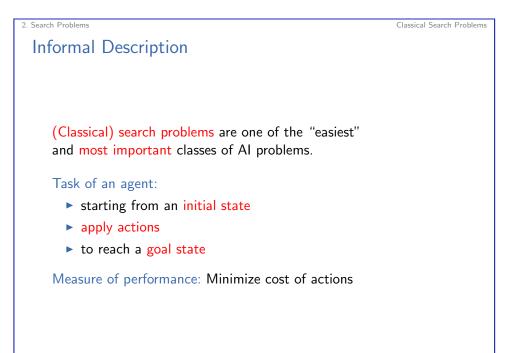


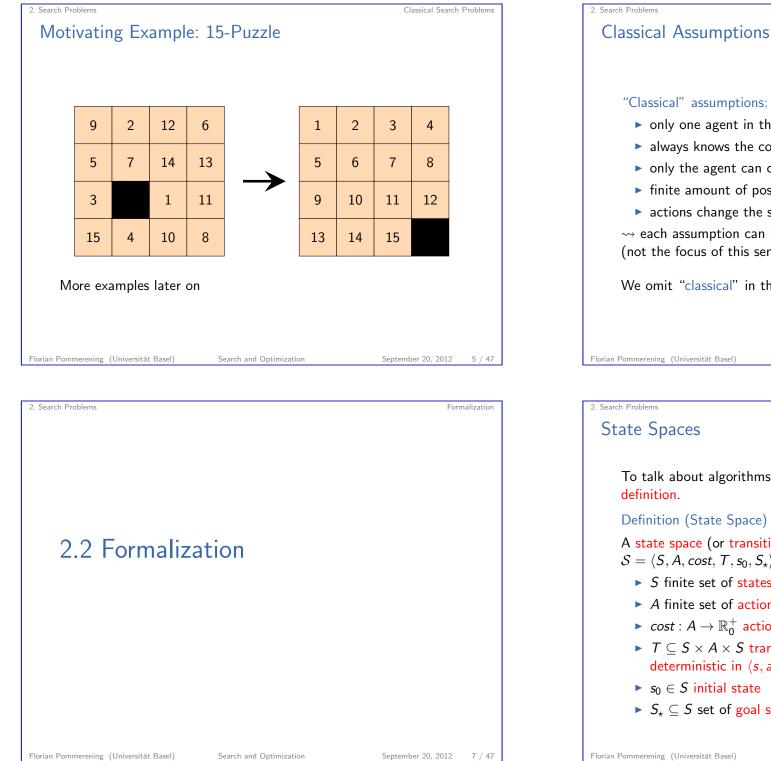


Seminar: Search ai September 20, 2012 — 2. S			
 2.1 Classical Sea 2.2 Formalization 2.3 Representat 2.4 Examples Blocks world Logistics Depot Driverlog Scanalyzer Sokoban Woodworking Satellite Rovers Elevators 			
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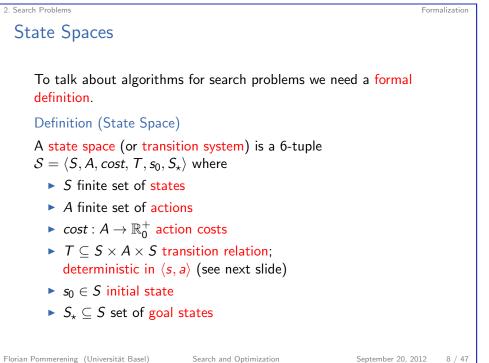


2. Search Problems

Classical Search Problems



"Classical" assumptions: only one agent in the environment (single agent) always knows the complete world state (full observability) only the agent can change the state (static) finite amount of possible states/actions (discrete) actions change the state deterministically ↔ each assumption can be generalized (not the focus of this seminar) We omit "classical" in the following.



