Planning and Optimization C22. Landmarks: LM-count Heuristic

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# Landmark Orderings

# Why Landmark Orderings?

- LM-cut heuristic uses integrated landmark and heuristic computation in each state.
- Other landmark-based heuristics compute landmarks once and propagate them over operator applications.
- Landmark orderings are used to detect landmarks that should be further considered because they (again) need to be satisfied later.

## Terminology

Let  $\pi = \langle o_1, \dots, o_n \rangle$  be a sequence of operators applicable in state I and let  $\varphi$  be a formula over the state variables.

- $\varphi$  is true at time *i* if  $I[\![\langle o_1, \ldots, o_i \rangle]\!] \models \varphi$ .
- Also special case i = 0:  $\varphi$  is true at time 0 if  $I \models \varphi$ .
- No formula is true at time i < 0.
- $\varphi$  is added at time *i* if it is true at time *i* but not at time *i*-1.
- φ is first added at time i if it is true at time i but not at any time j < i.</li>

# Landmark Orderings

#### Definition (Landmark Orderings)

Let  $\varphi$  and  $\psi$  be formula landmarks. There is

- a natural ordering between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow \psi$ ) if in each plan where  $\psi$  is true at time *i*,  $\varphi$  is true at some time *j* < *i*,
- a necessary ordering between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow_n \psi$ ) if in each plan where  $\psi$  is added at time *i*,  $\varphi$  is true at time *i* - 1,
- a greedy-necessary ordering between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow_{gn} \psi$ ) if in each plan where  $\psi$  is first added at time *i*,  $\varphi$  is true at time i 1.

# Natural Orderings

### Definition

There is a natural ordering between  $\varphi$  and  $\psi$  (written  $\varphi \rightarrow \psi$ ) if in each plan where  $\psi$  is true at time *i*,  $\varphi$  is true at some time *j* < *i*.

- We can directly determine natural orderings from the *LM* sets computed from the simplified relaxed task graph.
- For fact landmarks v, v', if  $n_{v'} \in LM(n_v)$  then  $v' \to v$ .

## Greedy-necessary Orderings

### Definition

There is a greedy-necessary ordering between  $\varphi$  and  $\psi$ (written  $\varphi \rightarrow_{gn} \psi$ ) if in each plan where  $\psi$  is first added at time *i*,  $\varphi$  is true at time i - 1.

- We can again determine such orderings from the sRTG.
- For an OR node  $n_v$ , we define the set of first achievers as  $FA(n_v) = \{n_o \mid n_o \in succ(n_v) \text{ and } n_v \notin LM(n_o)\}.$
- Then  $v' \rightarrow_{gn} v$  whenever  $n_{v'} \in succ(n_o)$  for all  $n_o \in FA(n_v)$ .

# Landmark-count Heuristic

## **Reached Landmarks**

A landmark is reached by a path if it has been true in any traversed state.

#### Definitions (Reached Landmarks)

Let  $\mathcal{L}$  be a set of formula landmarks for task  $\langle V, I, O, \gamma \rangle$  and let  $\pi$  be an operator sequence applicable in I.

The set of reached landmarks is defined as  $Reached(\pi, \mathcal{L}) = \begin{cases} \{\psi \in \mathcal{L} \mid I \models \psi\} & \pi = \langle \rangle \\ Reached(\pi', \mathcal{L}) \cup \{\psi \in \mathcal{L} \mid I[\![\pi]\!] \models \psi\} & \pi = \pi' \langle o \rangle \end{cases}$ 

Can be computed incrementally.

# Required Again

A reached landmark is required again, if it is currently false but must be true due to an ordering or because it is required by the goal.

### Definitions (Required Again)

Let  $\mathcal{L}$  be a set of formula landmarks for  $\Pi = \langle V, I, O, \gamma \rangle$  with orderings *Ord*, and let  $\pi$  be an operator sequence applicable in *I*.

