

Foundations of Artificial Intelligence

37. Automated Planning: Abstraction

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Automated Planning: Overview

Chapter overview: automated planning

- ▶ 33. Introduction
- ▶ 34. Planning Formalisms
- ▶ 35.–36. Planning Heuristics: Delete Relaxation
- ▶ 37. Planning Heuristics: Abstraction
- ▶ 38.–39. Planning Heuristics: Landmarks

Planning Heuristics

We consider **three basic ideas** for general heuristics:

- ▶ Delete Relaxation
- ▶ **Abstraction** ↽ this chapter
- ▶ Landmarks

Abstraction: Idea

Estimate solution costs by considering a **smaller** planning task.

37.1 SAS⁺

SAS⁺ Planning Task

Definition (SAS⁺ planning task)

A SAS⁺ planning task is a 5-tuple $\Pi = \langle V, \text{dom}, I, G, A \rangle$ with the following components:

- ▶ V : finite set of **state variables**
- ▶ dom : **domain**; $\text{dom}(v)$ finite and non-empty for all $v \in V$
 - ▶ **states**: **total assignments** for V according to dom
- ▶ I : the **initial state** (state = total assignment)
- ▶ G : **goals** (partial assignment)
- ▶ A : finite set of **actions** a with
 - ▶ $\text{pre}(a)$: its **preconditions** (partial assignment)
 - ▶ $\text{eff}(a)$: its **effects** (partial assignment)
 - ▶ $\text{cost}(a) \in \mathbb{N}_0$: its **cost**

German: SAS⁺-Planungsaufgabe

SAS⁺ Encoding

- ▶ in this and the next chapter: SAS⁺ encoding instead of STRIPS (see Chapter 34)
- ▶ difference: state variables v not binary, but with **finite domain** $\text{dom}(v)$
- ▶ accordingly, preconditions, effects, goals specified as **partial assignments**
- ▶ everything else equal to STRIPS

(In practice, planning systems convert automatically between STRIPS and SAS⁺.)

State Space of SAS⁺ Planning Task

Definition (state space induced by SAS⁺ planning task)

Let $\Pi = \langle V, \text{dom}, I, G, A \rangle$ be a SAS⁺ planning task.

Then Π induces the **state space** $\mathcal{S}(\Pi) = \langle S, A, \text{cost}, T, s_0, S_* \rangle$:

- ▶ **set of states**: total assignments of V according to dom
- ▶ **actions**: actions A defined as in Π
- ▶ **action costs**: cost as defined in Π
- ▶ **transitions**: $s \xrightarrow{a} s'$ for states s, s' and action a iff
 - ▶ $\text{pre}(a)$ complies with s (precondition satisfied)
 - ▶ s' complies with $\text{eff}(a)$ for all variables mentioned in eff , complies with s for all other variables (effects are applied)
- ▶ **initial state**: $s_0 = I$
- ▶ **goal states**: $s \in S_*$ for state s iff G complies with s

German: durch SAS⁺-Planungsaufgabe induzierter Zustandsraum

Example: Logistics Task with One Package, Two Trucks

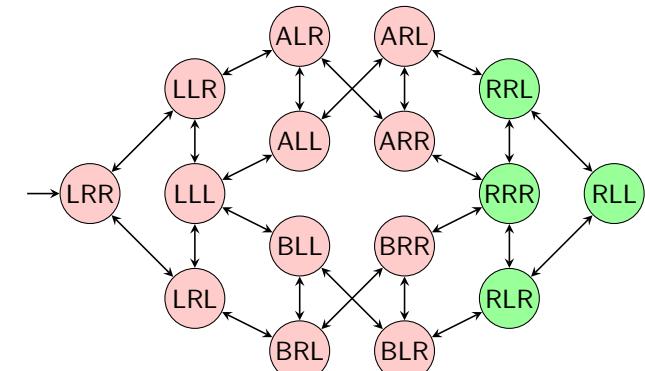
Example (one package, two trucks)