State Spaces: Transitions, Determinism

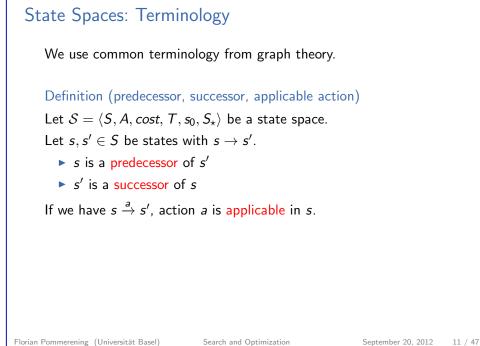
Definition (Transition, deterministic)

Let $S = \langle S, A, cost, T, s_0, S_* \rangle$ be a state space. The triples $\langle s, a, s' \rangle \in T$ are called transitions. We say S has the transition $\langle s, a, s' \rangle$ if $\langle s, a, s' \rangle \in T$ and write $s \xrightarrow{a} s'$ $(s \rightarrow s', \text{ if we do not care about } a)$. Transitions are deterministic in $\langle s, a \rangle$: $s \xrightarrow{a} s_1$ and $s \xrightarrow{a} s_2$ with $s_1 \neq s_2$ is not allowed.

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2. Search Problems



2. Search Problems

Formalizatio

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Formalization

State Space: Example

State spaces are often visualized as directed graphs.

states: nodes

- transitions: labeled edges (here: colors instead of labels)
- initial state: node marked with arrow
- goal states: marked (here: with ellipse)
- actions: edge labels
- action costs: given separately (or implicit = 1)
- paths to goal states correspond to solutions
- shortest paths correspond to optimal solutions

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Formalization

initial state

goal states

Formalization

State Spaces: Terminology We use common terminology from graph theory. Definition (path) Let $S = \langle S, A, cost, T, s_0, S_* \rangle$ be a state space. Let $s^{(0)}, \ldots, s^{(n)} \in S$ be states and $\pi_1, \ldots, \pi_n \in A$ actions, with $s^{(0)} \xrightarrow{\pi_1} s^{(1)} \cdots s^{(n-1)} \xrightarrow{\pi_n} s^{(n)}$ • $\pi = \langle \pi_1, \ldots, \pi_n \rangle$ is a path from $s^{(0)}$ to $s^{(n)}$ ▶ length of the path: $|\pi| = n$ • cost of the path: $cost(\pi) = \sum_{i=1}^{n} cost(\pi_i)$ Note: paths with length 0 are allowed • sometimes the state sequence $\langle s^{(0)}, \ldots, s^{(n)} \rangle$ or the sequence $\langle s^{(0)}, \pi_1, s^{(1)}, \ldots, s^{(n-1)}, \pi_n, s^{(n)} \rangle$ are also called path Florian Pommerening (Universität Basel) Search and Optimization September 20, 2012 12 / 47

State Spaces: Terminology

Additional terminology:

Definition (solution, optimal, solvable, reachable, dead end) Let $S = \langle S, A, cost, T, s_0, S_* \rangle$ be a state space.

- A path from a state s ∈ S to a state s_{*} ∈ S_{*} is a solution for/of s.
- A solution for s_0 is a solution for/of S.
- Optimal solutions (for s) have minimal cost among all solutions (for s).
- State space S is solvable if a solution for S exists.
- State s is reachable if there is a path from s_0 to s.

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State *s* is a dead end if no solution for *s* exists.

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Representation of State Spaces

Formalization

2. Search Problems

Representation of State Spaces

How to get the state space into the computer?

• As an explicit graph:

Nodes (states) and edges (transitions) represented explicitly, e. g. as adjacency lists or as adjacency matrix

- impossible for large problems (needs too much space)
- Dijkstra for small problems: $O(|S| \log |S| + |T|)$

As a declarative description:

- compact description as input
 state space exponentially larger than input
- algorithms work directly on compact description (e.g. reformulation, simplification of problem)

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2.3 Representation of State	e Spaces	
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Representation of State Spaces

2. Search Problems

How to get the state space into the computer?

As a black box: abstract interface for state spaces (used here)

abstract interface for state spaces

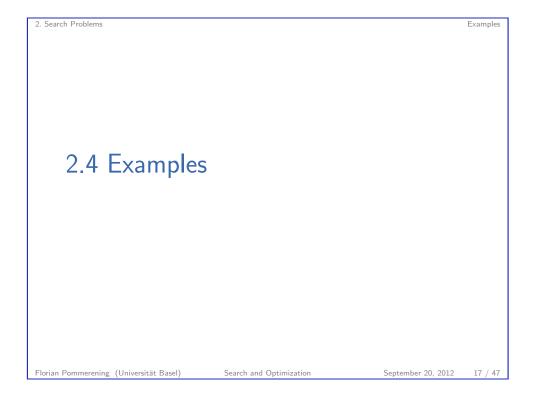
- State space $\mathcal{S} = \langle S, A, \textit{cost}, T, s_0, S_\star \rangle$ as black box:
 - init(): creates initial state Returns: the state s₀
 - is-goal(s): tests if state s is goal state Returns: true if s ∈ S_{*}; false otherwise
 - ▶ succ(s): lists all applicable actions and successors of s Returns: List of tuples (a, s') with $s \xrightarrow{a} s'$

