



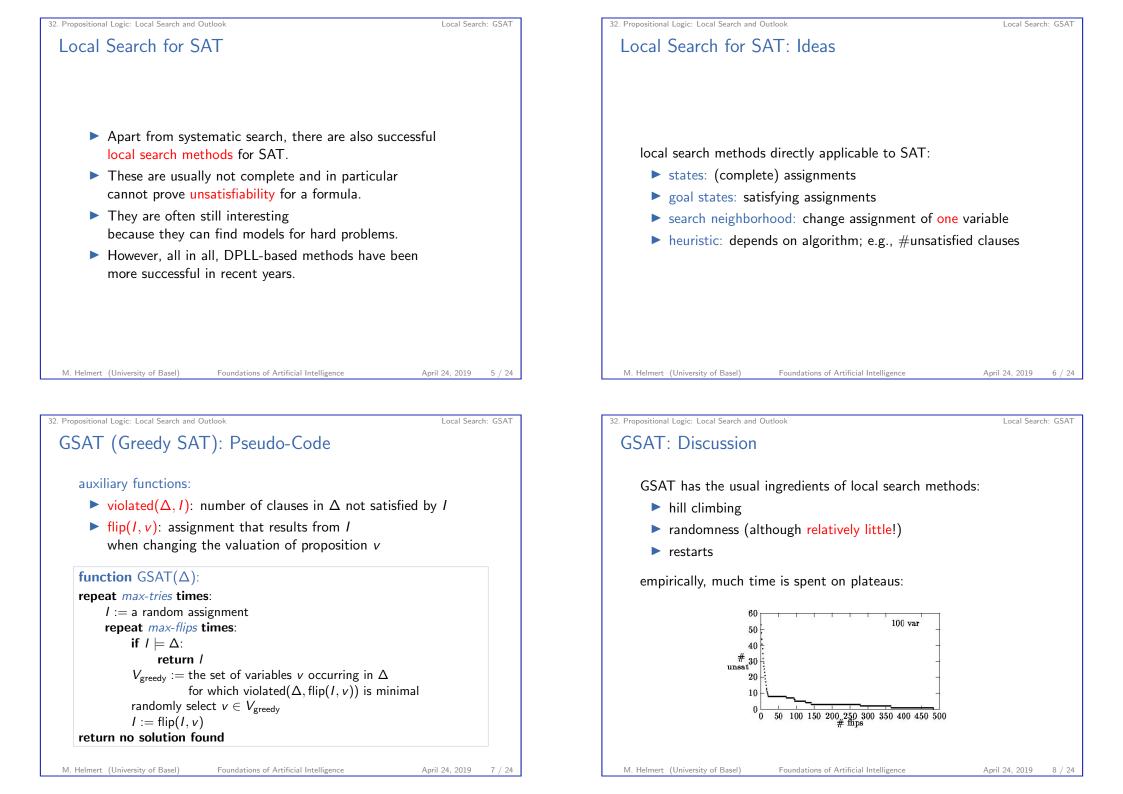
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32. Propositional Logic: Local Search and Outlook

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Local Search: GSAT

32.1 Local Search: GSAT



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Local Search: Walksat

32.2 Local Search: Walksat

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32. Propositional Logic: Local Search and Outlook

Walksat vs. GSAT

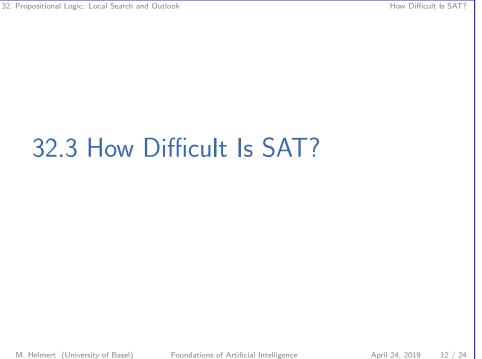
Comparison GSAT vs. Walksat:

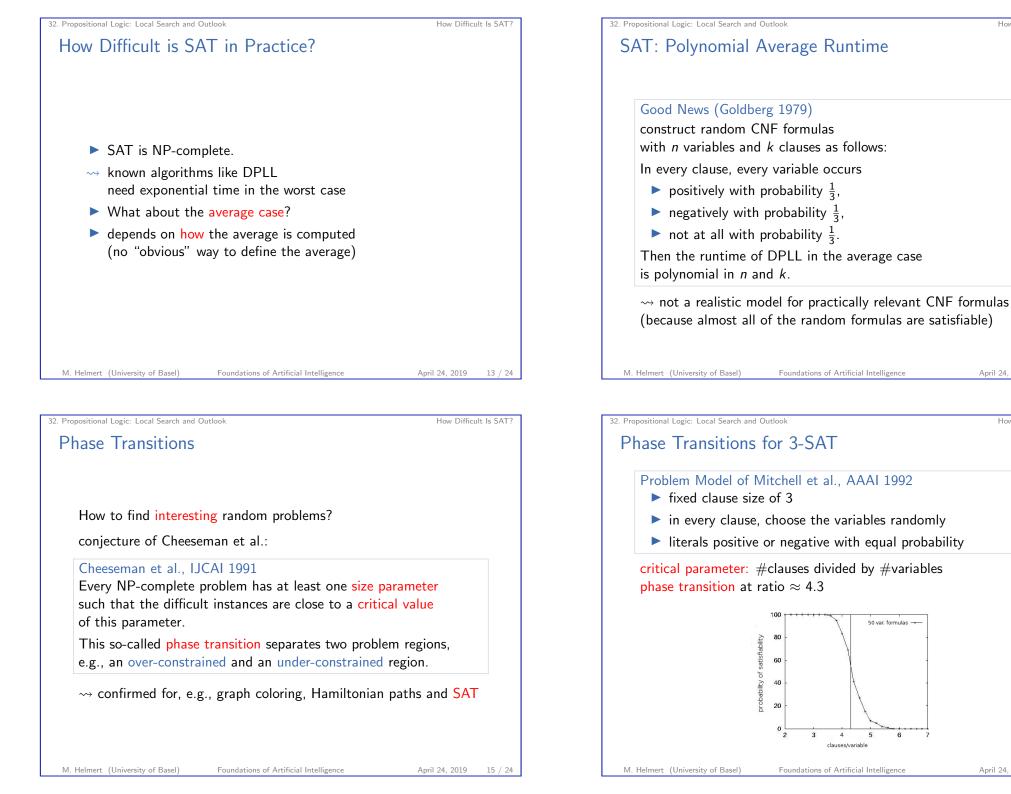
- much more randomness in Walksat because of random choice of considered clause
- "counter-intuitive" steps that temporarily increase the number of unsatisfied clauses are possible in Walksat
- → smaller risk of getting stuck in local minima

Walksat: Pseudo-Code

lost(Δ , I, v): #clauses in Δ satisfied by I, but not by flip(I, v)

