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- searches state space layer by layer
- always finds shallowest goal state first

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always finds shallowest goal state first

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return unsolvable

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10. State-Space Search: Breadth-first Search

BFS-Tree

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BFS-Tree (Final Version)

breadth-first search without duplicate elimination (final version):

DEC	+		
BES	- I ree		
if is_	goal(init()):		
	return ()		
open	:= new Deque		
open	.push_back(make	_root_node())	
while	e not <i>open</i> .is_em	pty():	
	n := open.pop_fr	ont()	
	for each $\langle a,s' angle$ (<pre>succ(n.state):</pre>	
	$n' := make_{-}$	node(n, a, s')	
	if is_goal(s')):	
	return	$extract_path(n')$	
	onen nush h	ack(n')	
	open.pusn_b		







10. State-Space Search: Breadth-first Search BFS-Graph BFS-Graph (Breadth-First Search with Duplicate Elim.) **BFS-Graph** if is_goal(init()): return () open := **new** Deque open.push_back(make_root_node()) *closed* := **new** HashSet closed.insert(init()) while not open.is_empty(): $n := open.pop_front()$ for each $\langle a, s' \rangle \in \text{succ}(n.\text{state})$: $n' := make_node(n, a, s')$ if is_goal(s'): **return** extract_path(n') if $s' \notin closed$: closed.insert(s')open.push_back(n') return unsolvable M. Helmert (University of Basel) Foundations of Artificial Intelligence March 19, 2018 25 / 32





10. State-Space Search: Breadth-first Search: Complexity Breadth-first Search: Complexity The following result applies to both BFS variants: Theorem (time complexity of breadth-first search) Let b be the branching factor and d be the minimal solution length of the given state space. Let $b \ge 2$. Then the time complexity of breadth-first search is $1 + b + b^2 + b^3 + \dots + b^d = O(b^d)$

Reminder: we measure time complexity in generated nodes.

It follows that the space complexity of both BFS variants also is $O(b^d)$ (if $b \ge 2$). (Why?)

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Summary

Breadth-first Search: Example of Complexity

example: b = 10; 100 000 nodes/second; 32 bytes/node

d	nodes	time	memory
3	1 1 1 1	0.01 s	35 KiB
5	111 111	1 s	3.4 MiB
7	10 ⁷	2 min	339 MiB
9	10 ⁹	3 h	33 GiB
11	10 ¹¹	13 days	3.2 TiB
13	10 ¹³	3.5 years	323 TiB
15	10 ¹⁵	350 years	32 PiB

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10. State-Space Search: Breadth-first Search

10.6 Summary

BFS-Tree or BFS-Graph?

What is better, BFS-Tree or BFS-Graph?

advantages of BFS-Graph:

- complete
- much (!) more efficient if there are many duplicates

advantages of BFS-Tree:

- simpler
- less overhead (time/space) if there are few duplicates

Conclusion

BFS-Graph is usually preferable, unless we know that there is a negligible number of duplicates in the given state space.

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