# Foundations of Artificial Intelligence 39. Automated Planning: The LM-cut Heuristic

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# Automated Planning: Overview

#### Chapter overview: automated planning

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- 38.-39. Planning Heuristics: Landmarks
  - 38. Landmarks
  - 39. The LM-cut Heuristic

## Formalism and Example

- As in the previous chapter, we consider delete-free planning tasks in normal form.
- We continue with the example from the previous chapter:

Example	
actions:	landmark examples:
• $a_1 = i \xrightarrow{3} x, y$	• $A = \{a_4\}$ (cost = 0)
• $a_2 = i \xrightarrow{4} x, z$	• $B = \{a_1, a_2\}$ (cost = 3)
• $a_3 = i \xrightarrow{5} y, z$	• $C = \{a_1, a_3\}$ (cost = 3)
• $a_4 = x, y, z \xrightarrow{0} g$	• $D = \{a_2, a_3\}$ (cost = 4)

# Finding Landmarks

# Justification Graphs

### Definition (precondition choice function)

A precondition choice function (pcf)  $P : A \rightarrow V$ maps every action to one of its preconditions.

### Definition (justification graph)

The justification graph for pcf P is a directed graph with labeled arcs.

- vertices: the variables V
- arcs:  $P(a) \xrightarrow{a} e$  for every action *a*, every effect  $e \in add(a)$

The LM-Cut Heuristic

Summary 00

### Example: Justification Graph

pcf P: 
$$P(a_1) = P(a_2) = P(a_3) = i$$
,  $P(a_4) = y$ 



### Cuts

### Definition (cut)

A cut in a justification graph is a subset C of its arcs such that all paths from i to g contain an arc in C.

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### Definition (cut)

A cut in a justification graph is a subset C of its arcs such that all paths from i to g contain an arc in C.

### Proposition (cuts are landmarks)

Let C be a cut in a justification graph for an arbitrary pcf.

Then the arc labels for C form a landmark.

proof idea:

- Consider the problem where all preconditions not picked by the pcf are ignored.
- Cuts are landmarks for this simplified problem.
- Hence they are also landmarks for the original problem.

#### Example

landmark  $A = \{a_4\}$  (cost = 0)



#### Example

landmark  $B = \{a_1, a_2\}$  (cost = 3)



#### Example

landmark  $C = \{a_1, a_3\}$  (cost = 3)



#### Example

landmark  $D = \{a_2, a_3\}$  (cost = 4)



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### Power of Cuts in Justification Graphs

• Which landmarks can be computed with the cut method?

# Power of Cuts in Justification Graphs

- Which landmarks can be computed with the cut method?
- all interesting ones!

Proposition (perfect hitting set heuristics)

Let  $\mathcal{L}$  be the set of all "cut landmarks" of a given planning task. Then  $h^{MHS}(I) = h^+(I)$  for  $\mathcal{L}$ .

 $\rightsquigarrow$  hitting set heuristic for  $\mathcal L$  is perfect.

proof idea:

• Show 1:1 correspondence of hitting sets *H* for *L* and plans, i.e., each hitting set for *L* corresponds to a plan, and vice versa.

# The LM-Cut Heuristic

### LM-Cut Heuristic: Motivation

- In general, there are exponentially many pcfs, hence computing all relevant landmarks is not tractable.
- The LM-cut heuristic is a method that chooses pcfs and computes cuts in a goal-oriented way.
- For planning tasks with uniform costs (i.e., cost(a) = 1 for all actions) it matches  $h^{\text{MHS-LP}}$  on the same set of landmarks.
- $\rightsquigarrow$  one of the best admissible planning heuristics

# LM-Cut Heuristic

### h<sup>LM-cut</sup> (Helmert & Domshlak, 2009)

Initialize  $h^{\text{LM-cut}}(I) := 0$ . Then iterate:

- Compute  $h^{\max}$  values of the variables. Stop if  $h^{\max}(g) = 0$ .
- Compute justification graph G for a pcf that chooses preconditions with maximal h<sup>max</sup> value. (Requires a tie-breaking policy.)
- Otermine the goal zone V<sub>g</sub> of G that consists of all vertices that have a zero-cost path to g.

Compute the cut L that contains the labels of all arcs v → v' such that v ∉ V<sub>g</sub>, v' ∈ V<sub>g</sub> and v can be reached from i without traversing a vertex in V<sub>g</sub>. It is guaranteed that cost(L) > 0.

- **Increase**  $h^{\text{LM-cut}}(I)$  by cost(L).
- Decrease cost(a) by cost(L) for all  $a \in L$ .













The LM-Cut Heuristic 000●

Summary 00

### Example: Computation of LM-Cut









# Summary

### Summary

• Cuts in justification graphs

are a general method to find landmarks.

- Hitting sets over all cut landmarks yield a perfect heuristic for delete-free planning tasks.
- The LM-cut heuristic is an admissible heuristic based on these ideas.