Consider the SAS⁺ planning task $\langle V, \text{dom}, I, G, A \rangle$ with:

- ▶ $V = \{p, t_A, t_B\}$
- ▶ $\text{dom}(p) = \{L, R, A, B\}$ and $\text{dom}(t_A) = \text{dom}(t_B) = \{L, R\}$
- ▶ $I = \{p \mapsto L, t_A \mapsto R, t_B \mapsto R\}$ and $G = \{p \mapsto R\}$
- ▶ $A = \{\text{pickup}_{i,j} \mid i \in \{A, B\}, j \in \{L, R\}\}$
 $\cup \{\text{drop}_{i,j} \mid i \in \{A, B\}, j \in \{L, R\}\}$
 $\cup \{\text{move}_{i,j,j'} \mid i \in \{A, B\}, j, j' \in \{L, R\}, j \neq j'\}$ with:
 - ▶ $\text{pickup}_{i,j}$ has preconditions $\{t_i \mapsto j, p \mapsto j\}$, effects $\{p \mapsto i\}$
 - ▶ $\text{drop}_{i,j}$ has preconditions $\{t_i \mapsto j, p \mapsto i\}$, effects $\{p \mapsto j\}$
 - ▶ $\text{move}_{i,j,j'}$ has preconditions $\{t_i \mapsto j\}$, effects $\{t_i \mapsto j'\}$
 - ▶ All actions have cost 1.

pickup corresponds to load, and drop to unload from Chapter 35
(renamed to avoid confusion in the following abbreviations)

State Space for Example Task



- ▶ state $\{p \mapsto i, t_A \mapsto j, t_B \mapsto k\}$ denoted as ijk
- ▶ annotations of edges not shown for simplicity
- ▶ for example, edge from LLL to ALL has annotation $\text{pickup}_{A,L}$

37.2 Abstractions

State Space Abstraction

State space abstractions drop distinctions between certain states, but preserve the state space behavior as well as possible.

- ▶ An abstraction of a state space \mathcal{S} is defined by an abstraction function α that determines which states can be distinguished in the abstraction.
- ▶ Based on \mathcal{S} and α , we compute the abstract state space \mathcal{S}^α which is “similar” to \mathcal{S} but smaller.

German: Abstraktionsfunktion, abstrakter Zustandsraum

Abstraction Heuristic

Use abstract solution costs (solution costs in \mathcal{S}^α) as heuristic values for concrete solution costs (solution costs in \mathcal{S}).
 \rightsquigarrow abstraction heuristic h^α

German: abstrakte/konkrete Zielabstände, Abstraktionsheuristik

Induced Abstraction

Definition (induced abstraction)

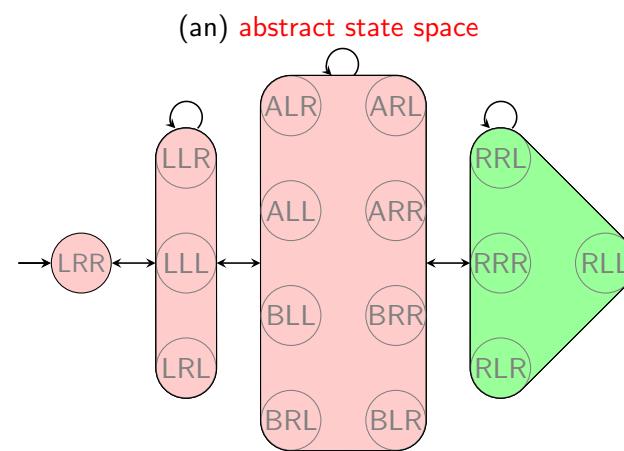
Let $\mathcal{S} = \langle S, A, \text{cost}, T, s_0, S_* \rangle$ be a state space, and let $\alpha : S \rightarrow S'$ be a surjective function.

