Foundations of Artificial Intelligence

37. Automated Planning: Abstraction

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Automated Planning: Overview

Chapter overview: automated planning

- ► 33. Introduction
- ▶ 34. Planning Formalisms
- ▶ 35.–36. Planning Heuristics: Delete Relaxation
- ▶ 37. Planning Heuristics: Abstraction
- ▶ 38.—39. Planning Heuristics: Landmarks

Planning Heuristics

We consider three basic ideas for general heuristics:

- Delete Relaxation
- ► Abstraction \leadsto this chapter
- ► Landmarks

Abstraction: Idea

Estimate solution costs by considering a smaller planning task.

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37.1 SAS⁺

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SAS⁺ Encoding

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in this chapter: SAS⁺ encoding instead of STRIPS (see Chapter 34)

b difference: state variables v not binary, but with finite domain dom(v)

accordingly, preconditions, effects, goals specified as partial assignments

everything else equal to STRIPS

(In practice, planning systems convert automatically between STRIPS and SAS⁺.)

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SAS⁺ Planning Task

Definition (SAS⁺ planning task)

A SAS⁺ planning task is a 5-tuple $\Pi = \langle V, \text{dom}, I, G, A \rangle$ with the following components:

- V: finite set of state variables
- ightharpoonup dom: domain; dom(v) finite and non-empty for all $v \in V$
 - ▶ states: total assignments for *V* according to dom
- ► I: the initial state (state = total assignment)
- ► G: goals (partial assignment)
- A: finite set of actions a with
 - pre(a): its preconditions (partial assignment)
 - eff(a): its effects (partial assignment)
 - $ightharpoonup cost(a) \in \mathbb{N}_0$: its cost

German: SAS⁺-Planungsaufgabe

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State Space of SAS⁺ Planning Task

Definition (state space induced by SAS⁺ planning task)

Let $\Pi = \langle V, dom, I, G, A \rangle$ be a SAS⁺ planning task. Then Π induces the state space $S(\Pi) = \langle S, A, cost, T, s_0, S_{\star} \rangle$:

- \triangleright set of states: total assignments of V according to dom
- actions: actions A defined as in Π
- \triangleright action costs: cost as defined in \square
- \blacktriangleright transitions: $s \xrightarrow{a} s'$ for states s, s' and action a iff
 - pre(a) complies with s (precondition satisfied)
 - \triangleright s' complies with eff(a) for all variables mentioned in eff; complies with s for all other variables (effects are applied)
- ightharpoonup initial state: $s_0 = I$
- ▶ goal states: $s \in S_{\star}$ for state s iff G complies with s

German: durch SAS⁺-Planungsaufgabe induzierter Zustandsraum

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State Space for Example Task

Example: Logistics Task with One Package, Two Trucks

Example (one package, two trucks)

Consider the SAS⁺ planning task $\langle V, dom, I, G, A \rangle$ with:

- $V = \{p, t_A, t_B\}$
- ightharpoonup dom $(p) = \{L, R, A, B\}$ and dom $(t_A) = dom(t_B) = \{L, R\}$
- $I = \{p \mapsto L, t_A \mapsto R, t_B \mapsto R\} \text{ and } G = \{p \mapsto R\}$
- ► $A = \{load_{i,i} \mid i \in \{A, B\}, j \in \{L, R\}\}$

 - ▶ load_{i,i} has preconditions $\{t_i \mapsto j, p \mapsto j\}$, effects $\{p \mapsto i\}$
 - unload_{i,j} has preconditions $\{t_i \mapsto j, p \mapsto i\}$, effects $\{p \mapsto j\}$

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State Space Abstraction

State space abstractions drop distinctions between certain states. but preserve the state space behavior as well as possible.

 \triangleright for example, edge from LLL to ALL has annotation load_{A I}

▶ state $\{p \mapsto i, t_A \mapsto j, t_B \mapsto k\}$ denoted as *ijk*

annotations of edges not shown for simplicity

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BRR

- \triangleright An abstraction of a state space S is defined by an abstraction function α that determines which states can be distinguished in the abstraction.
- **\triangleright** Based on S and α , we compute the abstract state space S^{α} which is "similar" to S but smaller.

German: Abstraktionsfunktion, abstrakter Zustandsraum

Abstraction Heuristic

Use abstract solution costs (solution costs in S^{α}) as heuristic values for concrete solution costs (solution costs in S). \rightarrow abstraction heuristic h^{α}

German: abstrakte/konkrete Zielabstände, Abstraktionsheuristik

 \cup {unload_{i,i} | $i \in \{A, B\}, j \in \{L, R\}\}$

 $\bigcup \{move_{i,j,j'} \mid i \in \{A,B\}, j,j' \in \{L,R\}, j \neq j'\} \text{ with: }$

- ▶ $move_{i,j,j'}$ has preconditions $\{t_i \mapsto j\}$, effects $\{t_i \mapsto j'\}$
- All actions have cost 1.

