Foundations of Artificial Intelligence
17. State-Space Search: IDA*

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## State-Space Search: Overview

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### 17.2 IDA*: Algorithm

The main drawback of the presented best-first graph search algorithms is their space complexity.
Idea: use the concepts of iterative-deepening DFS

- bounded depth-first search with increasing bounds
- instead of depth we bound $f$
(in this chapter $f(n):=g(n)+h\left(n\right.$.state) as in $\mathrm{A}^{*}$ )
$\rightsquigarrow I D A *^{*}$ (iterative-deepening $A^{*}$ )
- tree search, unlike the previous best-first search algorithms


First Attempt: IDA* Main Function
first attempt: iterative deepening A $^{*}$ (IDA*)
IDA* (First Attempt)
for $f_{-}$bound $\in\{0,1,2, \ldots\}$ :
solution := f_bounded_search(init(), 0,f_bound)
if solution $\neq$ none:
return solution
function f_bounded_search $\left(s, g, f_{-}\right.$bound $)$:
if $g+h(s)>f_{-}$bound:

## return none

if is_goal(s):
return $\rangle$
for each $\left\langle a, s^{\prime}\right\rangle \in \operatorname{succ}(s)$ :
solution := f_bounded_search $\left(s^{\prime}, g+\operatorname{cost}(a), f_{-}\right.$bound $)$
if solution $\neq$ none:
solution.push_front(a)

## return solution

return none
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- The pseudo-code can be rewritten to be even more similar to our IDDFS pseudo-code. However, this would make our next modification more complicated.
- The algorithm follows the same principles as IDDFS, but takes path costs and heuristic information into account.
- For unit-cost state spaces and the trivial heuristic $h: s \mapsto 0$ for all states $s$, it behaves identically to IDDFS.
- For general state spaces, there is a problem with this first attempt, however.


## Growing the $f$ Bound

## Setting the Next $f$ Bound

idea: let the $f$-bounded search compute the next sensible $f$ bound

- Start with $h($ init() ), the smallest $f$ bound
that results in a non-empty search tree.
- In every round, increase the $f$ bound to the smallest value that ensures that in the next round at least one additional path will be considered by the search.
$\rightsquigarrow$ f_bounded_search now returns two values:
- the next $f$ bound that would include at least one new node in the search tree ( $\infty$ if no such bound exists; none if a solution was found), and
- the solution that was found (or none).
final algorithm：iterative deepening $\mathrm{A}^{*}$（IDA＊）


## IDA＊

f＿bound $=h($ init（）$)$
while $f_{-}$bound $\neq \infty$ ：
$\left\langle f_{-}\right.$bound，solution $\rangle=\mathrm{f}_{-}$bounded＿search（init（）， $0, f_{-}$bound）
if solution $\neq$ none：
return solution
return unsolvable
function f＿bounded＿search $\left(s, g, f_{-} b o u n d\right)$ ：
if $g+h(s)>f_{-}$bound：
return $\langle g+h(s)$ ，none $\rangle$
if is＿goal（ $s$ ）：
return $\langle$ none，$\rangle\rangle$
new＿bound $:=\infty$
for each $\left\langle a, s^{\prime}\right\rangle \in \operatorname{succ}(s)$ ：
$\langle$ child＿bound，solution $\rangle:=$ f＿bounded＿search $\left(s^{\prime}, g+\operatorname{cost}(a), f_{-} b o u n d\right)$ if solution $\neq$ none：
solution．push＿front（a）
return $\langle$ none，solution〉
new＿bound $:=\min ($ new＿bound，child＿bound）
return 〈new＿bound，none〉


| IDA＊：Properties |  |  |  |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| Inherits important properties of $A^{*}$ and depth－first search： <br> semi－complete if $h$ safe and $\operatorname{cost}(a)>0$ for all actions a <br> optimal if $h$ admissible <br> space complexity $O(\ell b)$ ，where <br> $\ell$ ：length of longest generated path （for unit cost problems：bounded by optimal solution cost） $b$ ：branching factor |  |  |  |
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IDA*: Discussion
$\rightarrow$ compared to $A^{*}$ potentially considerable overhead because no duplicates are detected
$\rightsquigarrow$ exponentially slower in many state spaces
$\rightsquigarrow$ often combined with partial duplicate elimination (cycle detection, transposition tables)

- overhead due to iterative increases of $f$ bound often negligible, but not always
- especially problematic if action costs vary a lot: then it can easily happen that each new $f$ bound only considers a small number of new paths


### 17.4 Summary



