

Planning and Optimization

D5. Potential Heuristics

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Introduction

Introduction

- Operator-counting heuristics solve an LP to compute the heuristic estimate **for a single state**.
- Can we also define an **entire heuristic function** solving only one LP?
- **Axiomatic approach** for defining heuristics:
 - What should a heuristic look like mathematically?
 - Which properties should it have?
- Define a **space of interesting heuristics**.
- Use **optimization** to pick a good representative.

Potential Heuristics

Potential Heuristics: Idea

Heuristic design as an optimization problem:

- Define simple numerical **state features** f_1, \dots, f_n .
- Consider heuristics that are **linear combinations** of features:

$$h(s) = w_1 f_1(s) + \dots + w_n f_n(s)$$

with weights (**potentials**) $w_i \in \mathbb{R}$

- Find potentials for which h is admissible and well-informed.

Motivation:

- **declarative approach** to heuristic design
- heuristic **very fast to compute** if features are

Potential Heuristics

Features

Definition (feature)

A (state) **feature** for a planning task is a numerical function defined on the states of the task: $f : S \rightarrow \mathbb{R}$.

Potential Heuristics

Definition (potential heuristic)

A **potential heuristic** for a set of features $\mathcal{F} = \{f_1, \dots, f_n\}$ is a heuristic function h defined as a **linear combination** of the features:

$$h(s) = w_1 f_1(s) + \dots + w_n f_n(s)$$

with weights (**potentials**) $w_i \in \mathbb{R}$.

↪ cf. **evaluation functions** for board games like chess

Atomic Potential Heuristics

Atomic features test if some atom is true in a state:

Definition (atomic feature)

Let $X = x$ be an atom of a FDR planning task.

The **atomic feature** $f_{X=x}$ is defined as:

$$f_{X=x}(s) = \begin{cases} 1 & \text{if variable } X \text{ has value } x \text{ in state } s \\ 0 & \text{otherwise} \end{cases}$$

- We only consider **atomic** potential heuristics, which are based on the set of all atomic features.
- **Example** for a task with state variables X and Y :

$$h(s) = 3f_{X=a} + \frac{1}{2}f_{X=b} - 2f_{X=c} + \frac{5}{2}f_{Y=d}$$

Finding Good Potential Heuristics

How to Set the Weights?

We want to find **good** atomic potential heuristics:

- admissible
- consistent
- well-informed

How to achieve this? **Linear programming to the rescue!**

Admissible and Consistent Potential Heuristics

Constraints on potentials **characterize** (= are necessary and sufficient for) admissible and consistent atomic potential heuristics:

Goal-awareness

$$\sum_{\text{goal atoms } a} w_a = 0$$

Consistency

$$\sum_{\substack{a \text{ consumed} \\ \text{by } o}} w_a - \sum_{\substack{a \text{ produced} \\ \text{by } o}} w_a \leq \text{cost}(o) \quad \text{for all operators } o$$

Remarks:

- assumes transition normal form (not a limitation)
- goal-aware and consistent = admissible and consistent

Well-Informed Potential Heuristics

How to find a **well-informed** potential heuristic?

↪ encode **quality metric** in the **objective function**
and use LP solver to find a heuristic maximizing it

Examples:

- maximize **heuristic value of a given state** (e.g., initial state)
- maximize average heuristic value of **all states**
(including unreachable ones)
- maximize average heuristic value of some **sample states**
- minimize **estimated search effort**

Connection to Flow Heuristic

Relationship to Flow Heuristic

Theorem

For state s , let $h^{\max\text{pot}}(s)$ denote the *maximal* heuristic value of all admissible and consistent atomic potential heuristics in s .

Then $h^{\max\text{pot}}(s) = h^{\text{flow}}(s)$.

Proof idea: compare dual of $h^{\text{flow}}(s)$ LP to potential heuristic constraints optimized for state s .

If we optimize the potentials for a given state then for this state it equals the flow heuristic.

Summary

Summary

- General cost partitioning, operator-counting constraints and potential heuristics are **facets of the same phenomenon**
- Study of each reinforces understanding of the others.
- Potential heuristics can be used as **fast admissible approximations** of h^{flow} .
- **Generalization beyond h^{flow}** : use non-atomic features
- If features are cheap to compute, the **heuristic evaluation** for every state is extremely **fast**.

Literature

References on potential heuristics:



Florian Pommerening, Malte Helmert, Gabriele Röger and Jendrik Seipp.

From Non-Negative to General Operator Cost Partitioning.
Proc. AAAI 2015, pp. 3335–3341, 2015.

Introduces potential heuristics.



Jendrik Seipp, Florian Pommerening and Malte Helmert.
New Optimization Functions for Potential Heuristics.

Proc. ICAPS 2015, pp. 193–201, 2015.

Studies effect of **different optimization functions**.