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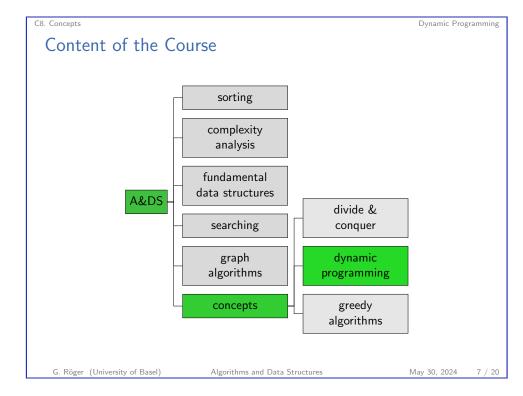
Base case: If the problem is small enough, solve it directly. Recursive case: Otherwise

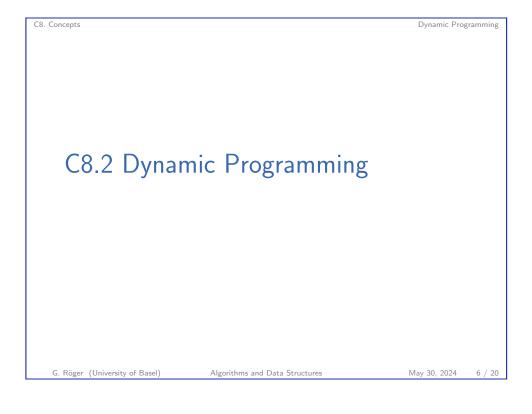
- Divide the problem into disjoint subproblems that are smaller instances of the same problem.
- Conquer the subproblems by solving them recursively.
- Combine the subproblem solutions to form a solution to the original problem.

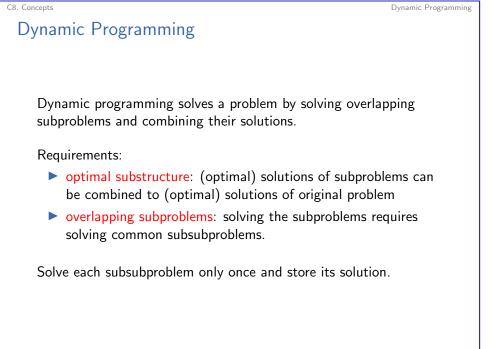
Examples: Strassen's algorithm for multiplying square matrices, merge sort

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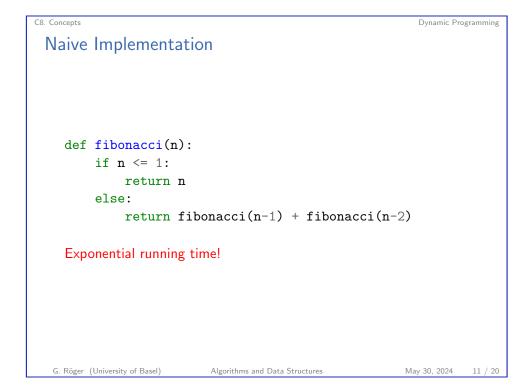
## Two Variants

C8. Concepts

- Top-down: Recursively call the algorithm for subproblems. If there already is a stored solution for the subproblem, use it. Otherwise solve it (recursively) and memoize its solution.
- Bottom-up: Solve the smallest subproblems first and combine their solutions into solutions of larger and larger subproblems.

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## C8. Concepts

## Example: Fibonacci Numbers

The *n*-th Fibonacci number is

$$Fib(n) = \begin{cases} 0 & \text{if } n = 0\\ 1 & \text{if } n = 1\\ Fib(n-1) + Fib(n-2) & \text{otherwise.} \end{cases}$$

We want to compute the *n*-th Fibonacci number.

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C8. Concepts

Dynamic Programming: Top-Down Variant

values = {0 : 0, 1 : 1}

def fibonacci(n):

    if n not in values:

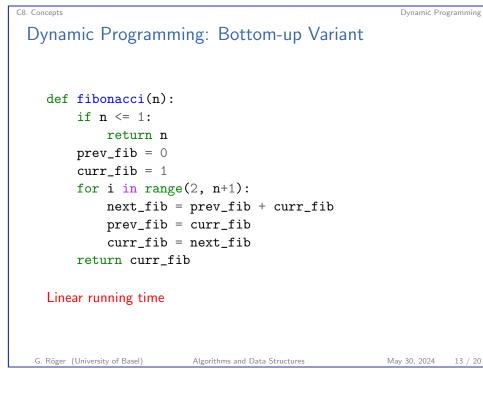
        values[n] = fibonacci(n-1) + fibonacci(n-2)

