (depends on algorithm)
- underlying data structure choice depends on this strategy

Interface of Open Lists



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Closed Lists

Closed Lists

Closed List

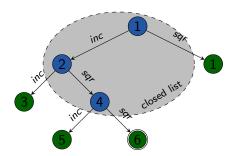
The closed list remembers expanded states to avoid duplicated expansions of the same state.

It must support two operations efficiently:

- insert a node whose state is not yet in the closed list
- test if a node with a given state is in the closed list;
 if yes, return it

Remark: despite the name, it is usually a very bad idea to implement closed lists as simple lists. (Why?)

Interface and Implementation of Closed Lists



- closed list *closed* keeps track of expanded states with the methods:
 - closed.insert(n) insert node n into closed;
 if a node with this state already exists in closed, replace it
 closed.lookup(s) test if a node with state s exists in the closed list;
 if yes, return it; otherwise, return none
- efficient implementation often as hash table with states as keys

Summary

Summary

- search node: represents states reached during search and associated information
- node expansion: generate successor nodes of a node by applying all actions applicable in the state belonging to the node
- open list or frontier:
 set of nodes that are currently candidates for expansion
- closed list: set of already expanded nodes (and their states)