## Planning and Optimization

F2. Cost Partitioning: Landmarks and Generalization

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F2.3 Summary

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F2.1 Cost Partitioning for Landmarks

F2.2 General Cost Partitioning

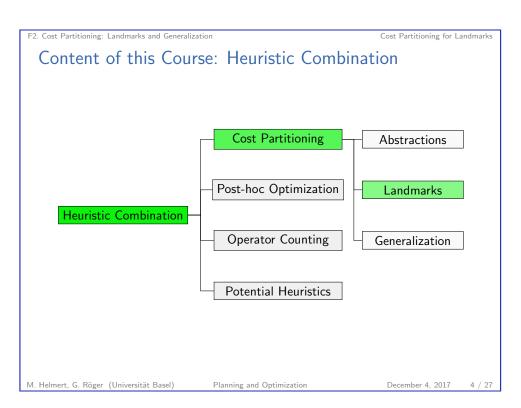
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F2. Cost Partitioning: Landmarks and Generalization

Cost Partitioning for Landmarks

# F2.1 Cost Partitioning for Landmarks



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Cost Partitioning for Landmarks

## Reminder: Disjunctive Action Landmarks

Disjunctive action landmark

- Set of operators
- ▶ Every plan uses at least one of them
- ► Landmark cost = cost of cheapest operator

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## Reminder: Cost Partitioning Heuristic for Landmarks

We have already seen a landmark heuristic based on cost partitioning:

Definition (Uniform Cost Partitioning Heuristic for Landmarks)

Let  $\mathcal{L}$  be a set of disjunctive action landmarks.

The uniform cost partitioning heuristic  $h^{UCP}(\mathcal{L})$  is defined as

$$h^{\mathsf{UCP}}(\mathcal{L}) = \sum_{L \in \mathcal{L}} \min_{o \in L} c'(o)$$
 with

$$c'(o) = cost(o)/|\{L \in \mathcal{L} \mid o \in L\}|.$$

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Cost Partitioning for Landmarks

### Reminder: Proof Back Then

Theorem (Uniform Cost Partitioning Heuristic is Admissible)

Let  $\mathcal{L}$  be a set of disjunctive action landmarks for state s of  $\Pi$ . Then  $h^{UCP}(\mathcal{L})$  is an admissible heuristic estimate for s.

#### Proof.

Let  $\pi = \langle o_1, \dots, o_n \rangle$  be an optimal plan for s. For  $L \in \mathcal{L}$  define a new cost function  $cost_L$  as  $cost_L(o) = c'(o)$  if  $o \in L$  and  $cost_L(o) = 0$  otherwise. Let  $\Pi_L$  be a modified version of  $\Pi$ , where for all operators o the cost is replaced with  $cost_1(o)$ . (...)

$$\sum_{L \in \mathcal{L}} cost_L(o) = \sum_{L \in \mathcal{L}: o \in L} cost(o) / |\{L \in \mathcal{L} \mid o \in L\}| = cost(o)$$

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## Heuristic is Based on Cost Partitioning

- ▶ For disj. action landmark L of state s in task  $\Pi'$ , let  $h_{L,\Pi'}(s)$  be the cost of L in  $\Pi'$ . Then  $h_{L,\Pi'}(s)$  is admissible.
- ▶ Consider set  $\{L_1, \ldots, L_n\}$  of disj. action landmarks for state s of task  $\Pi$ .
- Use cost partitioning  $\langle cost_{L_1}, \ldots, cost_{L_n} \rangle$ , where

$$cost_{L_i}(o) = egin{cases} cost(o)/|\{L \in \mathcal{L} \mid o \in L\}| & ext{if } o \in L_i \\ 0 & ext{otherwise} \end{cases}$$

- ▶ Let  $\langle \Pi_{L_1}, \dots, \Pi_{L_n} \rangle$  be the tuple of induced tasks.
- $h(s) = \sum_{i=1}^{n} h_{L_i,\Pi_{L_i}}(s)$  is an admissible estimate for s in Π.
- ▶ h is uniform cost partitioning heuristic for landmarks.