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Abstractions

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Induced Abstraction

Definition (induced abstraction)

Let $S = \langle S, A, cost, T, s_0, S_{\star} \rangle$ be a state space, and let $\alpha : S \to S'$ be a surjective function.

The abstraction of S induced by α , denoted as S^{α} , is the state space $S^{\alpha} = \langle S', A, cost, T', s'_0, S'_{\star} \rangle$ with:

- $T' = \{ \langle \alpha(s), a, \alpha(t) \rangle \mid \langle s, a, t \rangle \in T \}$

German: induzierte Abstraktion

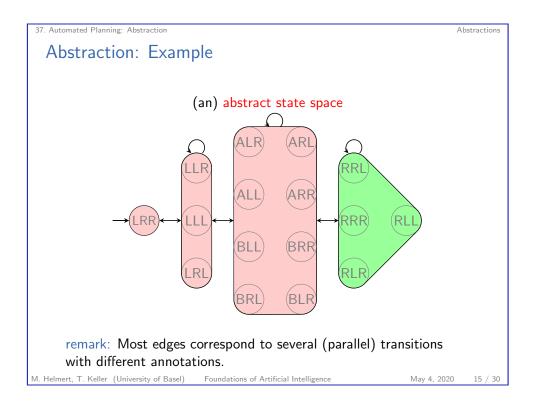
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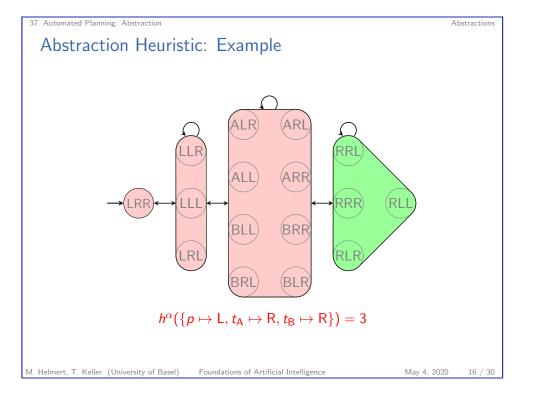
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Abstraction: Example concrete state space LLR ALR ARR RRR RLL BRR RLR M. Helmert, T. Keller (University of Basel) Foundations of Artificial Intelligence Abstractions Abstractions Abstractions Abstractions





Abstraction Heuristics: Discussion

- Every abstraction heuristic is admissible and consistent. (proof idea?)
- ▶ The choice of the abstraction function α is very important.
 - \triangleright Every α yields an admissible and consistent heuristic.
 - ightharpoonup But most α lead to poor heuristics.
- \blacktriangleright An effective α must yield an informative heuristic . . .
- ...as well as being efficiently computable.
- \blacktriangleright How to find a suitable α ?

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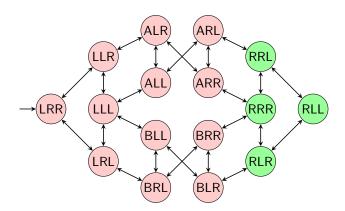
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37. Automated Planning: Abstraction Usually a Bad Idea: Single-State Abstraction one state abstraction: $\alpha(s) := \text{const}$ + compactly representable and α easy to compute very uninformed heuristic

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Usually a Bad Idea: Identity Abstraction



identity abstraction: $\alpha(s) := s$

- + perfect heuristic and α easy to compute
- too many abstract states \rightsquigarrow computation of h^{α} too hard

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Automatic Computation of Suitable Abstractions

Main Problem with Abstraction Heuristics How to find a good abstraction?