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cost(a): determines action cost of action a Returns: the non-negative number cost(a)

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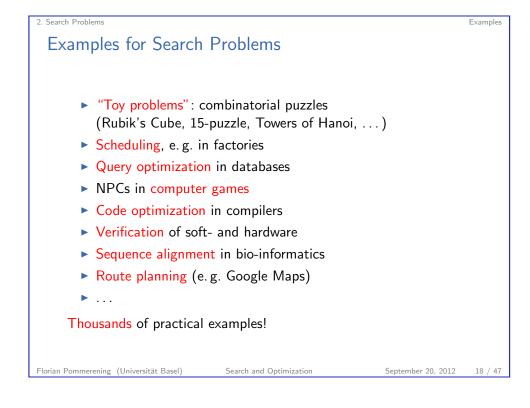
Representation of State Spaces

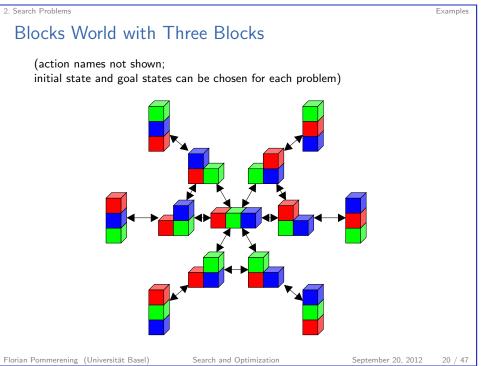


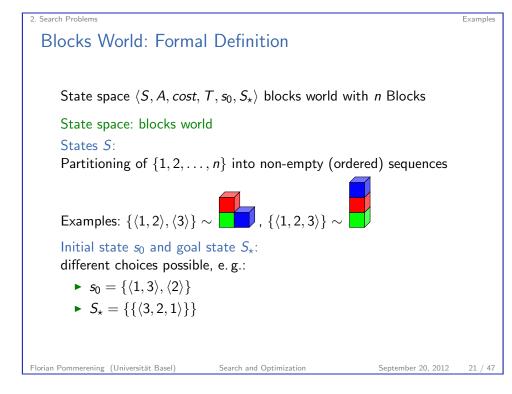
2. Search Problems

Example 1: Blocks world
The Blocks world is a traditional example problem in Al.
Task: blocks world
Some colored blocks are on a table.
They can be stacked to towers but only one block

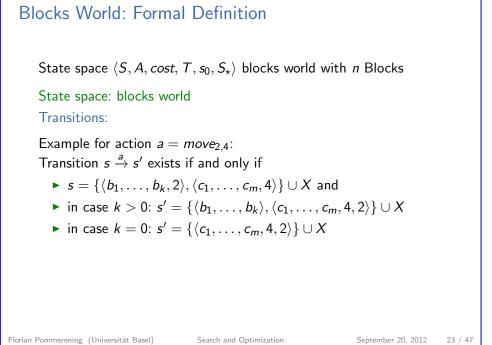
- They can be stacked to towers but only one block may be moved at a time.
- Our task is to reach a given goal configuration.







2. Search Problems



Search	Problems	

Blocks World: Formal Definition

State space $\langle S, A, cost, T, s_0, S_{\star} \rangle$ blocks world with *n* Blocks

State space: blocks world

Actions A:

- {*move*_{*b*,*b'*} | *b*, *b'* \in {1, ..., *n*} with *b* \neq *b'*}
 - Move block b on top of block b'.
 - Both have to be topmost block of a tower.
- { $totable_b \mid b \in \{1, \ldots, n\}$ }
 - ▶ Move block *b* on the table (~→ creates new tower).
 - ► Has to be topmost block of a tower.