function Walksat(Δ):		
repeat max-tries tim	ies:		
I := a random a	ssignment		
repeat max-flip	s times:		
if $I \models \Delta$:			
return	1		
C := rando	mly chosen unsatisfied clause in Δ		
if there is a	a variable v in C with lost(Δ , I, v) =	0:	
V_{choice}	$_{\rm s} :=$ all such variables in C		
else with p	robability p _{noise} :		
V_{choice}	$_{s} := $ all variables occurring in C		
else:			
$V_{\rm choice}$	s := variables v in C that minimize lo	$ost(\Delta, I, v)$	
randomly se	elect $v \in V_{\text{choices}}$		
I := flip(I)	v)		
return no solution	,		
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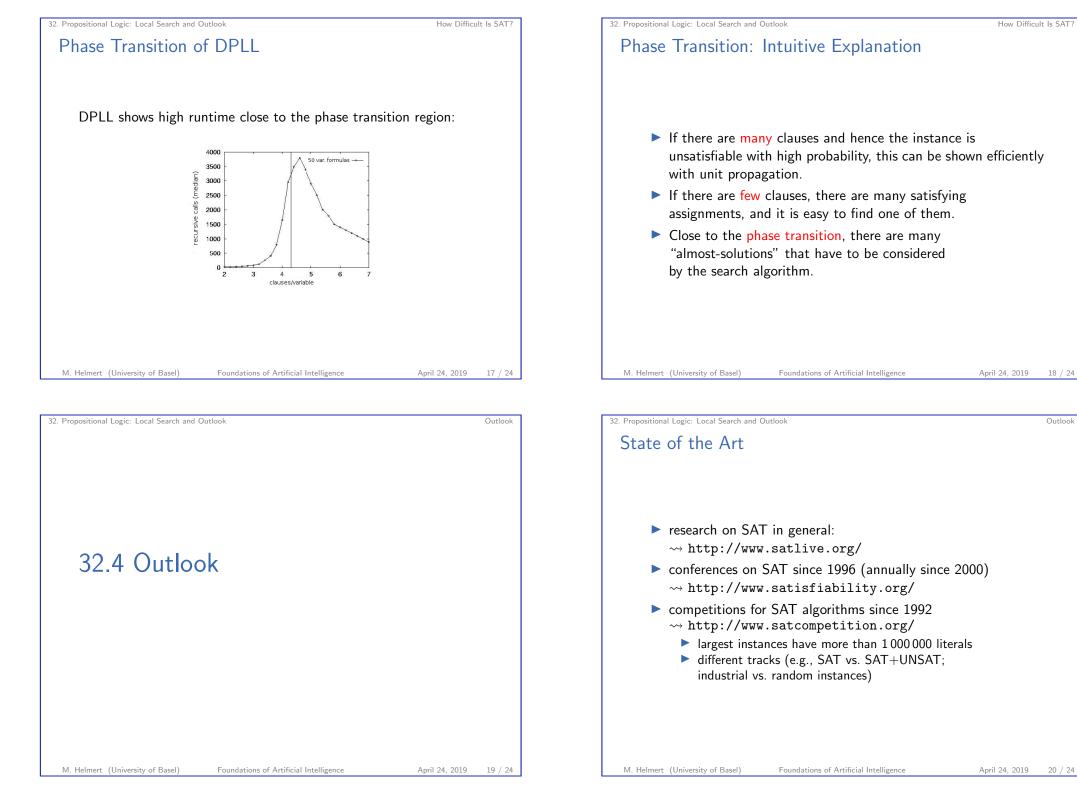


How Difficult Is SAT?

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How Difficult Is SAT?





More Advanced Topics

DPLL-based SAT algorithms:

- efficient implementation techniques
- accurate variable orders
- clause learning

local search algorithms:

- efficient implementation techniques
- adaptive search methods ("difficult" clauses are recognized after some time, and then prioritized)

SAT modulo theories:

 extension with background theories (e.g., real numbers, data structures, ...)

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32. Propositional Logic: Local Search and Outlook

Summary (1)

- local search for SAT searches in the space of interpretations; neighbors: assignments that differ only in one variable
- has typical properties of local search methods: evaluation functions, randomization, restarts
- example: GSAT (Greedy SAT)
 - hill climbing with heuristic function: #unsatisfied clauses
 - randomization through tie-breaking and restarts
- example: Walksat
 - focuses on randomly selected unsatisfied clauses
 - does not follow the heuristic always, but also injects noise
 - consequence: more randomization as GSAT and lower risk of getting stuck in local minima

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32.5 Summary

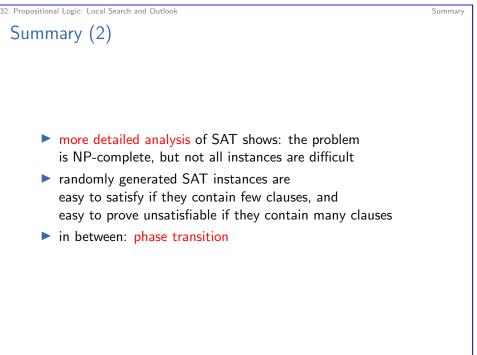
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Summary



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Summar

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