Several successful methods:

- ▶ pattern databases (PDBs) → this course (Culberson & Schaeffer, 1996)
- merge-and-shrink abstractions (Dräger, Finkbeiner & Podelski, 2006)
- Cartesian abstractions (Seipp & Helmert, 2013)

German: Musterdatenbanken, Merge-and-Shrink-Abstraktionen, Kartesische Abstraktionen

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37.3 Pattern Databases

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Pattern Databases

Pattern Databases: Background

- The most common abstraction heuristics are pattern database heuristics.
- ▶ originally introduced for the 15-puzzle (Culberson & Schaeffer, 1996) and for Rubik's Cube (Korf, 1997)
- ▶ introduced for automated planning by Edelkamp (2001)
- ▶ for many search problems the best known heuristics
- many many research papers studying
 - theoretical properties
 - efficient implementation and application
 - pattern selection

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Pattern Databases

Pattern Databases

Pattern Databases: Projections

A PDB heuristic for a planning task is an abstraction heuristic where

- ▶ some aspects (= state variables) of the task are preserved with perfect precision while
- ▶ all other aspects are not preserved at all.

formalized as projections; example:

- $ightharpoonup s = \{v_1 \mapsto d_1, v_2 \mapsto d_2, v_3 \mapsto d_3\}$
- ightharpoonup projection on $P = \{v_1\}$ (= ignore v_2, v_3): $\alpha(s) = s|_{P} = \{v_1 \mapsto d_1\}$
- ightharpoonup projection on $P = \{v_1, v_3\}$ (= ignore v_2): $\alpha(s) = s|_P = \{v_1 \mapsto d_1, v_3 \mapsto d_3\}$

German: Projektionen

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Pattern Databases

Pattern Databases: Definition

Definition (pattern database heuristic)

Let P be a subset of the variables of a planning task.

The abstraction heuristic induced by the projection π_P on P is called pattern database heuristic (PDB heuristic) with pattern P.

abbreviated notation: h^P for h^{π_P}

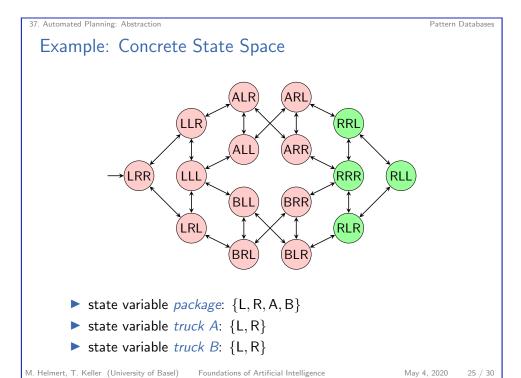
German: Musterdatenbank-Heuristik

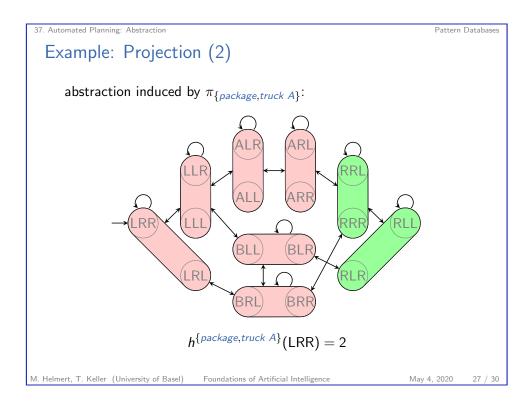
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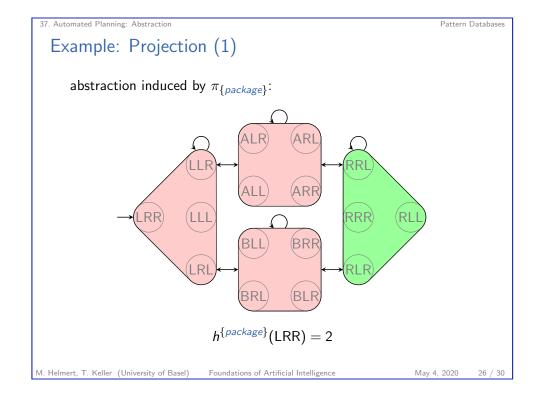
"pattern databases" in analogy to endgame databases (which have been successfully applied in 2-person-games)

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Pattern Databases

Pattern Databases in Practice

practical aspects which we do not discuss in detail:

- ► How to automatically find good patterns?
- ► How to combine multiple PDB heuristics?
- ► How to implement PDB heuristics efficiently?
 - ▶ good implementations efficiently handle abstract state spaces with 10⁷, 10⁸ or more abstract states
 - effort independent of the size of the concrete state space
 - ▶ usually all heuristic values are precomputed
 → space complexity = number of abstract states

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37.4 Summary

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Summary

basic idea of abstraction heuristics: estimate solution cost by considering a smaller planning task.

- \blacktriangleright formally: abstraction function α maps states to abstract states and thus defines which states can be distinguished by the resulting heuristic.
- ▶ induces abstract state space whose solution costs are used as heuristic
- ▶ Pattern database heuristics are abstraction heuristics based on projections onto state variable subsets (patterns): states are distinguishable iff they differ on the pattern.

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