



We discuss three basic ideas for general heuristics:

- Delete Relaxation
- Abstraction
- ► Landmarks ~→ this and next chapter

Basic Idea: Landmarks landmark = something (e.g., an action) that must be part of every solution

Estimate solution costs based on unachieved landmarks.

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Delete Relaxation

38.1 Delete Relaxation

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- A: finite set of actions, where for every $a \in A$, we define
 - ▶ $pre(a) \subseteq V$: its preconditions
 - $add(a) \subseteq V$: its add effects
 - $cost(a) \in \mathbb{N}_0$: its cost

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denoted as pre(a) \xrightarrow{cost(a)} add(a) (omitting set braces)
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Landmarks and Delete Relaxation

- In this chapter, we discuss a further technique to compute planning heuristics: landmarks.
- We restrict ourselves to delete-free planning tasks:
 - For a STRIPS task Π , we compute its delete relaxed task Π^+ ,
 - and then apply landmark heuristics on Π^+ .
- Hence the objective of our landmark heuristics is to approximate the optimal delete relaxed heuristic h⁺ as accurately as possible.
- More advanced landmark techniques work directly on general planning tasks.

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Delete Relaxation





Delete Relaxation

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Landmarks

Example: Delete-Free Planning Task in Normal Form

Example

actions:

- $\blacktriangleright a_1 = i \xrightarrow{3} x, y$
- $\blacktriangleright a_2 = i \xrightarrow{4} x, z$
- ► $a_3 = i \xrightarrow{5} y, z$
- $\blacktriangleright a_4 = x, y, z \xrightarrow{0} g$

optimal solution to reach $\{g\}$ from $\{i\}$:

- ▶ plan: *a*₁, *a*₂, *a*₄
- cost: 3 + 4 + 0 = 7 (= $h^+(\{i\})$ because plan is optimal)

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Landmarks

Definition (landmark)
A landmark of a planning task ∏ is a set of actions L such that every plan must contain an action from L.
The cost of a landmark L, cost(L) is defined as min_{a∈L} cost(a).
→ landmark cost corresponds to (very simple) admissible heuristic
Speaking more strictly, landmarks as considered in this course are called disjunctive action landmarks.
other kinds of landmarks exist (fact landmarks, formula landmarks, ...)



38. Automated Planning: Landmarks Landmarks **Example:** Landmarks Example actions: $\blacktriangleright a_1 = i \xrightarrow{3} x, y$ \blacktriangleright $a_2 = i \xrightarrow{4} x, z$ ▶ $a_3 = i \xrightarrow{5} v. z$ $\blacktriangleright a_4 = x, y, z \xrightarrow{0} g$ some landmarks: $\blacktriangleright A = \{a_4\} \text{ (cost 0)}$ $\blacktriangleright B = \{a_1, a_2\} \text{ (cost 3)}$ \triangleright $C = \{a_1, a_3\}$ (cost 3) $\blacktriangleright D = \{a_2, a_3\} \text{ (cost 4)}$ ▶ also: $\{a_1, a_2, a_3\}$ (cost 3), $\{a_1, a_2, a_4\}$ (cost 0), ... Keller & F. Pommerening (University of B Foundations of Artificial Intelligence May 10, 2023 12 / 25

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Overview: Landmarks

in the following:

exploiting landmarks:

How can we compute an accurate heuristic for a given set of landmarks?

 \rightsquigarrow this chapter

finding landmarks:

How can we find landmarks?

 \rightsquigarrow next chapter

LM-cut heuristic:

an algorithm to find landmarks and exploit them as a heuristic \rightsquigarrow next chapter

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Exploiting Landmarks
Assume the set of landmarks L = {A, B, C, D}.
How to use L for computing heuristics?
sum the costs: 0 + 3 + 3 + 4 = 10 ~> not admissible!
maximize the costs: max {0, 3, 3, 4} = 4

- → usually yields a weak heuristic
- better: hitting sets or cost partitioning

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Exploiting Landmarks

38.3 Exploiting Landmarks

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Exploiting Landmarks

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Hitting Sets

Definition (hitting set)

given: finite support set X, family of subsets $\mathcal{F} \subseteq 2^X$, cost $c: X \to \mathbb{R}^+_0$

hitting set:

- ▶ subset $H \subseteq X$ that "hits" all subsets in \mathcal{F} : $H \cap S \neq \emptyset$ for all $S \in \mathcal{F}$
- cost of *H*: $\sum_{x \in H} c(x)$

minimum hitting set (MHS):

- hitting set with minimal cost
- "classical" NP-complete problem (Karp, 1972)

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Exploiting Landmarks

Landmarks

Example: Hitting Sets

Example

 $X = \{a_1, a_2, a_3, a_4\}$ $\mathcal{F} = \{A, B, C, D\}$ with $A = \{a_4\}, B = \{a_1, a_2\}, C = \{a_1, a_3\}, D = \{a_2, a_3\}$

 $c(a_1) = 3$, $c(a_2) = 4$, $c(a_3) = 5$, $c(a_4) = 0$

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minimum hitting set: \{a_1, a_2, a_4\} with cost 3 + 4 + 0 = 7
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Exploiting Landmarks

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Hitting Sets for Landmarks

idea: landmarks are interpreted as instance of minimum hitting set

Definition (hitting set heuristic)

Let \mathcal{L} be a set of landmarks for a delete-free planning task in normal form with actions A, action costs *cost* and initial state I.

The hitting set heuristic $h^{\text{MHS}}(I)$ is defined as the minimal solution cost for the minimum hitting set instance with support set A, family of subsets \mathcal{L} and costs *cost*.

Proposition (Hitting Set Heuristic is Admissible)

The minimum hitting set heuristic h^{MHS} is admissible.

Why?

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Approximation of $h^{\rm MHS}$

- As computing minimal hitting sets is NP-hard, we want to approximate h^{MHS} in polynomial time.
- Solving the LP-relaxation of the IP is possible in polynomial time and gives a lower bound.

Definition $(h^{\text{MHS-LP}})$		
$Minimize \sum_{a \in A} u_a \cdot cost(a) \text{ subject to}$		
$\sum_{a\in L} u_a \geq 1$	for all $L\in\mathcal{L}$	
$u_a \in \mathbb{R}^+$	for all $a \in A$	
Originally expressed in a different form as optimal cost partitionin (Karpas & Domshlak, 2009).		

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38. Automated Planning: Landmarks Relationship of Heuristics Proposition (h^{MHS-LP} vs. h^{MHS}) Let \mathcal{L} be a set of landmarks for a planning task with initial state 1. Then $h^{MHS-LP}(1) \leq h^{MHS}(1) \leq h^+(1)$ 38. Automated Planning: Landmarks

Example: $h^{\text{MHS-LP}}$

Exploiting Landmarks

Example

 $cost(a_1) = 3$, $cost(a_2) = 4$, $cost(a_3) = 5$, $cost(a_4) = 0$ $\mathcal{L} = \{A, B, C, D\}$ with $A = \{a_4\}$, $B = \{a_1, a_2\}$, $C = \{a_1, a_3\}$, $D = \{a_2, a_3\}$

LP:

Minimize $3u_{a_1} + 4u_{a_2} + 5u_{a_3} + 0u_{a_4}$ subject to

$u_{a_4} \geq 1$	$(\rightsquigarrow A)$	
$u_{a_1}+u_{a_2}\geq 1$	$(\rightsquigarrow B)$	
$u_{a_1}+u_{a_3}\geq 1$	$(\rightsquigarrow C)$	
$u_{a_2}+u_{a_3}\geq 1$	$(\rightsquigarrow D)$	
$u_{oldsymbol{a}_i} \in \mathbb{R}^+$	for $i \in \{1, 2, 3, 4\}$	
optimal solution:		
$u_{a_1} = 0.5, \ u_{a_2} = 0.5, \ u_{a_3} = 0.5, \ u_{a$	$_{4} = 1 \rightsquigarrow h^{\text{MHS-LP}}(I) = 6$	
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Exploiting Landmarks

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Summary

Summary

- Landmarks are action sets such that every plan must contain at least one of the actions.
- Hitting sets yield the most accurate heuristic for a given set of landmarks, but the computation is NP-hard.
- With LP-relaxation we get a polynomial approach for the computation of informative landmark heuristics.

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