Action costs cost:

cost(a) = 1 for all actions a

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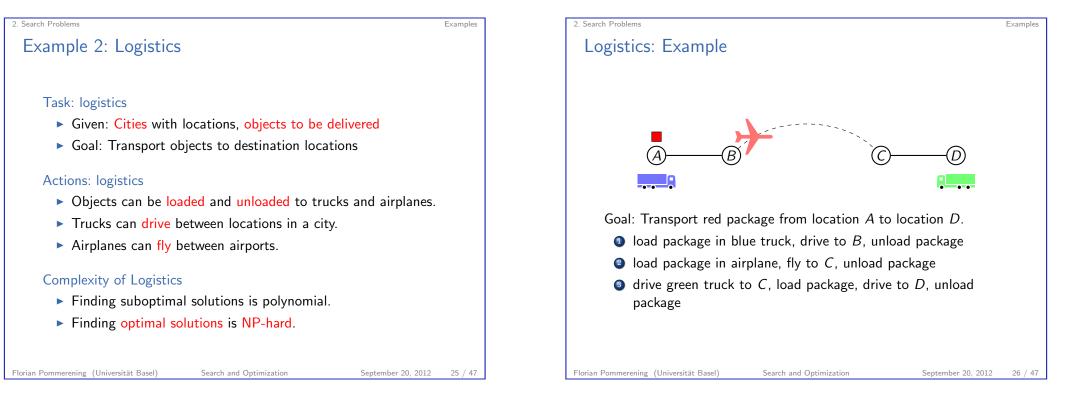
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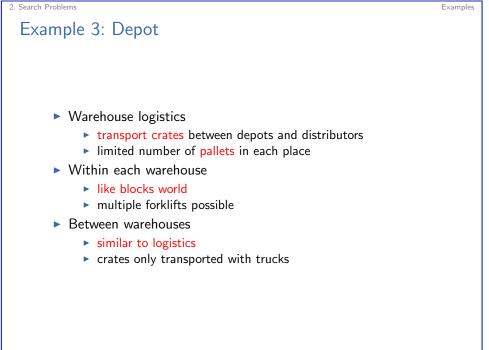
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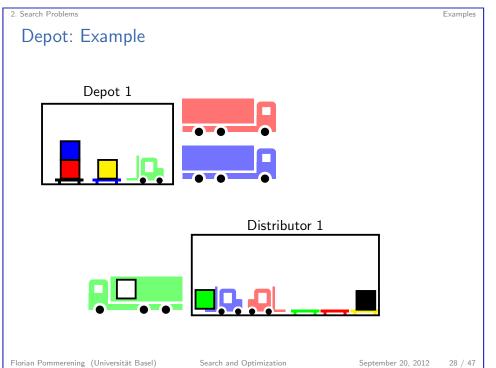
Examples

Blocks	States	Blocks	States					
1	1	10	58941091					
2	3	10	824073141					
3	13	12	12470162233					
4	73	13	202976401213					
5	501	14	3535017524403					
6	4051	15	65573803186921					
7	37633	16	1290434218669921					
8	394353	17	26846616451246353					
9	4596553	18	588633468315403843					
For every given initial state and goal state with n blocks								
simple algorithms can find solutions in $O(n)$ time. (How?)								

(for a compact problem representation).







Depot: Properties

Task: Depot

Satisfy goal properties, given an initial configuration of places, crates, and vehicles.

Different goals possible:

- enable access to a crate
- transport crates to Distributor
- rearrange crates
- combinations

Complexity of depot

- Can include blocks world subtask.
- ► ~→ Finding optimal solutions is also NP-hard

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Example

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2. Search Problems

Driverlog

Task: Driverlog

- Deliver packages to goal locations.
- Trucks and drivers can also have goal locations.

Actions: Driverlog

- Drivers can walk on footpaths.
- Drivers can board and leave trucks.
- Trucks with a driver can drive on streets.
- Packages can be loaded and unloaded into trucks.

Complexity of Driverlog

- Finding suboptimal solutions is polynomial.
- Finding optimal solutions is NP-hard.



