

# Planning and Optimization

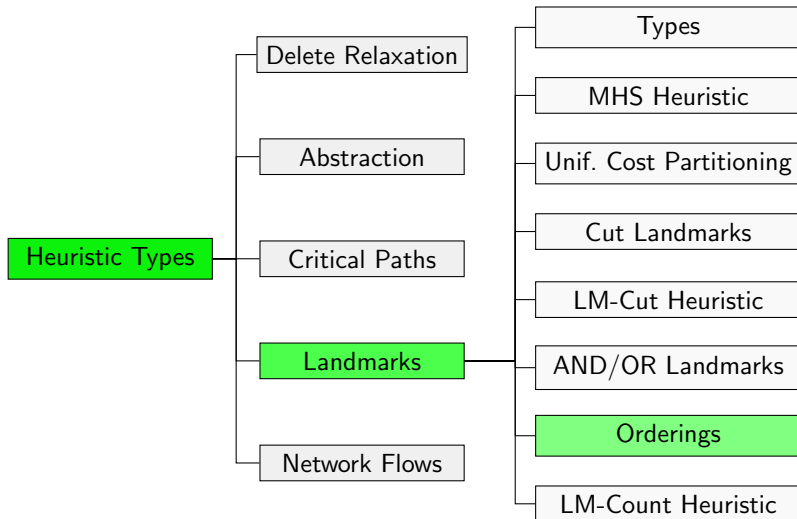
## E6. Landmarks: LM-count Heuristic

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# Content of this Course: Landmarks



# Landmark Orderings

# Why Landmark Orderings?

- **LM-cut heuristic** uses integrated landmark and heuristic computation **in each state**.
- Other landmark-based heuristics **compute landmarks once** and **propagate** them over operator applications.
- **Landmark orderings** are used to detect landmarks that should be further considered because they (again) need to be satisfied later.

# Terminology

Let  $\pi = \langle o_1, \dots, o_n \rangle$  be a sequence of operators applicable in state  $I$  and let  $\varphi$  be a formula over the state variables.

- $\varphi$  is **true at time  $i$**  if  $I[\langle o_1, \dots, o_i \rangle] \models \varphi$ .
- Also special case  $i = 0$ :  $\varphi$  is **true at time 0** if  $I \models \varphi$ .
- No formula is true at time  $i < 0$ .
- $\varphi$  is **added at time  $i$**  if it is **true at time  $i$**  but not at time  $i - 1$ .
- $\varphi$  is **first added at time  $i$**  if it is **true at time  $i$**  but not at any time  $j < i$ .

# Landmark Orderings

## Definition (Landmark Orderings)

Let  $\varphi$  and  $\psi$  be formula landmarks. There is

- a **natural ordering** between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow \psi$ ) if in each plan where  $\psi$  is true at time  $i$ ,  $\varphi$  is true at some time  $j < i$ ,
- a **necessary ordering** between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow_n \psi$ ) if in each plan where  $\psi$  is added at time  $i$ ,  $\varphi$  is true at time  $i - 1$ ,
- a **greedy-necessary ordering** between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow_{gn} \psi$ ) if in each plan where  $\psi$  is first added at time  $i$ ,  $\varphi$  is true at time  $i - 1$ .

# Natural Orderings

## Definition

There is a **natural ordering** between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow \psi$ ) if in each plan where  $\psi$  is true at time  $i$ ,  $\varphi$  is true at some time  $j < i$ .

- We can directly determine natural orderings from the  $LM$  sets computed from the simplified relaxed task graph.
- For fact landmarks  $v, v'$  with  $v \neq v'$ , if  $n_{v'} \in LM(n_v)$  then  $v' \rightarrow v$ .

# Greedy-necessary Orderings

## Definition

There is a **greedy-necessary ordering** between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow_{\text{gn}} \psi$ ) if in each plan where  $\psi$  is first added at time  $i$ ,  $\varphi$  is true at time  $i - 1$ .

- We can again determine such orderings from the sRTG.
- For an OR node  $n_v$ , we define the set of **first achievers** as  $FA(n_v) = \{n_o \mid n_o \in \text{succ}(n_v) \text{ and } n_v \notin LM(n_o)\}$ .
- Then  $v' \rightarrow_{\text{gn}} v$  if  $n_{v'} \in \text{succ}(n_o)$  for all  $n_o \in FA(n_v)$ .



# Landmark-count Heuristic

# Reached Landmarks

A landmark is **reached** by a path if it has been true in any traversed state.

## Definitions (Reached Landmarks)

Let  $\mathcal{L}$  be a set of formula landmarks for task  $\langle V, I, O, \gamma \rangle$  and let  $\pi$  be an operator sequence applicable in  $I$ .

