

## Planning and Optimization

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### Exercise Sheet 10

**Due: December 7, 2016**

#### Exercise 10.1 (1+2+1+1 marks)

Consider the STRIPS task  $\Pi = \langle V, I, O, G \rangle$  with variable set  $V = \{a, b, c, d, e, f, g\}$ , initial state  $I = \{a\}$ , operator set  $O = \{o_1, o_2, o_3, o_4, o_5, o_6\}$  and goal  $G = \{e\}$ . All operators in  $O$  have cost 1. The preconditions, add and delete lists are defined as follows:

- $pre(o_1) = \{a\}$ ,  $add(o_1) = \{b\}$ ,  $del(o_1) = \{a\}$
- $pre(o_2) = \{a\}$ ,  $add(o_2) = \{c\}$ ,  $del(o_2) = \emptyset$
- $pre(o_3) = \{b\}$ ,  $add(o_3) = \{d\}$ ,  $del(o_3) = \emptyset$
- $pre(o_4) = \{c\}$ ,  $add(o_4) = \{d\}$ ,  $del(o_4) = \emptyset$
- $pre(o_5) = \{d, g\}$ ,  $add(o_5) = \{e, f\}$ ,  $del(o_5) = \emptyset$
- $pre(o_6) = \emptyset$ ,  $add(o_6) = \{g\}$ ,  $del(o_6) = \emptyset$

- (a) Provide the simplified relaxed task graph  $sRTG(\Pi^+)$  in graphical form.
- (b) Compute the set of causal fact landmarks with the fixed-point algorithm introduced in chapter 21 (slides 15 and 16 in the handout version). Provide the intermediate steps of the algorithm.
- (c) Provide a formula landmark  $\varphi$  for  $\Pi^+$  with the property that  $\varphi$  is *not* a landmark of  $\Pi$ . Justify your answer.
- (d) Is there a fact landmark in  $\Pi$  that is *not* a causal landmark in  $\Pi$ ? If yes, provide such a landmark and justify your answer. Otherwise, justify why such a landmark does not exist.

#### Exercise 10.2 (1.5+1.5 marks)

Consider the STRIPS task  $\Pi = \langle V, I, O, G \rangle$  with variable set  $V = \{a, b, c, d\}$ , initial state  $I = \{a\}$ , operator set  $O = \{o_1, o_2, o_3, o_4\}$  and goal  $G = \{b, d\}$ . All operators in  $O$  have cost 1. The preconditions, add and delete lists are defined as follows:

- $pre(o_1) = \{a\}$ ,  $add(o_1) = \{b\}$ ,  $del(o_1) = \{a\}$
- $pre(o_2) = \{b\}$ ,  $add(o_2) = \{c\}$ ,  $del(o_2) = \{b\}$
- $pre(o_3) = \{c\}$ ,  $add(o_3) = \{d\}$ ,  $del(o_3) = \emptyset$
- $pre(o_4) = \{d\}$ ,  $add(o_4) = \{a, b\}$ ,  $del(o_4) = \emptyset$

The set of fact landmarks for  $I$  is given by  $\mathcal{L} = \{a, b, c, d\}$ .

*Please turn the page.*

- (a) Is there a natural ordering  $a \rightarrow b$  between the fact landmarks  $a$  and  $b$ ? Is there a necessary ordering  $a \rightarrow_n b$ ? Is there a greedy necessary ordering  $a \rightarrow_{gn} b$ ? Justify your answers.
- (b) Consider the path  $\pi = \langle o_1 o_2 \rangle$ . Compute  $h_{\mathcal{L}}^{\text{LM-count}}(\pi)$ . For the computation, also provide the sets  $\text{reached}(\pi, \mathcal{L})$  and  $\text{ReqAgain}(\pi, \mathcal{L}, \text{Ord})$ .

**Exercise 10.3** (3+1 marks)

Consider the planning task  $\Pi = \langle V, I, O, \gamma \rangle$  where a truck can move between locations  $A$  and  $B$ , and pickup and drop a package in  $B$  and  $A$ , respectively.  $\Pi$  is given as follows:

$$\begin{aligned}
 V &= \{T, P\} \text{ with } \text{dom}(T) = \{A, B\} \text{ and } \text{dom}(P) = \{A, B, T\} \\
 I &= \{T \mapsto A, P \mapsto B\} \\
 O &= \{\text{move}_{AB}, \text{move}_{BA}, \text{pickup}, \text{drop}\}, \text{ where} \\
 \text{move}_{AB} &= \langle T = A, T := B, 1 \rangle \\
 \text{move}_{BA} &= \langle T = B, T := A, 1 \rangle \\
 \text{pickup} &= \langle T = B \wedge P = B, P := T, 1 \rangle \\
 \text{drop} &= \langle T = A \wedge P = T, P := A, 1 \rangle \\
 \gamma &= (T = B \wedge P = A)
 \end{aligned}$$

- (a) Transform  $\Pi$  to transition normal form. Provide the linear program with objective value  $h^{\text{flow}}(I)$  and report  $h^{\text{flow}}(I)$ .
- (b) Does the introduction of the additional operator

$$\text{beam} = \langle P = B; P := A, 5 \rangle$$

alter the heuristic estimate? Justify your answer.

*The exercise sheets can be submitted in groups of two students. Please provide both student names on the submission.*