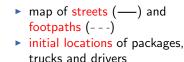


Example 4: Driverlog

- Another package delivery problem
- Path planning for drivers and trucks
- Given

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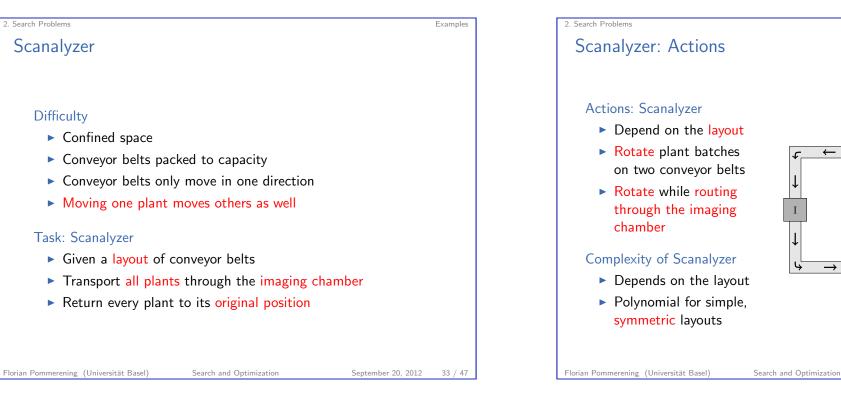
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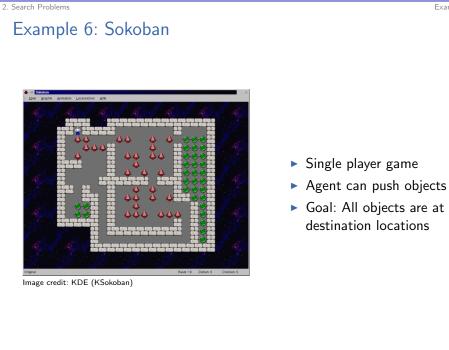
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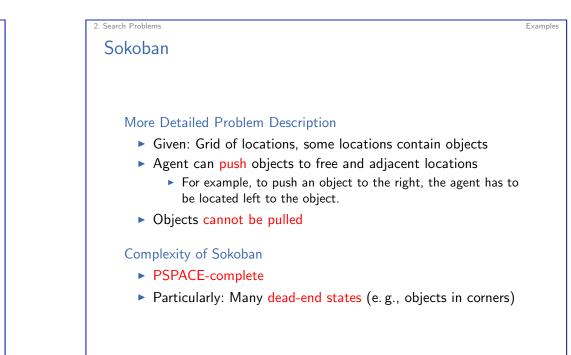
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Business application (LemnaTec)
Logistics for smart greenhouses
automated greenhouses with integrated imaging facilities
plants on conveyor belts

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Examples







Examples

 \leftarrow A \leftarrow

← B ←

 \leftarrow C \leftarrow

 \rightarrow D \rightarrow

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 \rightarrow E \rightarrow

 \rightarrow F \rightarrow

t

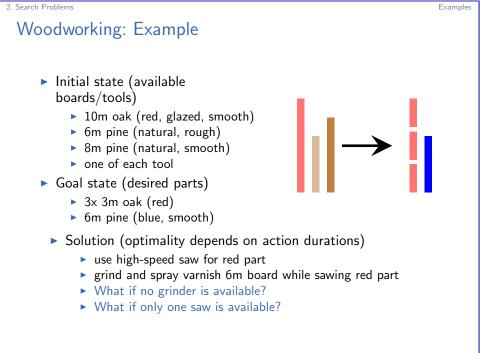
Example 7: Woodworking



- Use different tools to create parts with the correct
 - size (here: one dimensional)
 - color
 - material (pine, oak, mahogany, ...)
 - surface (smooth, rough, ...)
 - treatment (varnished, glazed, untreated, ...)
- Different tools can be used in parallel
- Minimize time to finish all parts

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2. Search Problems

Example

Woodworking

Available Tools

- Saws and high-speed saws
 - cut boards to size
 - dead ends possible by wrong cut
 - high-speed saws cut faster but need set-up time
- Grinders and planers
 - remove existing color and treatment
 - grinder leaves smoother surface
 - planer removes more material
- Glazers, immersion varnishers and spray varnishers
 - change color and treatment
 - color has to be available for this machine

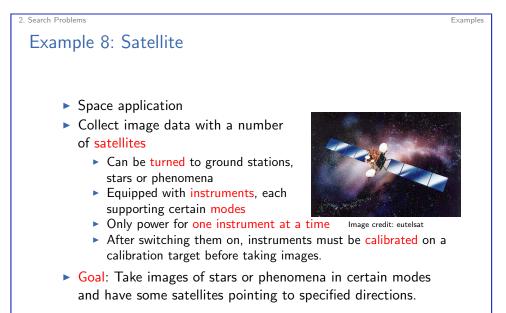
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mage Credit: GoRan