The set of landmarks that are required again is defined as  $ReqAgain(\pi, \mathcal{L}, Ord) = \{\varphi \in Reached(\pi, \mathcal{L}) \mid I[\![\pi]\!] \not\models \varphi \text{ and}$  $(\gamma \models \varphi \text{ or exists } \varphi \rightarrow_{gn} \psi \in Ord : \psi \notin Reached(\pi, \mathcal{L}))\}.$ 

## Landmark-count Heuristic

The landmark-count heuristic counts the landmarks that have not been reached or are required again.

#### Definition (LM-count Heuristic)

Let  $\Pi$  be a planning task with initial state I and let  $\mathcal{L}$  be a set of landmarks for I with orderings *Ord*.

The LM-count heuristic for an operator sequence  $\pi$  that is applicable in I is

 $h_{\mathcal{L}}^{\mathsf{LM-count}}(\pi) = |(\mathcal{L} \setminus \mathit{reached}(\pi, \mathcal{L})) \cup \mathit{ReqAgain}(\pi, \mathcal{L}, \mathit{Ord})|.$ 

## LM-count Heuristic is Path-dependent

- LM-count heuristic gives estimates for paths (it is a path-dependent heuristic).
- Search algorithms need estimates for states.
- $\rightsquigarrow$  use estimate for the currently considered path to the state.
- $\rightsquigarrow$  heuristic estimate for a state is not well-defined.

## LM-count Heuristic is Inadmissible

#### Example

Consider STRIPS planning task  $\Pi = \langle \{a, b\}, \emptyset, \{o\}, \{a, b\} \rangle$  with  $o = \langle \emptyset, \{a, b\}, \emptyset, 1 \rangle$ . Let  $\mathcal{L} = \{\{a\}, \{b\}\}$  and  $Ord = \emptyset$ .

The estimate for the initial state  $I = \{\}$  is  $h_{\mathcal{L}}^{\text{LM-count}}(\langle \rangle) = 2$  while  $h^*(I) = 1$ .

 $\rightsquigarrow h^{\text{LM-count}}$  is inadmissible.

## LM-count Heuristic: Comments

- Practical implementations store the set of reached landmarks for each state.
- LM-Count alone is not a particularily informative heuristic.
- On the positive side, it complements  $h^{\text{FF}}$  very well.
- For example, the LAMA planning system alternates between expanding a state with minimal  $h^{\text{FF}}$  and minimal  $h^{\text{LM-count}}$  estimate.
- There is an admissible variant of the heuristic based on operator cost partitioning.

# Summary



- The LM-count heuristic propagates landmarks over operator applications.
- It counts how many landmarks still need to be satisfied.
- The LM-count heuristic is inadmissible (but there is an admissible variant).
- Landmark orderings can be useful for detecting when a landmark should be further considered.

# Literature (1)

### References on landmark heuristics:

- Julie Porteous, Laura Sebastia and Joerg Hoffmann.
  On the Extraction, Ordering, and Usage of Landmarks in Planning.
   Proc. ECP 2001, pp. 174–182, 2013.
   Introduces landmarks.
- Malte Helmert and Carmel Domshlak.
  Landmarks, Critical Paths and Abstractions: What's the Difference Anyway?
  Proc. ICAPS 2009, pp. 162–169, 2009.
  Introduces cut landmarks and LM-cut heuristic.

# Literature (2)

- Lin Zhu and Robert Givan. Landmark Extraction via Planning Graph Propagation. *Doctoral Consortium ICAPS 2003*, 2003. Core idea for complete landmark generation.
- Emil Keyder, Silvia Richter and Malte Helmert.
  Sound and Complete Landmarks for And/Or Graphs *Proc. ECAI 2010*, pp. 335–340, 2010.
   Introduces landmarks from AND/OR graphs and usage of Π<sup>m</sup> compilation.

# Literature (3)

## Silvia Richter and Matthias Westphal.

The LAMA Planner: Guiding Cost-Based Anytime Planning with Landmarks.

## JAIR 39 (2010), pp. 127–177, 2010.

Introduces landmark-count heuristic and contains another landmark generation method.

Erez Karpas and Carmel Domshlak. Cost-Optimal Planning with Landmarks. *Proc. IJCAI 2009*, pp. 1728–1733, 2009. Introduces admissible variant of landmark heuristic.