The **abstraction of \mathcal{S} induced by α** , denoted as \mathcal{S}^α , is the state space $\mathcal{S}^\alpha = \langle S', A, \text{cost}, T', s'_0, S'_* \rangle$ with:

- ▶ $T' = \{\langle \alpha(s), a, \alpha(t) \rangle \mid \langle s, a, t \rangle \in T\}$
- ▶ $s'_0 = \alpha(s_0)$
- ▶ $S'_* = \{\alpha(s) \mid s \in S_*\}$

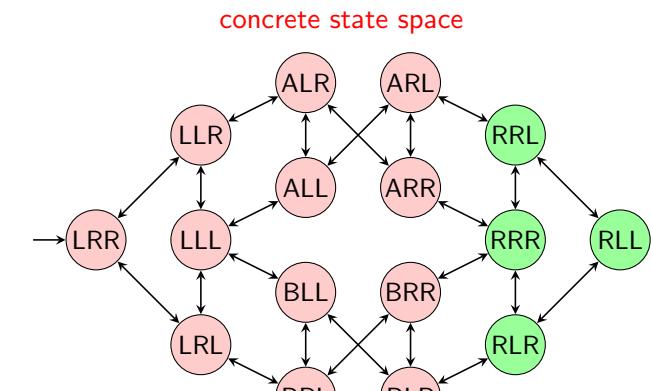
German: induzierte Abstraktion

Abstraction: Example

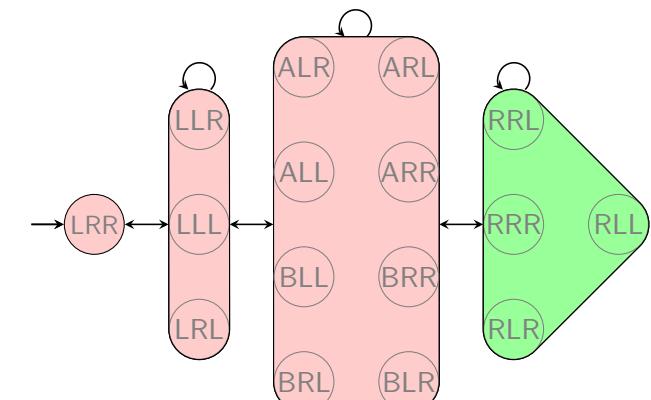


remark: Most edges correspond to several (parallel) transitions with different annotations.

Abstraction: Example



Abstraction Heuristic: Example

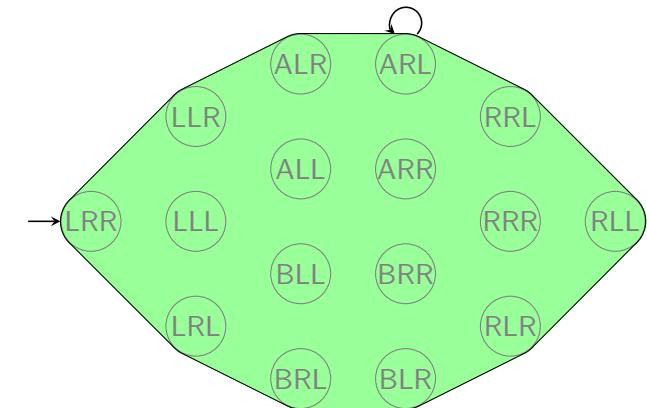


$$h^\alpha(\{p \mapsto L, t_A \mapsto R, t_B \mapsto R\}) = 3$$

Abstraction Heuristics: Discussion

- ▶ Every abstraction heuristic is **admissible** and **consistent**.
(**proof idea?**)
- ▶ The choice of the **abstraction function α** is very important.
 - ▶ **Every α** yields an admissible and consistent heuristic.
 - ▶ But most α lead to poor heuristics.
- ▶ An effective α must yield an **informative heuristic** ...
- ▶ ... as well as being **efficiently computable**.
- ▶ **How to find a suitable α ?**