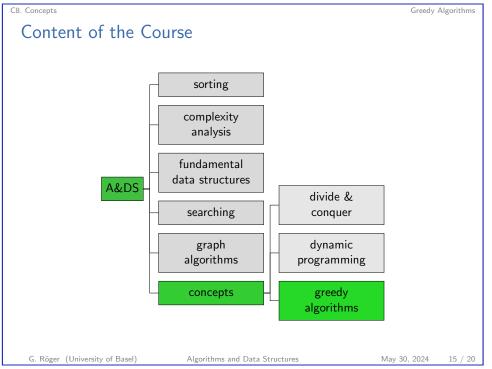
    return values[n]

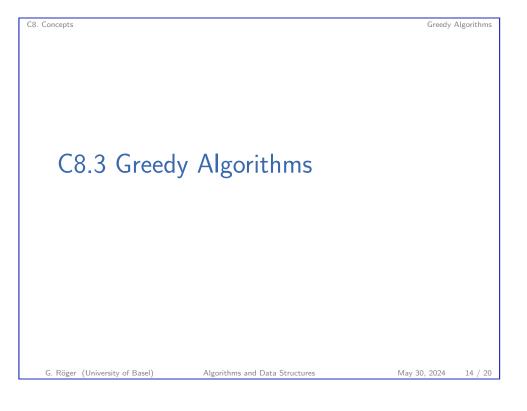
Linear running time
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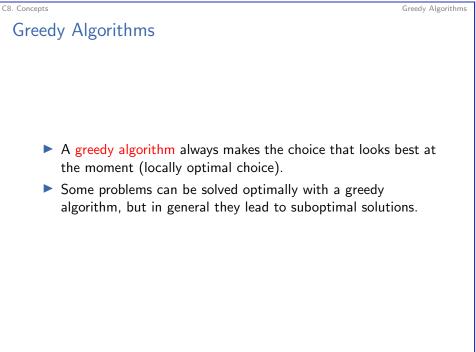
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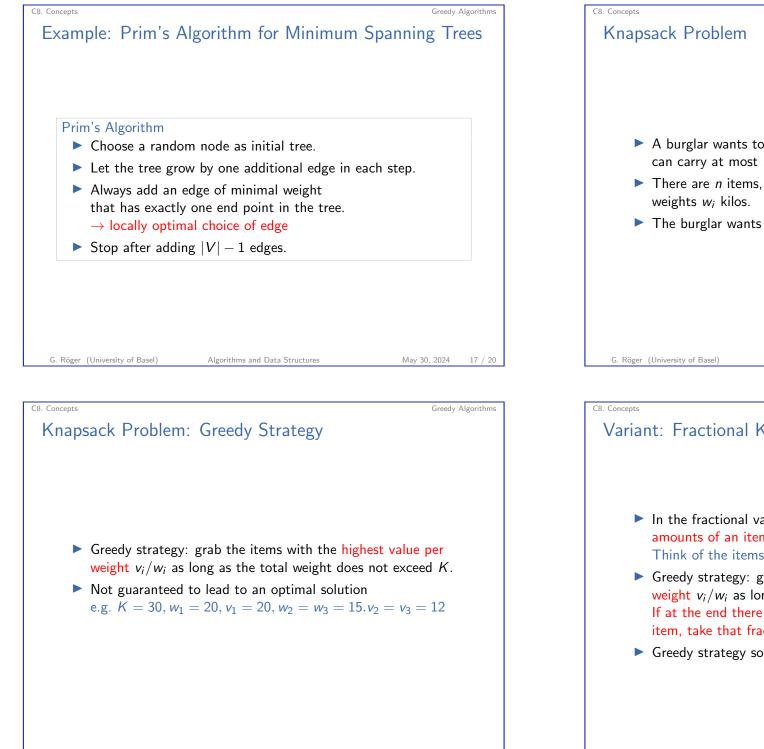


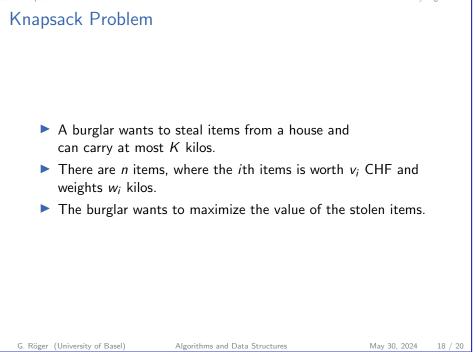




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Greedy Algorithms