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Cost Partitioning for Landmarks

## Optimal Cost Partitioning for Landmarks

### Can we find a better cost partitioning?

- ▶ Use again LP that covers heuristic computation and cost partitioning.
- ▶ LP variable Cost<sub>L</sub> for cost of landmark L in induced task (corresponds to  $h_{L_i,\Pi_{I_i}}$ )
- ▶ Explicit variables for cost partitioning not necessary. Use implicitly  $cost_I(o) = Cost_I$  for all  $o \in L$  and 0 otherwise.

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# Optimal Cost Partitioning for Landmarks: LP

#### Variables

 $\mathsf{Cost}_I$  for each disj. action landmark  $L \in \mathcal{L}$ 

#### Objective

Maximize  $\sum_{L \in \mathcal{L}} \mathsf{Cost}_L$ 

### Subject to

 $\sum \quad \mathsf{Cost}_L \leq \mathit{cost}(o)$ for all operators o  $Cost_I \geq 0$ for all landmarks  $L \in \mathcal{L}$ 

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# Optimal Cost Partitioning for Landmarks (Dual view)

Variables

Counto for each operator o

Objective

Minimize  $\sum_{o} Count_{o} \cdot cost(o)$ 

Subject to

 $\sum_{\sigma} \mathsf{Count}_{\sigma} \geq 1 \text{ for all landmarks } L$ 

 $Count_o > 0$  for all operators o

Minimize "plan cost" with all landmarks satisfied.

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General Cost Partitioning

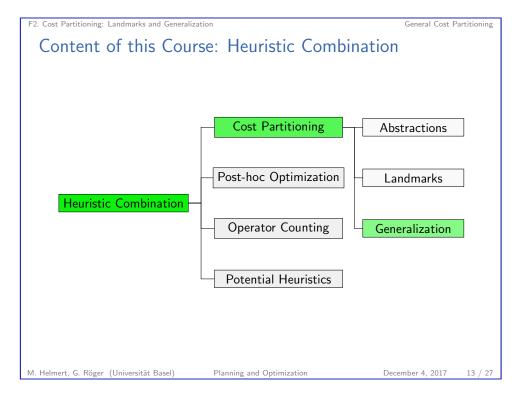
# F2.2 General Cost Partitioning

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General Cost Partitioning

## General Cost Partitioning

### Cost functions usually non-negative

- ▶ We tacitly also required this for task copies
- ▶ Makes intuitively sense: original costs are non-negative
- ▶ But: not necessary for cost-partitioning!

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General Cost Partitioning

## General Cost Partitioning

### Definition (General Cost Partitioning)

Let  $\Pi$  be a planning task with operators O.

A general cost partitioning for  $\Pi$  is a tuple  $\langle cost_1, \ldots, cost_n \rangle$ , where

- $ightharpoonup cost_i: O \to \mathbb{R}$  for 1 < i < n and
- $ightharpoonup \sum_{i=1}^n cost_i(o) \le cost(o)$  for all  $o \in O$ .

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General Cost Partitioning

## General Cost Partitioning: Admissibility

### Theorem (Sum of Solution Costs is Admissible)

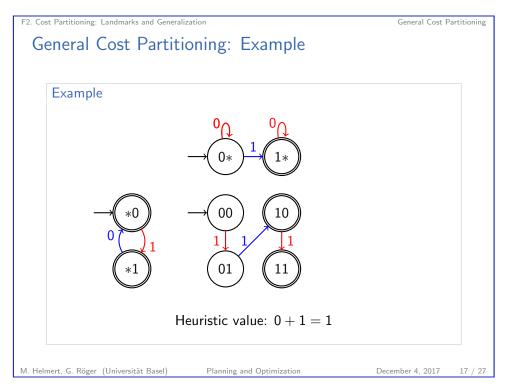
Let  $\Pi$  be a planning task,  $\langle cost_1, \ldots, cost_n \rangle$  be a general cost partitioning and  $\langle \Pi_1, \dots, \Pi_n \rangle$  be the tuple of induced tasks.