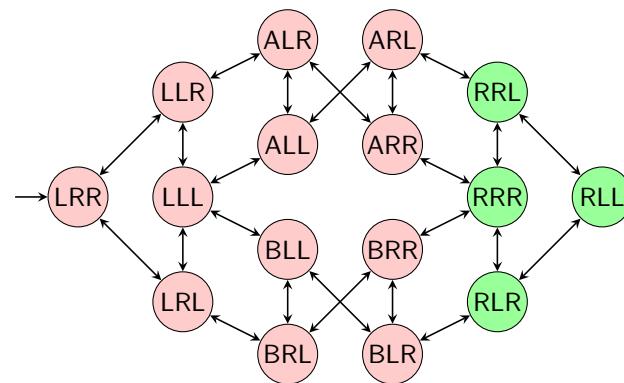
Usually a Bad Idea: Single-State Abstraction



one state abstraction: $\alpha(s) := \text{const}$

- + compactly representable and α easy to compute
- very uninformed heuristic

Usually a Bad Idea: Identity Abstraction



identity abstraction: $\alpha(s) := s$

- + perfect heuristic and α easy to compute
- too many abstract states \rightsquigarrow computation of h^α too hard

Automatic Computation of Suitable Abstractions

Main Problem with Abstraction Heuristics

How to find a good abstraction?

Several successful methods:

- ▶ **pattern databases (PDBs)** \rightsquigarrow this course
(Culberson & Schaeffer, 1996)
- ▶ **merge-and-shrink** abstractions
(Dräger, Finkbeiner & Podolski, 2006)
- ▶ **Cartesian** abstractions
(Seipp & Helmert, 2013)

German: Musterdatenbanken, Merge-and-Shrink-Abstraktionen,
Kartesische Abstraktionen

37.3 Pattern Databases

Pattern Databases: Projections

A PDB heuristic for a planning task is an abstraction heuristic where

- ▶ some aspects (= state variables) of the task are preserved **with perfect precision** while
- ▶ all other aspects are not preserved **at all**.

formalized as **projections**; example:

- ▶ $s = \{v_1 \mapsto d_1, v_2 \mapsto d_2, v_3 \mapsto d_3\}$
- ▶ **projection on $P = \{v_1\}$** (= ignore v_2, v_3):
 $\alpha(s) = s|_P = \{v_1 \mapsto d_1\}$
- ▶ **projection on $P = \{v_1, v_3\}$** (= ignore v_2):
 $\alpha(s) = s|_P = \{v_1 \mapsto d_1, v_3 \mapsto d_3\}$

German: Projektionen

Pattern Databases: Background

- ▶ The most common abstraction heuristics are **pattern database heuristics**.
- ▶ originally introduced for the **15-puzzle** (Culberson & Schaeffer, 1996) and for **Rubik's Cube** (Korf, 1997)
- ▶ introduced for **automated planning** by Edelkamp (2001)
- ▶ for many search problems the **best known** heuristics
- ▶ many many research papers studying
 - ▶ theoretical properties
 - ▶ efficient implementation and application
 - ▶ pattern selection
 - ▶ ...

Pattern Databases: Definition

Definition (pattern database heuristic)

Let P be a subset of the variables of a planning task.

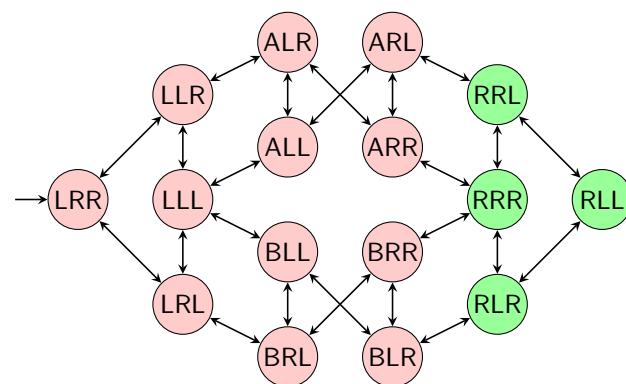
The abstraction heuristic induced by the **projection π_P** on P is called **pattern database heuristic (PDB heuristic)** with **pattern P** .
abbreviated notation: h^P for h^{π_P}

