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Planning and Optimization

E3. Landmarks: Introduction & Minimum Hitting Set Heuristic

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Landmarks

# E3.1 Landmarks

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E3. Landmarks: Introduction & Minimum Hitting Set Heuristic

# Landmarks

Basic Idea: Something that must happen in every solution

## For example

- some operator must be applied
- some atom must be true
- some formula must be true
- $\rightarrow$  Derive heuristic estimate from this kind of information.

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# Reminder: Terminology Consider sequence of transitions $s^0 \xrightarrow{\ell_1} s^1, \ldots, s^{n-1} \xrightarrow{\ell_n} s^n$ such that $s^0 = s$ and $s^n = s'$ . • $s^0, \ldots, s^n$ is called (state) path from s to s' • $\ell_1, \ldots, \ell_n$ is called (label) path from s to s' • $s^0 \xrightarrow{\ell_1} s^1, \ldots, s^{n-1} \xrightarrow{\ell_n} s^n$ is called trace from s to s' M. Helmert, G. Röger (Universität Basel) Planning and Optimization November 22, 2017 6 / 29 E3. Landmarks: Introduction & Minimum Hitting Set Heuristic **Disjunctive Action Landmarks**

E3. Landmarks: Introduction & Minimum Hitting Set Heuristic

Definition (Disjunctive Action Landmark) Let s be a state of planning task  $\Pi = \langle V, I, O, \gamma \rangle$ . A disjunctive action landmark for s is a set of operators  $L \subseteq O$ such that every label path from s to a goal state contains an operator from L.

The cost of landmark *L* is  $cost(L) = min_{o \in L} cost(o)$ .

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# Example Task

- ► Two trucks, one airplane
- Airplane can fly between locations A3 and B1
- > Trucks can drive arbitrarily between locations A1, A2, and A3

Landmarks

- ▶ Package to be transported from A1 to B1
- Operators
  - ▶ Load(v, l) and Unload(v, l) for vehicle v and location l
  - Drive(t, l, l') for truck t and locations l, l'
  - ► Fly(*I*, *I'*) for locations *I*, *I'*





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### Example: Formula Landmarks at(Package, A3) and in(Package, Airplane) are fact landmarks. in(Package, Truck1) $\lor$ in(Package, Truck2) is a formula landmark. Truck1 A3 A3

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### E3. Landmarks: Introduction & Minimum Hitting Set Heuristic

## Uniform Cost Partitioning

# Uniform Cost Partitioning (2)

Theorem (Uniform Cost Partitioning Heuristic is Admissible) Let  $\mathcal{L}$  be a set of disjunctive action landmarks for state s of  $\Pi$ . Then  $h^{UCP}(\mathcal{L})$  is an admissible heuristic estimate for s.

## Proof.

Let  $\pi = \langle o_1, \ldots, o_n \rangle$  be an optimal plan for *s*. For  $L \in \mathcal{L}$  define a new cost function  $cost_L$  as  $cost_L(o) = c'(o)$  if  $o \in L$  and  $cost_L(o) = 0$  otherwise. Let  $\Pi_L$  be a modified version of  $\Pi$ , where for all operators *o* the cost is replaced with  $cost_L(o)$ . We make three independent observations:

- For L ∈ L the value cost'(L) := min<sub>o∈L</sub> c'(o) is an admissible estimate for s in Π<sub>L</sub>.
- 2  $\pi$  is also a plan for s in  $\Pi_L$ , so  $h_{\Pi_L}^*(s) \leq \sum_{i=1}^n cost_L(o_i)$ .

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•  $\sum_{L \in \mathcal{L}} cost_L(o) = cost(o)$  for each operator o.

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Relationship

Theorem Let  $\mathcal{L}$  be a set of disjunctive action landmarks for state s. Then  $h^{UCP}(\mathcal{L}) \leq h^{MHS}(\mathcal{L}) \leq h^*(s)$ .

(Proof omitted.)

# Uniform Cost Partitioning (3)

## Proof (continued).

Together, this leads to the following inequality (subscripts indicate for which task the heuristic is computed):





Summary

- Landmarks describe properties that are shared by all plans of a task.
- Hitting sets yield the most accurate heuristic for a given set of disjunctive action landmarks, but the computation is NP-hard.
- Uniform cost partitioning is a polynomial approach for the computation of informative heuristics from disjunctive action landmarks.

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