The set of **reached landmarks** is defined as  $Reached(\pi, \mathcal{L}) =$

$$\begin{cases} \{\psi \in \mathcal{L} \mid I \models \psi\} & \pi = \langle \rangle \\ Reached(\pi', \mathcal{L}) \cup \{\psi \in \mathcal{L} \mid I[\llbracket \pi \rrbracket] \models \psi\} & \pi = \pi' \langle o \rangle \end{cases}$$

Can be computed incrementally.

# Required Again

A reached landmark is required again, if it is currently false but must be true due to an ordering or because it is required by the goal.

## Definitions (Required Again)

Let  $\mathcal{L}$  be a set of formula landmarks for  $\Pi = \langle V, I, O, \gamma \rangle$  with orderings  $Ord$ , and let  $\pi$  be an operator sequence applicable in  $I$ .

The set of landmarks that are **required again** is defined as

$$ReqAgain(\pi, \mathcal{L}, Ord) = \{\varphi \in Reached(\pi, \mathcal{L}) \mid I \llbracket \pi \rrbracket \not\models \varphi \text{ and } (\gamma \models \varphi \text{ or exists } \varphi \rightarrow_{gn} \psi \in Ord : \psi \notin Reached(\pi, \mathcal{L}))\}.$$

# Landmark-count Heuristic

The landmark-count heuristic counts the landmarks that have not been reached or are required again.

## Definition (LM-count Heuristic)

Let  $\Pi$  be a planning task with initial state  $I$  and let  $\mathcal{L}$  be a set of landmarks for  $I$  with orderings  $Ord$ .

The **LM-count heuristic** for an operator sequence  $\pi$  that is applicable in  $I$  is

$$h_{\mathcal{L}}^{\text{LM-count}}(\pi) = |(\mathcal{L} \setminus \text{reached}(\pi, \mathcal{L})) \cup \text{ReqAgain}(\pi, \mathcal{L}, Ord)|.$$

# LM-count Heuristic is Path-dependent

- LM-count heuristic gives estimates for paths (it is a **path-dependent** heuristic).
- Search algorithms need estimates for states.
- $\rightsquigarrow$  use estimate for the currently considered path to the state.
- $\rightsquigarrow$  heuristic estimate for a state is not well-defined.

# LM-count Heuristic is Inadmissible

## Example

Consider STRIPS planning task  $\Pi = \langle \{a, b\}, \emptyset, \{o\}, \{a, b\} \rangle$  with  $o = \langle \emptyset, \{a, b\}, \emptyset, 1 \rangle$ . Let  $\mathcal{L} = \{a, b\}$  and  $Ord = \emptyset$ .

The estimate for the initial state  $I = \{\}$  is  $h_{\mathcal{L}}^{\text{LM-count}}(\langle \rangle) = 2$  while  $h^*(I) = 1$ .

$\leadsto h^{\text{LM-count}}$  is **inadmissible**.

# LM-count Heuristic: Comments

- Practical implementations **store the set of reached landmarks** for each state.
- LM-Count alone is not a particularly informative heuristic.
- On the positive side, it complements  $h^{FF}$  very well.
- For example, the LAMA planning system alternates between expanding a state with minimal  $h^{FF}$  and minimal  $h^{LM-count}$  estimate.
- There is an admissible variant of the heuristic based on operator cost partitioning.

# Summary



# Summary

- The LM-count heuristic propagates landmarks over operator applications.
- It counts how many landmarks still need to be satisfied.
- The LM-count heuristic is inadmissible (but there is an admissible variant).
- Landmark orderings can be useful for detecting when a landmark should be further considered.

# Literature (1)

References on landmark heuristics:



Julie Porteous, Laura Sebastia and Joerg Hoffmann.

On the Extraction, Ordering, and Usage of Landmarks in Planning.

*Proc. ECP 2001*, pp. 174–182, 2013.

Introduces landmarks.



Malte Helmert and Carmel Domshlak.

Landmarks, Critical Paths and Abstractions: What's the Difference Anyway?

*Proc. ICAPS 2009*, pp. 162–169, 2009.

Introduces cut landmarks and LM-cut heuristic.

## Literature (2)



Lin Zhu and Robert Givan.

Landmark Extraction via Planning Graph Propagation.

*Doctoral Consortium ICAPS 2003*, 2003.

Core idea for complete landmark generation.



Emil Keyder, Silvia Richter and Malte Helmert.

Sound and Complete Landmarks for And/Or Graphs

*Proc. ECAI 2010* , pp. 335–340, 2010.

Introduces landmarks from AND/OR graphs  
and usage of  $\Pi^m$  compilation.

## Literature (3)



Silvia Richter and Matthias Westphal.

The LAMA Planner: Guiding Cost-Based Anytime Planning with Landmarks.

*JAIR 39 (2010)* , pp. 127–177, 2010.

Introduces landmark-count heuristic and contains another landmark generation method.



Erez Karpas and Carmel Domshlak.

Cost-Optimal Planning with Landmarks.

*Proc. IJCAI 2009*, pp. 1728–1733, 2009.

Introduces admissible variant of landmark heuristic.