

Planning and Optimization December 11, 2017 — F6. Comparison of Heuristic Families II			
F6.1 Landmarks v	s. h ^{max}		
F6.2 Abstractions vs. Critical Path			
F6.3 Overview			
F6.4 Summary			
M. Helmert, G. Röger (Universität Basel)	Planning and Optimization	December 11, 2017	2 / 16

F6.1 Landmarks vs. *h*^{max}

M. Helmert, G. Röger (Universität Basel)

F6. Comparison of Heuristic Families II

Planning and Optimization

Landmarks vs. h^{max}

F6. Comparison of Heuristic Families II

Landmarks to h^{max}

Theorem

Elementary landmark heuristics can be compiled into additive h^{max} heuristics in polynomial time.

Proof.

Let *L* be a subset of the operators. If L^+ is not a landmark for *s* in Π^+ then $h_L(s) = 0$ and therefore trivially $h^{\max}(s) \ge h_L(s)$. Otherwise no goal state of Π^+ is reachable from *s* without an operator from L^+ . So if $h^{\max}(s) \ne \infty$ then the cost computation of h^{\max} must use an operator from L^+ and therefore $h^{\max}(s) \ge \min_{o \in L} cost(o) = h_L$.

Planning and Optimization

M. Helmert, G. Röger (Universität Basel)

December 11, 2017 5 / 16

F6. Comparison of Heuristic Families II

Abstractions vs. Critical Path

Landmarks vs. hm

F6.2 Abstractions vs. Critical Path

h^{\max} to Landmarks

Theorem

For states with finite h^{max} value, the h^{max} heuristic can be compiled into additive elementary landmark heuristics in polynomial time.

Proof sketch:

The LM-Cut heuristic computes in each step a cut landmark and adapts the operator costs. Let $cost_i, cost_{i+1}$ be the operator costs before and after an iteration that discovered landmark L. Then $h_{cost_i}^{\max}(s) \leq h_{L,cost_i}(s) + h_{cost_{i+1}}^{\max}(s)$. The core argument is that every "reasonable" path in the justification graph enters the goal zone only once and therefore uses only one operator from L. So reducing the cost of each operator in L by $h_{L,cost_i}(s)$ cannot reduce h^{\max} by more than this value. The overall result of the theorem follows from a recursive application of the proof while $h_{cost_{i+1}}^{\max}(s) > 0$.

Planning and Optimization

M. Helmert, G. Röger (Universität Basel)

December 11, 2017

6 / 16

Abstractions vs. Critical Path

Landmarks vs. hm

F6. Comparison of Heuristic Families II

 h^m to PDBs

Theorem

There is no polynomial-time compilation from h^m heuristics into additive PDB heuristics.

Proof.

We know that elementary landmarks are in polynomial time compilable into additive h^{max} but not into additive PDB heuristics. So there is no polynomial-time compilation from $h^{\text{max}} = h^1$ into additive PDB heuristics. As $h^m \ge h^1$ for $m \ge 1$, this holds for any m.

F6. Comparison of Heuristic Families II

Abstractions vs. Critical Path

PDBs to h^m

Theorem

There is no polynomial-time compilation of PDB heuristics into additive h^m heuristics.

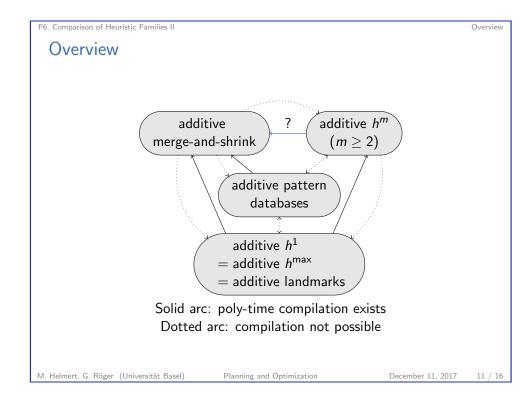
Proof.

Consider family $(\Pi_n)_{n \in \mathbb{N}_1}$ of STRIPS tasks, where $\Pi_n = \langle V_n, I_n, O_n, \gamma \rangle$ with $V_n = \{v_1, \dots, v_n\}$, $I_n(v) = \mathbf{F}$ for $v \in V_n$, $O = \{\langle \bigwedge_{i=1}^{j-1} v_i, v_j \land \bigwedge_{i=1}^{j-1} \neg v_i, 1 \rangle \mid 1 \leq j \leq n\}$ and $\gamma = \bigwedge_{i:i\text{-th bit in bin}(n) \text{ is } 1^{V_i}$. A PDB on pattern $\{v_1, \dots, v_{\lceil \log n \rceil}\}$ has O(n) states and encodes the perfect goal distance $h^*(I) = n$. For a perfect initial estimate, the h^m heuristic needs to consider variable subsets up to size $\lceil \log n \rceil$. As m must be fixed due to the polynomial-time requirement, we can thus find for any such m a large enough n that proves the theorem.

Planning and Optimization

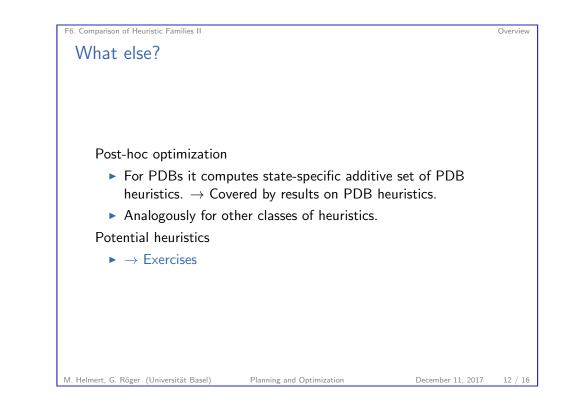
M. Helmert, G. Röger (Universität Basel)

December 11, 2017 9 / 16



F6.3 Overview

F6. Comparison of Heuristic Families II



So far no results for

▶ flow heuristics. and

merge-and-shrink heuristics.

13 / 16

Summar

December 11, 2017

14 / 16

F6.4 Summary

F6. Comparison of Heuristic Families II

M. Helmert, G. Röger (Universität Basel)

M. Helmert, G. Röger (Universität Basel)

December 11, 2017

F6. Comparison of Heuristic Families II

Summary

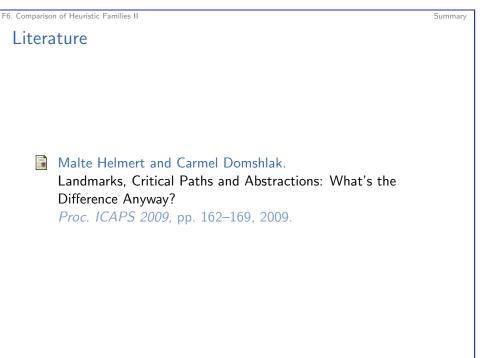
- Relaxation-based landmark heuristics dominate additive h^{max} heuristics and vice versa.
- Additive critical path heuristics with m ≥ 2 strictly dominate relaxation-based landmark heuristics and additive h^{max} heuristics.

▶ landmarks not based on delete relaxation (Π^m landmarks),

Planning and Optimization

 \blacktriangleright compilability from h^m heuristics into additive

- Merge-and-shrink heuristics strictly dominate relaxation-based landmark heuristics and additive h^{max} heuristics.
- PDB heuristics are incomparable with relaxation-based landmark heuristics and additive h^{max} heuristics.



Planning and Optimization