German: Musterdatenbank-Heuristik

remark:

- ▶ “pattern databases” in analogy to **endgame databases** (which have been successfully applied in 2-person-games)

Example: Concrete State Space

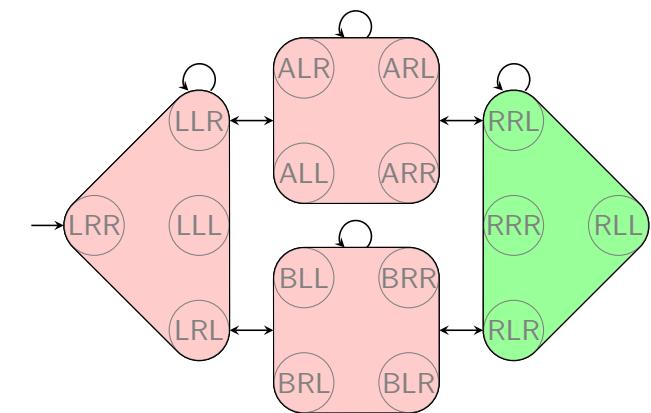


- ▶ state variable *package*: {L, R, A, B}
- ▶ state variable *truck A*: {L, R}
- ▶ state variable *truck B*: {L, R}

Example: Projection (1)

Example: Projection (1)

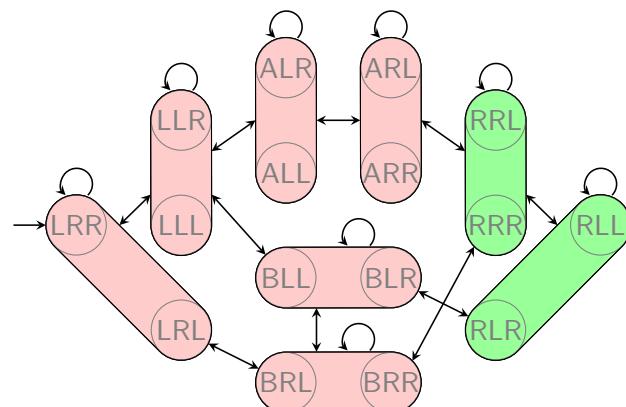
abstraction induced by $\pi_{\{\text{package}\}}$:



$$h^{\{\text{package}\}}(\text{LRR}) = 2$$

Example: Projection (2)

abstraction induced by $\pi_{\{\text{package}, \text{truck A}\}}$:



$$h^{\{\text{package}, \text{truck A}\}}(\text{LRR}) = 2$$

Pattern Databases in Practice

practical aspects which we do not discuss in detail:

- ▶ How to automatically find **good patterns**?
- ▶ How to combine **multiple** PDB heuristics?
- ▶ How to **implement** PDB heuristics efficiently?
 - ▶ good implementations efficiently handle **abstract** state spaces with 10^7 , 10^8 or more abstract states
 - ▶ effort independent of the size of the **concrete** state space
 - ▶ usually all heuristic values are precomputed
~~ space complexity = number of abstract states

37.4 Summary

Summary

- ▶ basic idea of **abstraction heuristics**: estimate solution cost by considering a **smaller** planning task.
- ▶ formally: **abstraction function** α maps states to **abstract states** and thus defines which states can be distinguished by the resulting heuristic.
- ▶ induces **abstract state space** whose solution costs are used as heuristic
- ▶ **Pattern database heuristics** are abstraction heuristics based on **projections** onto state variable subsets (**patterns**): states are distinguishable iff they differ on the pattern.