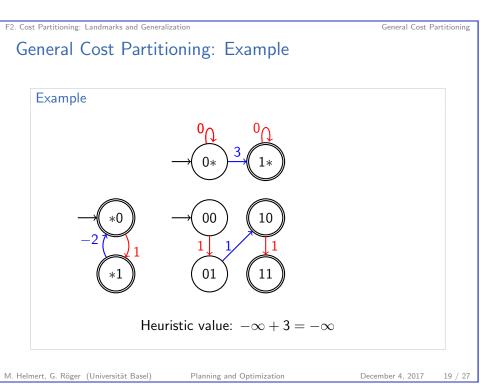
Then the sum of the solution costs of the induced tasks is an admissible heuristic for  $\Pi$ , i.e.,  $\sum_{i=1}^{n} h_{\Pi_i}^* \leq h_{\Pi}^*$ .

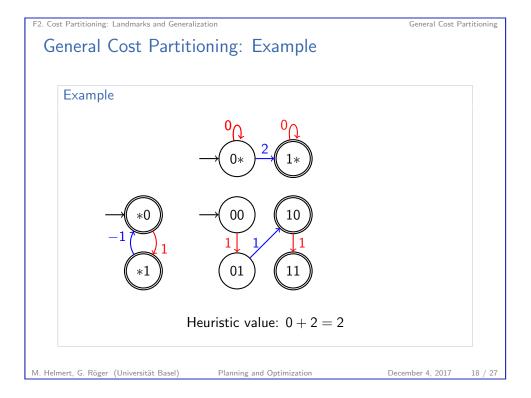
(Proof omitted.)

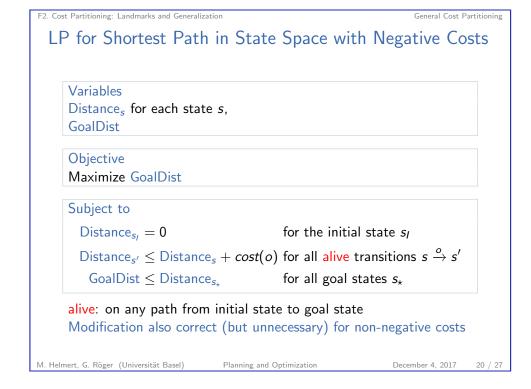
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General Cost Partitioning

## General Cost Partitioning: Remarks

- ▶ More powerful than non-negative cost partitioning
- ▶ Optimal general cost partitioning: omit constraints to non-negative cost variables
  - optimal cost partitioning maximizes objective value
  - removing constraints can only increase heuristic value
- ▶ Optimal general cost partitioning is never worse than an optimal non-negative cost partitioning.

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# F2.3 Summary

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## Summary

- ▶ We can compute an optimal cost partitioning for a given set of disjunctive action landmarks in polynomial time.
- ▶ In constrast to standard (non-negative) cost partitioning, general cost partitioning allows negative operators costs.
- ▶ General cost partitioning has the same relevant properties as non-negative cost partitioning but is more powerful.

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## Literature (1)

References on cost partitioning:



Stefan Edelkamp.

Automated Creation of Pattern Database Search Heuristic.

Proc. MoChArt 2006, pp. 35-50, 2006.

Introduces 0-1 cost partitioning for abstraction heuristics.



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Structural Patterns Heuristics: Basic Idea and Concrete Instance.

ICAPS 2007 HDIP Workshop, 2007.

Introduces arbitrary non-negative cost partitioning.

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Literature (2)

Fan Yang, Joseph C. Culberson, Robert Holte, Uzi Zahavi and Ariel Felner.

A General Theory of Additive State Space Abstractions.

JAIR 32, pp. 631-662, 2008.

Introduces arbitrary non-negative cost partitioning

Erez Karpas and Carmel Domshlak. Cost-optimal Planning with Landmarks.

Proc. IJCAI 2009, pp. 1728-1733, 2009. Introduces optimal cost partitioning for landmarks (different formulation than in the slides).

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# Literature (4)

Michael Katz and Carmel Domshlak. Optimal Admissible Composition of Abstraction Heuristics. Artificial Intelligence 174 (12-13), pp. 767-798, 2010. Introduces optimal cost partitioning for abstraction heuristics.

Florian Pommerening, Malte Helmert, Gabriele Röger and Jendrik Seipp.

From Non-Negative to General Operator Cost Partitioning.

Proc. AAAI 2015, pp. 3335-3341, 2015.

Introduces general cost partitioning.

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Smaller LP for optimal cost partitioning for landmarks.

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