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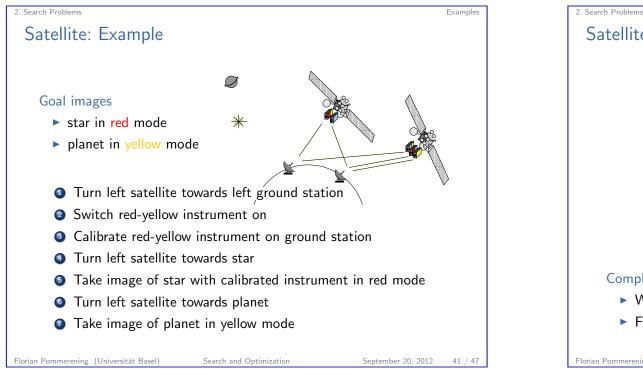
Example

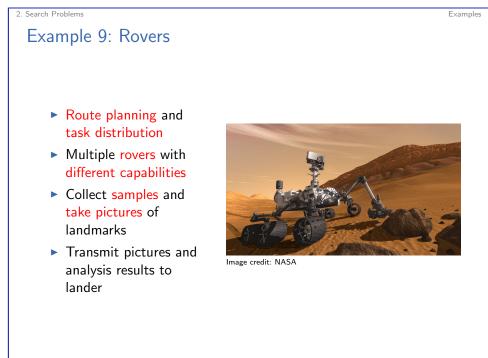


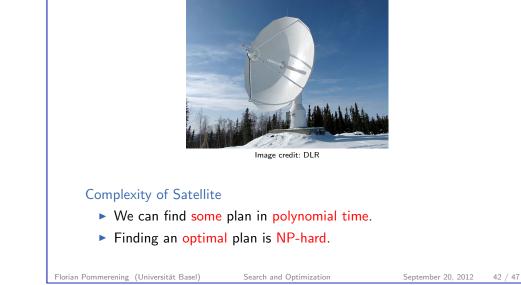
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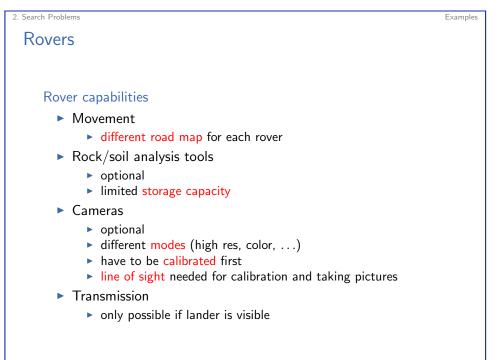
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Satellite: Properties



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Examples



Rovers

Examples

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2. Search Problems



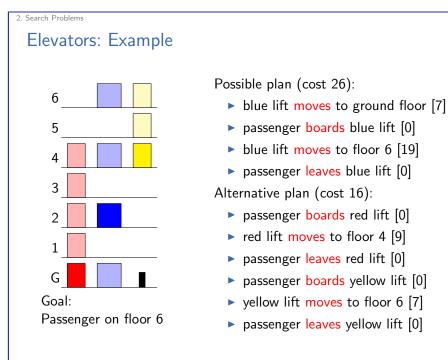
- Given a set of rovers with their equipment and road maps
- Collect all designated samples and pictures
- ► Transmit results back to lander

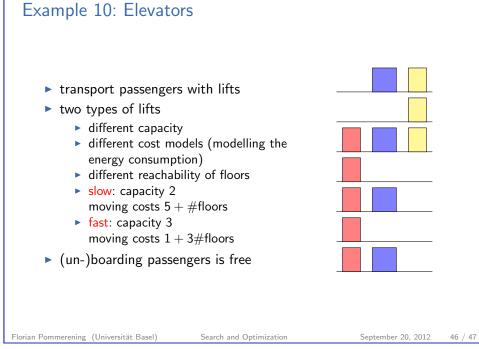
Complexity of Rovers

- Finding suboptimal solutions is polynomial.
- Finding optimal solutions is NP-hard.

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Examples

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